Introduction

This paper is intended to benefit the person faced with the occasional task of designing gas insulated high-voltage structures or spark gaps and who must decide upon the proper geometry, spacings, gas type, and pressure for reliable voltage-holding. Generally, the data available to an occasional designer of high-voltage shielding structures is scattered throughout a number of references. The designer is often uncertain as to whether or not the presented data applies to his case, how it will scale if such parameters as materials, dimensions, or pressure are changed, and what factors affect the accuracy of the data. A consistent design approach has been in use by high-voltage specialists for years, but seems to be unfamiliar to many others. This approach is presented below along with a summary of how various factors affect voltage breakdown. The design procedures described apply to situations where the influence of nearby insulators is negligible. The accuracy of the data is estimated to be within 10 to 15%, a value usually attained in practice only when one follows the cautionary advice discussed in the paragraphs on materials preparation, gas properties, and conditioning.

Uniform and Enhanced Fields

If two infinite, plane, conducting electrode surfaces are parallel, are separated by a distance \( X \), and have a potential difference between them of \( V \), then everywhere between them there exists a three-dimensionally uniform electric field that can be expressed as

\[
E = \frac{V}{X}.
\]

(1)

(Throughout this paper, \( E \) will have the units of \( \text{V/cm} \).) In this case, \( E \) is the maximum field anywhere in the system. For properly prepared conductors at less than 2 to 3 atm pressure, the maximum field value corresponding to breakdown is only a property of the insulating gas medium and not the type of metal used in the electrodes. For most practical cases, fields are not everywhere uniform and, in fact, are almost always higher at a conductor surface than anywhere in the gaseous insulating medium. For example, in the case of a sphere separated from a plane, the field is higher at the surface of the sphere than elsewhere in the system. The field at the sphere is called an enhanced field and the sphere is referred to as the enhanced electrode. At ordinary pressures, the amount of enhancement is only dependent on the geometry of the electrode system and not on such parameters as pressure or the type of gas. For any generalized system of two electrodes separated by a distance \( X \), at their point of closest approach, we can define

\[
E_{\text{mean}} = \frac{V}{X}.
\]

(2)

and

\[
f^* = \frac{E_{\text{max}}}{E_{\text{mean}},}
\]

(3)

where \( f^* \) is defined as the field enhancement factor and is equal to the ratio of the maximum field anywhere, \( E_{\text{max}} \), to \( E_{\text{mean}} \). Values of \( f^* \) for a number of common geometries are plotted in Figs. 1 through 6. These curves are extremely useful in the design of anti-corona shields.

Figures 1 and 2 are plots of calculated data. The reference to "One Sphere Grounded" refers to the case where one sphere is grounded to one wall of an enclosing conducting box that is spaced several sphere diameters away from the pair of spheres. Figure 3 data was measured in an electrolytic field plotting tank for a corona shield.

The relative electric strength of the most common insulating gases at atmospheric pressure and in near-uniform fields is as follows:

<table>
<thead>
<tr>
<th>GAS</th>
<th>( V/\text{Air} )</th>
<th>( N_2 )</th>
<th>( CO_2 )</th>
<th>( SF_6 )</th>
<th>Freon 12 ( (CF_2) )</th>
<th>Freon 114 ( (CF_3) )</th>
<th>Freon 116 ( (CF_4) )</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>1.6</td>
<td>1.1</td>
<td>0.95</td>
<td>0.6</td>
<td>2.5-3.0</td>
<td>2.3-2.5</td>
<td>2.6</td>
</tr>
</tbody>
</table>

The absolute electric strength of a gas in uniform fields as a function of pressure, temperature, and separation is described by Paschen's law, which can be written as follows for air

\[
E_{\text{max}} = \frac{V}{X} = \left( \frac{203}{T} \right) \left( \frac{p}{760} \right) \left( \frac{1}{X} \right)^{0.68} \sqrt{\frac{298}{T} \frac{X}{760}}
\]

(4)

where \( X \) is separation in cm, \( p \) is pressure in Torr, \( T \) is temperature in \( \text{K} \).

Avoiding Corona

In most gases at pressures of less than 2 to 3 atm, it has been found that breakdown occurs, without having gone through a period of high voltage. Also, no significant difference in voltage is observed as the polarity of the applied voltage is reversed. Breakdown occurs when the basic electric strength of the insulating gas medium is exceeded; this usually takes place first at the surface of the enhanced electrode, initiating the full discharge. At high \( f^* \) values, with applied voltage higher than the corona threshold, strong polarity effects are observed; breakdown voltage is lower with a positive enhanced electrode. Breakdown voltage becomes almost totally dependent on the spacing and very insensitive to the shape of the enhanced electrode. For certain conditions, the breakdown voltage is observed to decrease with increasing pressure. To avoid these effects and the production of ozone (in the case of an air medium) or other deleterious chemical effects, the designer almost always strives to satisfy the criterion \( f^* < 5 \).
and $E_{\text{max}}$ is the breakdown field [not to be confused with the generalized maximum field referred to in Eq. (2)]. Equation (8) agrees very well with experimental data and is plotted in Figs. 7 and 8. Note that the often quoted value of 30 kV/cm for the electric strength of air strictly applies only to a 1 cm separation.

The effect of altitude of $E_{\text{max}}$ for air is governed by the change in air density. A plot of $E_{\text{max}}$ vs altitude is shown in Fig. 9. Paschen's law is observed to fail at pressures $\geq 120$ psi, for air; $E_{\text{max}}$ then varies $\propto 10^{-3}$. $E_{\text{max}}$ is plotted vs pressure for air and sulphur hexafluoride (SF$_6$) in Fig. 10. This figure reveals a common phenomenon at higher pressures; namely, the significant influence of electrode material has on $E_{\text{max}}$. It also shows that N$_2$ becomes progressively poorer than air at higher pressures.

SF$_6$ is completely non-toxic under ordinary conditions but slowly decomposes in the presence of continuous open arcs. The breakdown products have been analyzed and are highly toxic and corrosive. However, one should not decide against its use solely because of these factors. The breakdown products can be completely removed by flowing the gas through activated alumina. For most applications involving only infrequent sparking and relatively small quantities of the gas, simple venting outside a building is a common practice. SF$_6$ is very commonly used in pressurized spark gaps for switching high-energy systems. It has been found very important to dry the SF$_6$ and avoid any trace of oils in order to obtain predictable, repeatable results in spark gap applications.

Figure 11 shows $E_{\text{max}}$ vs percent fill for mixtures of SF$_6$ in N$_2$ and Freon 12 in air. Both are in common usage. The approximately 2:3:1 mixture of Freon 12 over air has been found to hold at least up to its liquefaction point ($\approx 75$ psig at 23°C). It is cheaper than SF$_6$ but has the disadvantage of forming conductive carbon deposits in the presence of arcing. It is therefore only suitable when there is infrequent sparking, and not at all for spark gaps. The rapid improvement in $E_{\text{max}}$ with a small addition of SF$_6$ to N$_2$ is striking. Except where recovery of gas is planned, there is rarely justification for increasing the SF$_6$ percentage beyond 25 or 30%. Pressure reductions below $10^{-3}$ cm Hg cause the arcs to burn 20-25% lower values of $E_{\text{max}}$ than does air at the same pressure for pressures of 100 to 300 psig. At high pressures, the overall area of the electrodes strongly affects $E_{\text{max}}$. Figure 12 shows this dependence for N$_2$ and N$_2$-CO$_2$ mixtures.

It is important to realize that even at voltages as low as a few kilovolts, sharp edges and/or closely spaced projections can produce large field enhancements, causing $E_{\text{max}}$ to be exceeded and leading to breakdown.

**Miscellaneous Effects**

For sinusoidal CW applied voltage, breakdown voltage steadily decreases with frequency. The reduction levels off at $\sim 18$ to 20% at 61 kHz and remains essentially unchanged throughout the RF and microwave regions. For ac, the peak value of the voltage waveform is the correct one to use for shielding design purposes.

For pulsed voltage application times less than a few microseconds, time-dependent processes result in values of $E_{\text{max}}$ that increase as the pulse width is decreased. In air, for a constant separation at atmospheric pressure, the permissible uniform field value of $E_{\text{max}}$ increases a factor of $\approx 3$ as pulse width is reduced from 1 usec to 1 nsec (where statistical breakdown lags are eliminated by using that free electrons are readily available). Plots of $E_{\text{max}}/P$ vs $P$ for short-pulse dc and microwave frequencies between 1 and 27 GHz, for numerous gases, are given in references 15 and 16. Here, $P$ is the maximum allowable pulse width and equals the format of the arc breakdown. Design relations have been developed which permit precision design of spark gaps operated in the nanosecond regime with non-sinusoidal waveforms, and which have repeatable, predictable breakdown times, even with high $f^2$ values.

Breakdown voltage increases with humidity by an amount that is relatively independent of electrode shapes. However, it is strongly dependent on the type and geometry of insulators present and on polarity at high values of field enhancement. Generally, one can expect variations in breakdown voltage to be $\approx 10$ to 15% over normal ranges of relative humidity. The presence of water condensation on electrode surfaces can reduce breakdown voltages by 50 to 80%, compared to that of dry surfaces. Oil has a slightly smaller effect. If present on insulator surfaces, water can cause large reductions in breakdown voltage.

Whenever possible, new systems should be conditioned by allowing sparking to occur at a low energy value (typically in the $10^{-5}$ to $10^{-1}$ joule range). Now spark gaps typically require $\approx 50$ to 500 shots to become conditioned up to a reliable, repeatable breakdown voltage level. It frequently is more difficult to fully condition anti-corona shields but the same principles apply. To shorten the conditioning process, or to increase the likelihood of a shield design performing as it theoretically should, electrode surfaces should be smooth, polished, and clean. For the rare occasions where a is necessary, use of electrodes with $f^2 = 1$ (for field enhancement), Rowgowski-profile electrodes can be used. This design achieves the $f^2 = 1$ condition with the minimum electrode extent. Cleanliness is essential to good performance. All fingerprints, oils, dust and other contaminants should be removed. Alcohol or Freon-type solvents are commonly used for this purpose. When the application is a pressurized spark gap, the conditioning should be performed at a pressure near the maximum value anticipated. A curve of breakdown voltage vs pressure is usually plotted, averaging many readings for each point, and is very useful in establishing changing operating points.

Such gases as helium and hydrogen at temperatures near their liquefaction points (4.2°K and 20°K, respectively) have higher values of $E_{\text{max}}$ than air at room temperatures. Data for several gases at small and large separations are given in references (21) and (22).

**Design Philosophy and Procedure**

At the outset of a design, a decision should be made as to what safety factor is desired between the maximum operating level and the breakdown level. This is defined as:

$$a = \frac{V_{\text{operate, max}}}{V_{\text{breakdown}}} = \frac{V_{\text{OP}}}{V_{\text{BD}}} (a \leq 1)$$

For indoor research apparatus, $a$ is typically in the 0.3 to 0.8 range, depending on the required reliability, shielding costs, and how undesirable are the consequences of occasional breakdown. Well-designed spark gaps for switching large, short-pulsed systems have a very low prefire probability and low jitter in breakdown voltage when $a$ is $\approx 0.85$. Most spark gaps operated at $a \leq 0.7$ to 0.75 display acceptable spurious breakdown rates when operated under dc or CW conditions.

Next, the designer should recognize that nearly all shielding requirements encountered can be well approximated by and designed according to the geometries of figures 3 to 6 and the subsequent data presented above.

The third point to be made is that the final design should be tested (and conditioned) if at all possible.
verify the design. At voltages $>100$ kV, being overly cautious in choosing a can result in large shields that are more expensive than necessary. Also the cost of hipot power supplies may be excessive.

Finally, we recall that the maximum field anywhere (normally at an enhanced electrode) cannot exceed the value of $E_{\text{max}}$ for the gas medium under the conditions employed. Setting this value of $E_{\text{max}}$ equal to the first equality in (4), and combining with (6) yields

$$f^* = \frac{a X E_{\text{max}}}{v_{\text{op}}}$$  \hspace{1cm} (7)

where $E_{\text{max}}$ is the near-uniform field value obtainable from Figs. 6 through 12. Usually there is only one unknown in (7) so that most practical problems may be solved. Examples of common problems include solving for the required shield diameter, given the quantities on the right hand of (7), or solving for the required pressure in a specific gas, given a fixed geometry, operating voltage, and $a$-value.

For often-encountered geometries and gases, the foregoing procedures can be used to plot more specialized but easily referenced data. An example of this is the useful plot of Fig. 13 (in this case based on an empirical relation which fits experimental data).\textsuperscript{23}

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References

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