

ОБЪЕДИНЕННЫЙ
ИНСТИТУТ
ЯДЕРНЫХ
ИССЛЕДОВАНИЙ
ДУБНА



SU7700910

E2 - 9273

R.P.Zaikov, V.Tcholakov

All

**INFINITE-COMPONENT CONFORMAL FIELDS.
SPECTRAL REPRESENTATION
OF THE TWO-POINT FUNCTION**

1975

RANGE OF JINR PUBLICATIONS

The preprints and communications of the Joint Institute for Nuclear Research (JINR) are considered to be original publications. They are published in accordance with Article 4 of the JINR Statute. Difference between the preprints and communications consists in that text of the preprint will be published in future in one of scientific journals or in aperiodic collections.

Indexing

The preprints, communications and deposited publications of the JINR have a single numbering (four last figures of the index).

The first sign of the index - a letter, denotes the language the paper is published in:

"P" - published in Russian;

"E" - published in English;

"D" - published both in Russian and in English.

The figure following the letter denotes the subject category of the given publication. List of subject categories of the JINR publications is sent periodically to the recipients.

Above-described index is placed in the right upper corner of the cover and on the title-page of each publication.

References

In bibliographical references to the JINR preprints and communications we recommend to indicate: author's initials and name, an abbreviation of the name of the institute, index, place and year of publication.

An example of bibliographical reference:

I. Ivanov. JINR, P2-4985, Dubna, 1971.

E2 - 9273

R.P.Zaikov,* V.Tcholakov*

**INFINITE-COMPONENT CONFORMAL FIELDS.
SPECTRAL REPRESENTATION
OF THE TWO-POINT FUNCTION**

Submitted to Bulgarian Journal of Physics.

* Present address: Higher Pedagogical
Institute, Schumen, Bulgaria.

1. Introduction

As a rule, one considers the finite-component conformal fields ¹⁻³. These fields are transformed according to representations of class Ia or Ib given by Mack and Salam ⁴, i.e., when the generators of special conformal transformations acting on the spin variables are represented by nilpotent operators or trivially. In those cases the stability subgroup of the conformal group has finite-dimensional representations.

In the cases of conformal invariant operator product expansion, or of the conformal invariant partial wave expansions of Green functions ⁵, we deal with infinite dimensional representations of the conformal group (with respect to its stability subgroup).

In this paper we consider the fields which are transformed according to the representations of class II ⁴, i.e., when the generators of the special conformal group acting on the spin variables are represented in a nontrivial way. In that case the representations of stability subgroup are essentially infinite-dimensional. To specify the irreducible representations of the conformal group $SO(4,2)$ we use its Casimir operators ⁶⁻⁹. The unitary irreducible representations of the conformal group are given in papers ⁶⁻⁸.

The conformal invariant spectral representation of the two-point function for the fields with arbitrary integer spin, which are transformed according to any irreducible representations of $SO(4,2)$ group, is obtained. The case of half integer spin may be considered analogously.

2. Irreducible Representations of Conformal Group

Consider the fields $\Phi(x; \xi)$ which have the following transformation properties with respect to the conformal group

$$U(\Lambda) \Phi(x; \xi) U(\Lambda)^{-1} = \Phi(\Lambda x; \Lambda \xi), \quad (2.1)$$

where $\Lambda \in \text{SO}(4, 2)$ and $\xi \in \mathbb{C}^4$ here $\mathbb{C}^4 = \{\xi_\mu \mid \xi^2 = 0, \xi \in G\}$ is the future light cone.

In the infinitesimal form the transformation law (2.1) has the form:

$$\begin{aligned} [P_\mu, \Phi(x; \xi)] &= i \frac{\partial}{\partial x^\mu} \Phi(x; \xi), \\ [M_{\mu\nu}, \Phi(x; \xi)] &= -i(x_\mu \frac{\partial}{\partial x^\nu} - x_\nu \frac{\partial}{\partial x^\mu}) \Phi(x; \xi) + \Sigma_{\mu\nu} \Phi(x; \xi), \\ [D, \Phi(x; \xi)] &= (i x^\nu \frac{\partial}{\partial x^\nu} + \Lambda) \Phi(x; \xi), \\ [K_\mu, \Phi(x; \xi)] &= -i(2x_\mu x^\nu \frac{\partial}{\partial x^\nu} - x^2 \frac{\partial}{\partial x^\mu} - 2i x^\nu (g_{\mu\nu} \Lambda + \Sigma_{\mu\nu})) \Phi(x; \xi) \\ &\quad + \epsilon k_\mu \Phi(x; \xi), \end{aligned} \quad (2.2)$$

where $\epsilon = 0$ for the "fundamental" tensor fields and $\epsilon = 1$ for any other fields. The operators

$$\begin{aligned} \Sigma_{\mu\nu} &= -i(\xi_\mu \frac{\partial}{\partial \xi^\nu} - \xi_\nu \frac{\partial}{\partial \xi^\mu}), \\ \Lambda &= i(d + \xi^\nu \frac{\partial}{\partial \xi^\nu}), \\ k_\mu &= 2i \xi_\mu (d + \xi^\nu \frac{\partial}{\partial \xi^\nu}), \end{aligned} \quad (2.3)$$

are generators of the stability subgroup of the conformal group, i.e., the subgroup which leaves $x = 0$.

It is well known that the conformal group has three independent Casimir operators

$$\begin{aligned} \hat{C}_{II} &= \frac{1}{2} J_{AB} J^{AB}, \\ \hat{C}_{III} &= \frac{1}{48} E_{ABCDEF} J^{AB} J^{CD} J^{EF}, \\ \hat{C}_{IV} &= J_{AB} J^{BC} J_{CD} J^{CA}, \end{aligned} \quad (2.4)$$

where $(A, B, \dots = 0, 1, 2, 3, 5, 6)$ and

$$\begin{aligned} J_{\mu\nu} &= M_{\mu\nu} + J_{5\mu} \frac{1}{2} (P_{\nu} - K_{\nu}), \\ J_{6\mu} &= \frac{1}{2} (P_{\mu} + K_{\mu}), \quad J_{65} = D. \end{aligned} \quad (2.5)$$

The fields which transform according to arbitrary irreducible representations of the conformal group are given as a solution of the following system of eqs.

$$[C_k, \Phi(x; \xi)] = c_k \Phi(x; \xi) \quad (k = II, III, IV), \quad (2.6)$$

where c_k are the eigenvalues of the corresponding Casimir operators. For the "tensor" representations $c_{III} = 0$, i.e., in our case any unitary irreducible representation is labelled by the pair of real parameters $\lambda = c_{II}, c_{IV}$. Substituting (2.2) and (2.3) into (2.6), we have

$$\begin{aligned} [\hat{C}_{II}, \Phi(x; \xi)] &= \{ d(d-4) - 2(d-1) \xi^{\mu} \frac{\partial}{\partial x^{\mu}} + 2(d-1) \xi^{\mu} \frac{\partial}{\partial x^{\mu}} \} \xi^{\nu} \frac{\partial}{\partial \xi^{\nu}} \\ &+ 2 \xi^{\mu} \xi^{\nu} \frac{\partial^2}{\partial \xi^{\mu} \partial \xi^{\nu}} \} \Phi(x; \xi), \end{aligned} \quad (2.7)$$

$$[\hat{C}_{III}, \Phi(x; \xi)] = 0, \quad (2.8)$$

$$|C_{IV}, \Phi(x; \xi)| = |d(d-4)(d-2)^2 + 4(d-2)(d-4)| - \epsilon d_1 \xi^\mu \frac{\partial}{\partial x^\mu} + (d - \epsilon \xi^\mu \frac{\partial}{\partial x^\mu}) \xi^\nu \frac{\partial}{\partial \xi^\nu} + \xi^\mu \xi^\nu \frac{\partial^2}{\partial \xi^\mu \partial \xi^\nu} | \Phi(x; \xi), \quad (2.9)$$

where $\epsilon = 0$ for the "fundamental" fields and $\epsilon = 1$ for any other fields. In our case k_μ are not nilpotent operators and, consequently, the corresponding representations of the stability subgroup are infinite-dimensional.

3. Two-Point Function for the Irreducible Fields

Consider the two-point function

$$F^{[X_1, X_2]}(x_1, \xi_1; x_2, \xi_2) = \langle 0 | \Phi(x_1; \xi_1, X_1) \Phi(x_2, \xi_2, X_2) | 0 \rangle, \quad (3.1)$$

where the fields $\Phi(x, \xi, X)$ transform according to an arbitrary "tensor" representation of the conformal group $X = \{c_{II}, c_{IV}\}$. We consider as well, the conventional "fundamental" tensor fields ($\epsilon = 0$) and any "nonfundamental" fields. The conformal invariance for the two-point function (3.1) is

$$F^{[X_1, X_2]}(\Lambda x_1, \Lambda \xi_1; \Lambda x_2, \Lambda \xi_2) = F^{[X_1, X_2]}(x_1, \xi_1; x_2, \xi_2), \quad (3.2)$$

where $\Lambda = SO(4, 2)$.

From (2.7) and (2.9) it follows that it is convenient to pass to the momentum space. Taking into account the translational invariance and spectrum condition, we have

$$F^{[X_1, X_2]}(x_1 - x_2; \xi_1, \xi_2) = \int d^4 p \Theta(p) e^{-ip(x_1 - x_2)} \times F^{[X_1, X_2]}(p; \xi_1, \xi_2), \quad (3.3)$$

where $\Theta(p) = \theta(p^0) \theta(p^2)$ is the characteristic function of the future cone, and $\bar{F}^{[X_1, X_2]}(p; \xi_1, \xi_2)$ is the kernel of the two-point function.

From the irreducibility conditions for the fields (2.6) there follow the corresponding conditions for the two-point function and consequently for its kernel $\bar{F}^{[X_1, X_2]}(p; \xi_1, \xi_2)$, i.e., one has

$$(\hat{C}_k^a - c_k^a) \bar{F}^{[X_1, X_2]}(p; \xi_1, \xi_2) = 0, \quad (k = 1, 2), \quad (3.4)$$

(k = II, IV).

From (2.7), (2.8), (2.9), (3.3) and (3.4) we have the following system of partial differential equations

$$\{d^a(d^a - 4) + 2i\epsilon(3/2 - a)d_1^a p\xi^a + 2[d^a + i\epsilon(3/2 - a)p\xi^a] \cdot \xi_a^{1'} \frac{\partial}{\partial \xi_a^{1'}} + 2\xi_a^{\mu} \xi_a^{1'} \frac{\partial^2}{\partial \xi_a^{\mu} \partial \xi_a^{1'}} - c_{II}^a \bar{F}^{[X_1, X_2]}(p; \xi_1, \xi_2) = 0, \quad (3.5)$$

$$\{d^a(d^a - 4)(d^a - 2)^2 + 4(d^a - 4)(d^a - 2)[i\epsilon(3/2 - a)p\xi^a + (d_1^a + i\epsilon(3/2 - a)p\xi^a) \xi_a^{1'} \frac{\partial}{\partial \xi_a^{1'}} + \xi_a^{\mu} \xi_a^{1'} \frac{\partial^2}{\partial \xi_a^{\mu} \partial \xi_a^{1'}}] - c_{IV}^a \bar{F}^{[X_1, X_2]}(p; \xi_1, \xi_2) = 0 \quad (a = 1, 2), \quad (3.6)$$

where $\epsilon(a) = 0$ for the "fundamental" fields and $\epsilon(a) = \Theta(a) - \Theta(-a)$ for any other fields.

Let us write down eqs. (3.5) and (3.6) in terms of relativistically invariant variables $p^2, p\xi^a = z^a$ and

$$w = 1 - \frac{p^2(\xi^1 \xi^2)}{(p\xi^1)(p\xi^2)}. \quad \text{Then we have}$$

$$\{d^n(d^n-4) + 2i\epsilon(3/2-a)d_1^n z_n + 2\{d^n + i\epsilon(3/2-a)z_n\}z_n \frac{\partial}{\partial z_n} + 2z_n^2 \frac{\partial^2}{\partial z_n^2} - c_{11}^n \{F^{[X_1, X_2]}(p^2, z_n, w) = 0, \quad (3.7)$$

$$\{d^n(d^n-4)(d^n-2)^2 + 4(d^n-i)(d^n-2)\{i\epsilon(3/2-a)z_n + (d^n + i\epsilon(3/2-a)z_n)z_n \frac{\partial}{\partial z_n} + z_n^2 \frac{\partial^2}{\partial z_n^2}\} - c_{1V}^n \{F(p^2, z_n, w) = 0 \quad (3.8)$$

The solutions of the system of partial differential eqs. (3.7) and (3.8) may be written down in the form

$$F^{[X_1, X_2]}(p^2, z_n, w) = f^{[X_1, X_2]}(p^2, w) z_1^{r_1} z_2^{r_2} \cdot t_{r_1}^{X_1}(z_1) t_{r_2}^{X_2}(z_2), \quad (3.9)$$

where $f^{[X_1, X_2]}(p^2, w)$ are arbitrary functions (which will be determined from the dilatation and special conformal invariance) and $t_{r_i}^{X_i}(z_i)$ are solutions of the following differential equation

$$\{z_n \frac{d^2}{dz_n^2} + [d^n + 2i\epsilon + i\epsilon(3/2-a)z_n] \frac{d}{dz_n} + i\epsilon(3/2-a) - \lambda\} t_{r_n}^{X_n} = 0. \quad (3.10)$$

Consider, first, the case of the "fundamental" fields. In that case the solution of eq. (3.10) ($\epsilon = 0$) is given by

$$U_1(z) = c_1 + c_2 z^{1-d-2r} \quad (3.11)$$

where c_1 and c_2 are arbitrary constants.

For "nonfundamental" fields ($r \neq 0$) the solutions of eq. (3.10) are the degenerate hypergeometrical functions. If $d^a + 2r^a$ is noninteger, the general solution of (3.10) is

$$U_a^{\lambda}(z_a) = A_a \Phi(d_1^a, \dots, d^a + 2r^a; i_1(3/2-a)z_a) + \\ + B_a |i_1(3/2-a)z_a|^{-d^a-2r^a} \Psi(d_1^a-d^a-r^a, 2-d^a-2r^a; \\ i_1(3/2-a)z_a) \quad (a=1, 2). \quad (3.12)$$

For $d^a + 2r^a$ integer the general solution of eq. (3.10) has the form

$$U_a^{\lambda}(z_a) = A_a \Psi(d_1^a, \dots, d^a + 2r^a; i_1(3/2-a)z_a) + \\ + B_a |i_1(3/2-a)z_a|^{-d^a-2r^a} \Psi(d^a-d_1^a-r^a, d^a+2r^a; -i_1(3/2-a)z_a), \quad (3.13)$$

where Ψ are the Tricomi functions

The functions $\Phi(a, c, x)$ and $x^{1-c}\Phi(a-c, 2-c, x)$ as well as $\Psi(a, c, x)$ and $c^x\Psi(c-a, c, -x)$ give the non-equivalent representations labeling with the same numbers $X = |c_H|, c_{IV} = 1$.

The functions Ψ are connected with Φ by the following relations

$$\Psi(a, c, x) = \frac{\Gamma(1-c)}{\Gamma(a-c+1)} \Phi(a, c, x) + \\ + \frac{\Gamma(c-1)}{\Gamma(a)} x^{1-c} \Phi(a-c+1, 2-c, x).$$

The functions Φ and Ψ have the following integral representations

$$\Phi(a, c; x) = \frac{\Gamma(c)}{\Gamma(a)\Gamma(c-a)} \int_0^1 du e^{-ux} u^{a-1} (1-u)^{c-a-1},$$

$$\operatorname{Re} c > \operatorname{Re} a > 0,$$

and

$$\Psi(a, c; x) = \frac{1}{2\pi i} \int_{\gamma-i\infty}^{\gamma+i\infty} \frac{\Gamma(a+s)\Gamma(-s)\Gamma(1-c-s)}{\Gamma(a)\Gamma(a-c+1)} x^s ds,$$

where $-\operatorname{Re} a \leq \gamma \leq \min(0, 1-\operatorname{Re} c)$.

Consider now in more detail the case when $a = -n$ with n integer. In this case $d_1^0 = d_2^0 = -n$, the degenerate hypergeometrical function Φ transforms into the Lagere polynomials, i.e., in this case the solutions of eq. (3.10) are

$$\begin{aligned} \Gamma_{\pm n}^{\pm} = & A_n'' L_n^{d_1^0, 2\nu_n^{\pm}}(i\epsilon(3/2-a)z_n) + B_n'' |i\epsilon(3/2-a)z_n|^{1-d_1^0-2\nu_n^{\pm}} \\ & \times \Phi(-n-d_1^0-2\nu_n^{\pm}, 2-d_1^0-2\nu_n^{\pm}, i\epsilon(3/2-a)z_n). \end{aligned} \quad (3.14)$$

The Lagere polynomials satisfy the following differential equations

$$x \frac{d^2}{dx^2} + (a-x+1) \frac{d}{dx} + n L_n^a(x) = 0 \quad (3.15)$$

and are connected with the functions Φ as follows

$$L_n^a(x) = \frac{\Gamma(n+a+1)}{n!\Gamma(a+1)} \Phi(-n, a+1, x).$$

The numbers ν are related to the eigenvalues of the Casimir operators c_{II} and c_{IV} via the following relations

$$c_{II} = (\rho_1 + 2)^2 + (\rho_2 + 1)^2 - 5, \quad (3.16)$$

$$c_{1V} = (\rho_1 + 2)^2 |(\rho_1 + 2)^2 - 2(\rho_2 + 1)^2 + 1| + (\rho_2 + 1)^2 |(\rho_2 + 1)^2 + 1|, \quad (3.17)$$

where we use the following labelling:

$$\rho_1 = d + i - 4, \quad \rho_2 = i. \quad (3.18)$$

For the unitary representations of the conformal group, following [11], we have the following cases

$$\begin{aligned} 1) \quad & \rho_1 = -2 + i\sigma_1, \quad \rho_2 = -1 + i\sigma_2 \\ & 0 < \sigma_1 < \infty, \quad 0 < \sigma_2 < \infty \\ 2) \quad & -1 < \rho_2 < 1, \quad \sigma = 0 \\ 3) \quad & \text{Im} \rho_1 = \text{Im} \rho_2 = 0. \end{aligned} \quad (3.19)$$

From (3.9) and (3.16) it follows that in any case (3.19) there are both "fundamental" and "nonfundamental" fields transforming according to some irreducible representations which are specified by the same pair of numbers $\lambda = [\sigma_1, \sigma_2]$. In such a manner we have generalized the theorem of Gatto et al. [11] to the case of any representations of conformal group.

4. Conformal Invariant Two-Point Kernel

The kernel (3.9) will be conformally invariant if the following equations [3]

$$D\tilde{F}(p^2, z_a, w) = 0, \quad (4.1)$$

$$K_\mu \tilde{F}(p^2, z_a, w) = 0,$$

are satisfied, where D and K_{μ} are the generators of dilatations and special conformal transformations acting on the two-point function. Following paper ³, we have that the solution of eqs. (4.1) exists only for

$$\lambda_1 = \lambda_2 \quad (4.2)$$

and they are given by

$$E^{|\lambda_1 - \lambda_2|} (p^2, z_a, w) = N^{\lambda} (p^2)^{d-2} z_1^{\lambda} z_2^{\lambda} t^{\lambda} (z_1) t^{\lambda} (z_2) \\ \sum_{s=0}^{\infty} \frac{(2s+1) \Gamma(\Gamma-s-2) \Gamma(d-s-1) \Gamma(d-s-2)}{\Gamma(\Gamma-s+1)} P_s(w),$$

where $P_s(w)$ is the Legendre polynomials.

From (4.3) it follows that the two-point function exists when either both the fields are "fundamental" or one is "fundamental", or both the fields are "nonfundamental".

In any case of unitary representations of $SO(1,2)$ the kernel (4.3) is positively defined, but is local only when $\Gamma - \lambda$ is positive integer number.

Acknowledgement:

One of the authors (R.P.Z.) is indebted to Dr. D.T. Stoyanov for stimulating interest and to Profs. D.I. Blokhintsev and V.A. Mescherjakov for hospitality kindly extended to him at the Laboratory of Theoretical Physics of JINR, Dubna, where the present paper was completed.

References

1. A.A. Migdal. *Phys.Lett.*, 37B, 98 (1971); 37B, 386 (1971).
2. G.Mack and I.T.Todorov. *Phys.Rev.*, D8, 1764(1973).
3. R.P.Zaikov. *Bulg. J.Phys.*, 2, 89 (1975).
4. G.Mack and A.Salam. *Ann.Phys.*, 53, 174 (1969).

5. I. T. Todorov, *Preprint, CERN T4 1646, Geneva, 1973.*
6. T. Yao. *J. Math. Phys.*, 8, 1931(1967); 9, 1615 (1968); 12, 315 (1971);
7. А. Н. Лезнов, Н. А. Федосеев. *ТМФ*, 5, 191 /1970/.
8. Macfadyen. *J. Math. Phys.*, 12, 1436 (1971); 14, 57 (1973); 14, 638 (1973).
9. J. Lopuszanski and Z. Oziewicz. *Conformally Invariant Equation of the Quantum Field Theory. Preprint Wroclaw (1974).*
10. I. T. Todorov and R. P. Zaikov. *J Math. Phys.*, 10, 2014 (1969).
11. S. Ferrara et al. *Ann. Phys.*, 76, 161 (1973).

Received by Publishing Department
on October 31, 1975.

Subject Categories of the JINR Publications

Index	Subject
1.	High energy experimental physics
2.	High energy theoretical physics
3.	Low energy experimental physics
4.	Low energy theoretical physics
5.	Mathematics
6.	Nuclear spectroscopy and radiochemistry
7.	Heavy ion physics
8.	Cryogenics
9.	Accelerators
10.	Automatization of data processing
11.	Computing mathematics and technique
12.	Chemistry
13.	Experimental techniques and methods
14.	Solid state physics. Liquids.
15.	Experimental physics of nuclear reactions at low energies.
16.	Health physics. Shieldings
17.	Theory of condensed matter.

Will you fill blank spaces in your library?

You can receive by post the books listed below. Prices - in US \$,
including the packing and registered postage

D1-5969	Proceedings of the International Symposium on High Energy Physics. Dresden, 1971.	773pg	10.00
D-6004	Binary Reactions of Hadrons at High Energies. Dubna, 1971.	768 pg	12.59
D10-6142	Proceedings of the International Symposium on Data Handling of Bubble and Spark Chambers. Dubna, 1971.	564 pg	9.96
D13-6210	Proceedings of the Vth International Symposium on Nuclear Electronics. Warsaw, 1971.	372 pg	6.36
D1-6349	Proceedings of the IVth International Conference on High Energy Physics and Nuclear Structure. Dubna, 1971.	670pg	9.92
D-6465	International School on Nuclear Structure. Alushta, 1972.	525 pg	9.54
D- 6840	Proceedings of the Second International Symposium on High Energy and Elementary Particle Physics (Strbske Pleso, CSSR, 1972).	398 pg	6.78
D2-7161	Proceedings of the III International Seminar on Non-Local Quantum Field Theory. Alushta, 1973.	280 pg	5.00
D12-7111	Deep Inelastic and Many-Body Processes. Dubna, 1973.	507 pg	8.76
D13-7616	Proceedings of the VII International Symposium on Nuclear Electronics. Budapest, 1973.	372 pg	5.62
D12-7612	Proceedings of the International School of Young Physicists on High Energy Physics. Gomel, 1973.	623 pg	10.53
D10-7707	Meeting on Programming and Mathematical Methods for Solving the Physical Problems. Dubna, 1973.	564 pg	8.23

D1,2-7781	Proceedings of the III International Symposium on High Energy and Elementary Particle Physics. Sibiu, Romania, 1973.	478pg 7.29
D3-7991	Proceedings of the II International School on Neutron Physics. Alushta, 1974.	554pg 4.35
D1,2-8405	Proceedings of the IV International Symposium on High Energy and Elementary Particle Physics. Varna, 1974.	376pg 3.89
D10,11-8450	International School on Use of Computers in Nuclear Research. Tashkent, 1974.	465 pg 4.52
P1,2-8529	The International School-Seminar of Young Scientists. Actual Problems of Elementary Particle Physics. Sochi, 1974.	582 pg 4.70
	Proceedings of the VI European Conference on Controlled Fusion and Plasma Physics. Moscow, 1973. v.1.	666 pg 21.00
	Proceedings of the VI European Conference on Controlled Fusion and Plasma Physics. Moscow, 1973. v. II	466 pg 15.00

Orders for the above-mentioned books can be sent at the address:
Publishing Department, JINR
Head Post Office, P.O. Box 79
101000 Moscow, USSR.



Conditions of Exchange

The preprints and communications of the Joint Institute for Nuclear Research are distributed free of charge on the mutual exchange basis to the universities, institutes, libraries, scientific groups of more than 50 countries.

Besides the regular distribution on the exchange basis, the Publishing Department fulfils annually about 4000 individual requests for our preprints and communications. The index of our publication must be obligatory indicated in such requests.

Addresses

Letters on all the questions concerning the exchange of publications as well as requests for individual publications are to be sent at the address:

*Publishing Department
Joint Institute for
Nuclear Research
Head Post Office,
P.O. Box 79
101000 Moscow,
U.S.S.R.*

We kindly ask to send all the publications on the exchange basis and also free of charge subscriptions to scientific journals at the address:

*Scientific-Technical Library
Joint Institute for
Nuclear Research
Head Post Office
P.O. Box 79
101000 Moscow,
U.S.S.R.*

Издательский отдел Объединенного института ядерных исследований.
Заказ 20653, Тираж 680. Уч.-изд. листов 0,73.
Редактор Э.В.Ивашкевич Подписано к печати 10.12.75 г.
Корректор Н.А.Курьева