

70,72,74,76Ge(d,<sup>3</sup>He)69,71,73,75Ga

réactions at 26 MeV

-----  
G. ROTBARD, G. LA RANA, M. VERGNES  
G. BERRIER, J. KALIFA

I. P. N. - 91405 Orsay, France

G. GUILBAUT, R. TAMISIER

Institut de Physique de Nantes, BP 1644.

44-Nantes - France

IPND PhN 76-64

$^{70,72,74,76}\text{Ge}(d,^3\text{He})^{69,71,73,75}\text{Ga}$  reactions at 26 MeV

G. Rotbard, G. La Rana\*, M. Vergnes, G. Barrier, J. Kalifa  
Institut de Physique Nucléaire 91406 Orsay, France

-----  
G. Guilbaut, R. Tamisier  
Institut de Physique de Nantes, BP 1044, 44 Nantes - France

#### Abstract

The  $^{70,72,74,76}\text{Ge}(d,^3\text{He})^{69,71,73,75}\text{Ga}$  reactions have been studied at 26 MeV with 15 keV resolution (F.W.H.M), using the Orsay MP tandem accelerator and a split pole magnetic spectrometer. The spectroscopic factors are determined for 15 levels in  $^{69}\text{Ga}$  and 11 levels in each of the 3 other Ga isotopes. Level schemes are proposed for the practically unknown  $^{73}\text{Ga}$  and  $^{75}\text{Ga}$ . Very simple model wave functions previously proposed for Ge nuclei are seen to reproduce quite well the measured occupation numbers for the proton orbitals. Anomalies in these occupation numbers are observed between  $Z = 31$  and  $32$  and between  $N = 40$  and  $42$ , this last one corresponding to the structural transition observed recently in a comparison of the (p,t) and (t,p) reactions. These anomalies could be related to changes in the nuclear shape.

## I. Introduction

The structure of the nuclei in the region of neutron number  $N = 40$  is still a subject of controversy. The occurrence of a low-lying  $0^+$  excited state in the even-even nuclei is interpreted either in terms of neutron configuration mixing in the  $2p_{1/2}$ ,  $1g_{9/2}$  orbitals<sup>1)</sup> or in terms of proton configuration mixing in the  $2p_{3/2}$ ,  $1f_{5/2}$  orbitals<sup>2,3)</sup> or even in terms of shape coexistence<sup>4)</sup>. Some discontinuities observed at  $N = 40$  in systematic studies of even-even nuclei in this region by means of ( $^3\text{He},d$ )<sup>2)</sup>, ( $d,^3\text{He}$ )<sup>5)</sup>, ( $p,t$ )<sup>6)</sup> and ( $t,p$ )<sup>7)</sup> reactions, appear as an evidence for a structural transition between the  $N=40$  and  $N=42$  ground states. The primary aim of the present work is to test the possible influence of this transition on the occupation numbers of the proton shell model orbitals in the ground states of the even-even isotopes. These occupation numbers could in principle be deduced from the number of holes measured<sup>8)</sup> as the sum of the spectroscopic factors in the  $\text{Ge}(^3\text{He},d)\text{As}$  reactions. However the number of protons being appreciably smaller than the number of proton holes in the valence shells ( $2p$ ,  $1f_{5/2}$ ), a direct measurement by means of the  $\text{Ge}(d,^3\text{He})\text{Ga}$  reaction is expected to give more reliable values. In the case of the reaction on the two lightest Ga isotopes, the spin and parity of the levels of the final Ga nuclei are well known and there is no difficulty to distribute the  $l = 1$  strength between  $2p_{1/2}$  and  $2p_{3/2}$  and the  $l=3$  strength between  $1f_{5/2}$  and  $1f_{7/2}$ . The two heaviest Ga isotopes,  $^{73}\text{Ga}$  and  $^{75}\text{Ga}$ , are however practically unknown and the second aim of this work is to obtain spectroscopic informations on these nuclei.

## 2. Experimental procedure

The Orsay ME<sup>3</sup> tandem Van de Graaff accelerator was used to provide a  $1\mu\text{A}$  beam of 26 MeV deuterons on  $\text{GeO}_2$  targets. The thicknesses and isotopic enrichments of these targets are given in table 1. A split pole magnetic spectrometer equipped with four solid state position sensitive detectors (50 mm long) in its focal plane was used for analysis and detection of the emitted  $^3\text{He}$  particles. The experimental set-up described in previous papers<sup>2,5,6)</sup> has been improved by the installation of remotely operated, quickly removable beam defining slits, at the entrance of the reaction chamber. This improvement was necessary at forward angles to avoid edge scattering of deuterons during

the experiment, the magnetic rigidity of the deuterons of the beam being larger than that of the detected  $^3\text{He}$  particles. It was possible in this way to measure the cross sections at angles as small as  $8^\circ$ .

Typical spectra are given in figure 1. The overall resolution is 15 keV (F.W.H.M). Comparison of spectra permits the identification of contaminant groups originating from the other isotopes. The absolute cross sections are estimated with an uncertainty of the order of 20%, mainly due to the uncertainty in the determination of the target thicknesses (using a gauge). A relative normalization of the cross sections on different isotopes was obtained using a natural Ge target.

### 3. Analysis of the data.

#### 3.1. Excitation energies and Q values.

The presence on the same spectra of groups of  $^3\text{He}$  originating from different isotopes permits the measurement of the difference of Q values with an accuracy estimated to lie between  $\pm 7$  keV. Table 2 shows that the measured Q values are in agreement with those reported by H. Wapstra and K. Bos<sup>9)</sup> and improve the accuracy of the known Q values for the heaviest isotopes. The accuracy of the measured excitation energies is also estimated to be within  $\pm 7$  keV.

#### 3.2. D.W.B.A. analysis, choice of the optical potentials.

The angular distributions are shown in figures 2 to 5. D.W.B.A. calculations were carried out using the program DWUCK<sup>10)</sup>. Optical model parameters previously used for the analysis of the ( $^3\text{He},d$ ) reaction in the Ge-Ga region<sup>2,8,11)</sup> fail to fit consistently the whole set of experimental results: The Q value varies from isotope to isotope and the kinetic energy of the outgoing  $^3\text{He}$  particles approaches the coulomb barrier for the heaviest isotopes. There is then a dependence of the angular distribution on the isotope and on the excitation energy. The dependence on the isotope is larger in the calculated angular distributions than in the experimental ones. For instance the potentials which gave good fits for the  $^{69,71}\text{Ga}(^5\text{He},d)^{70,72}\text{Ge}$  reactions<sup>2)</sup> give also good fits for the inverse  $^{70,72}\text{Ge}(d,^3\text{He})^{69,71}\text{Ga}$  reactions, but

poorer fits for the reactions on the heaviest Ge isotopes. The potential from Bechetti and Greenlees<sup>12)</sup>, for  $^3\text{He}$  contains a  $(N-Z)/A$  dependant term and gives, associated with the potential from Perey and Perey<sup>13)</sup> for deuterons (see table 3), a rather good fit for the whole set of experimental results. All the spectroscopic factors given in tables 4 to 7 have been extracted using these potentials. (The potentials of ref.2 give about the same results for  $^{69,71}\text{Ga}$ ).

#### 4. Spectroscopic results for the Ga isotopes.

The spectroscopic results deduced from the DWBA analysis are presented in tables 4 to 7. The transferred angular momentum  $l$  and the spectroscopic factor  $C^2S_{lj}$  have been determined for 15 levels in  $^{69}\text{Ga}$ , 11 levels in  $^{71}\text{Ga}$ , 11 levels in  $^{73}\text{Ga}$  and 11 levels in  $^{75}\text{Ga}$ . The excitation energy, spin and parity were previously known for most of the levels observed in  $^{69}\text{Ga}$  (14) and  $^{71}\text{Ga}$  (15). The spectroscopic factors are practically the only new information obtained. However the  $l = 3$  pattern of the angular distributions corresponding to the 2425 keV level in  $^{69}\text{Ga}$  and to the 1907 and 1995 keV levels in  $^{71}\text{Ga}$  limits the previously unknown spin and parity value to  $J^\pi = 5/2^-$  or  $7/2^-$ . The value  $J^\pi = 7/2^-$  is preferred because :

i) The total  $2p, 1f5/2$  spectroscopic sum rule limit is already reached with the sum of the spectroscopic factors for levels known as  $J^\pi = 1/2^-, 3/2^-$  and  $5/2^-$ . Levels of unknown spin, with large  $l = 3$  spectroscopic factors, as is the case for the levels discussed, should therefore have the spin-parity value  $J^\pi = 7/2^-$ .

ii) These levels have not been observed in the  $^{68,70}\text{Zn}(^3\text{He}, d)^{69,71}\text{Ga}$  reactions<sup>11)</sup>. That can be explained easily if  $J^\pi = 7/2^-$  because the  $F7/2$  proton orbital is essentially full in the Zn ground states. (Which is not the case for the  $f5/2$  orbital).

The value  $J^\pi = 7/2^-$  is also preferred, for the same reasons, for the 1396 keV level of  $^{71}\text{Ga}$ , already known as  $J^\pi = 5/2^-$  or  $7/2^-$ . The arguments are weaker for the 1476 keV level of  $^{71}\text{Ga}$ , because the spectroscopic factor is smaller.

The two heaviest Ga isotopes studied were, until very recently, practically unknown. For  $^{73}\text{Ga}$ , Three  $\gamma$  rays were observed<sup>16)</sup> in the  $^{73}\text{Zn} \rightarrow ^{73}\text{Ga}$  beta decay. Other informations have been deduced<sup>7)</sup> from the shapes of the angular distributions in the  $^{71}\text{Ga}(t,p)^{72}\text{Ga}$  reaction. Levels with  $L = 0$  pattern in the  $(t,p)$  reaction have necessarily the same spin and parity,  $J^\pi = 3/2^-$ , as the  $^{71}\text{Ga}$  ground state. This is the case for the ground state and the levels at 214 and 912 keV. The level at 1112 keV is the only one corresponding to an  $l = 1$  transfer in the  $(d,^3\text{He})$  reaction (which limits the spin-parity value to  $J^\pi = 1/2^-$  or  $3/2^-$ ) and to a transfer  $L \neq 0$  in the  $(t,p)$  reaction. Accordingly the value  $J^\pi = 1/2^-$  is preferred, but  $3/2^-$  cannot be completely excluded. We have no way to make a choice between  $J^\pi = 5/2^-$  or  $7/2^-$  for the low-lying levels at 198 and 495 keV populated by  $l=3$  transfer. The value  $J^\pi = 5/2^-$  is preferred from a comparison with the level schemes of the lighter Ga isotopes (see figure 6). This argument could seem weak, but it is buttressed by the fact that the strength of the two  $l=3$  transitions corresponding to these levels adds nicely to the measured  $l=1$  strength to give a value of 4.07, very close to the sum rule limit of 4 for the  $2p, 1f_{5/2}$  valence shells. Other higher lying levels with large spectroscopic factors, corresponding to  $l=3$  transfer, are supposed to have  $J^\pi = 7/2^-$ .

Excitation energies for 3 levels of  $^{75}\text{Ga}$  have been deduced by Aleklett et al<sup>17)</sup> from the  $\gamma$  rays observed in the  $^{75}\text{Zn} \rightarrow ^{75}\text{Ga}$  beta decay. Their 228 keV level corresponds to the second excited level of  $^{75}\text{Ga}$ , observed in the  $(d,^3\text{He})$  reaction at 232 keV. The region where the proposed 432 and 606 keV levels of  $^{75}\text{Ga}$  should appear is obscured at forward angles in the  $^{76}\text{Ge}(d,^3\text{He})^{75}\text{Ga}$  reaction by the very intense peak of the  $^{16}\text{O}(d,^3\text{He})^{15}\text{N}_{g.s.}$  reaction. Very weak peaks, possibly corresponding to these levels, are observed at other angles, but only upper limits for the spectroscopic factors can be given. The spin value is not determined for any level in our study, only the momentum transfer  $l$  is determined, hence the spin-parity values are  $J^\pi = 1/2^-$  or  $3/2^-$  for  $l=1$  transfer,  $J^\pi = 5/2^-$  or  $7/2^-$  for  $l=3$  transfer. Hypothesis are made, based on a comparison with the level schemes of the lighter Ga isotopes and continuity arguments : the ground state is supposed to have  $J^\pi = 3/2^-$  as the ground states of all the other Ga isotopes, the first level at 232 keV corresponding to an  $l=3$  transfer is supposed, as in the other Ga isotopes to have  $J^\pi = 5/2^-$ . The other levels, at higher excitation energies, with large spectroscopic factors corresponding to  $l=3$  transfer, are supposed to have  $J^\pi = 7/2^-$ . The level at

1236 keV, which has an  $l=1$  spectroscopic factor of the same order as the one measured for the  $J^\pi=1/2^-$  level around 1100 keV excitation energy in  $^{71}\text{Ga}$  and  $^{73}\text{Ga}$ , is tentatively supposed to have  $J^\pi=1/2^-$ .

The summed spectroscopic strengths, energy weighted spectroscopic strengths and percentage of the observed total strength carried by the strongest transition, for each  $l, j$  value, are given in table 8. It can be seen that the major part of the observed  $2p1/2$ ,  $2p3/2$ ,  $1f5/2$  and  $1g9/2$  strength is carried by a single level in each of the isotopes studied. The same is true in the  $^{64,70}\text{Zn}(^3\text{He},d)^{65,71}\text{Ga}$  reactions<sup>11)</sup> and the strength is carried by the same levels in  $^{69,71}\text{Ga}$ , observed in both studies. These levels, which have therefore a strong single particle character are : the  $J^\pi=3/2^-$  ground state, a  $J^\pi=1/2^-$  level lying under 350 keV in  $^{65,67,69}\text{Ga}$  and raising between 1100 and 1240 keV in  $^{71,73,75}\text{Ga}$ , the first  $J^\pi=5/2^-$  level, whose energy varies between 180 and 580 keV with a maximum energy in  $^{69}\text{Ga}$ , a  $J^\pi=9/2^+$  level whose energy is minimum near 1200 keV for  $^{73}\text{Ga}$ . (It must be stressed that the  $l=4$  nature of the transitions observed for  $^{73,75}\text{Ga}$  is only tentative). Correspondance between these levels are indicated in figure 6 where the level schemes of all the Ga isotopes between  $A=65$  and  $A=75$  are compared.

## 5. Occupation numbers in the ground states of Ge and neighbouring nuclei.

### 5.1. Empirical discussion.

As shown by Mac Farlane and French<sup>18)</sup> the sum of all the spectroscopic factors corresponding to a given  $l, j$  transfer in a pick-up reaction is equal to the average number of particles on the shell model  $l, j$  orbital in the target ground state wave function. The summed spectroscopic factors shown in table 8 permit to conclude that :

i) Only a weak ( $C^2S \sim 0.25$ )  $l=4$  transition is observed. This result, as well as the fact that in the  $\text{Ge}(^3\text{He},d)$  As only a weak  $l=3$  strength corresponding to  $J^\pi=7/2^-$  has been observed<sup>8)</sup> indicates that, to a good approximation, the  $2p, 1f5/2$  orbitals may be considered as the only active ones in the proton wave functions of the Ge ground states.

ii) The total  $2p_{1f5/2}$  strength is very close to 4, indicating that essentially all the strength is observed.

iii) Only a part of the possible  $1f_{7/2}$  strength is observed, clearly because of the limitation in excitation energy of the observed spectra. The fact that a larger fraction is observed in the two heaviest isotopes seems to indicate that the  $1f_{7/2}$  orbital is coming closer to the Fermi surface than in the lighter isotopes.

iiii) There is a striking change between the wave functions of the two lightest and of the two heaviest Ge isotopes : there is one more proton on the  $f_{5/2}$  orbital and one less on the  $2p_{3/2}$  orbital in the two heaviest isotopes ( $N=42$  and  $44$ ) than in the two lightest ( $N=38$  and  $40$ ). This clearly corresponds to an abrupt change in the proton configurations between  $N=40$  and  $42$ .

An anomaly of the occupation numbers for several nuclei in the same region has been previously reported<sup>5)</sup> : the population of the proton  $p$  orbitals, also measured using the  $(d, ^3\text{He})$  reaction, is larger in the Ga isotopes ( $Z=31$ ) than in  $^{75}\text{As}$  ( $Z=33$ ). The comparison, in table 9, of the present  $^{70,72,74,76}\text{Ge}(d, ^3\text{He})^{69,71,73,75}\text{Ga}$  results with the previous  $^{69,71}\text{Ga}(d, ^3\text{He})^{68,70}\text{Zn}$  and  $^{75}\text{As}(d, ^3\text{He})^{74}\text{Ge}$  results indicates that the previously reported anomaly is in fact due to the transition between  $N=40$  and  $N=42$ , rather than to the change in the number of protons when going from Ga to As.

In summary, one can say schematically that, when one adds protons to a given nucleus, at least between  $Z=31$  and  $33$ , they never go on the  $p$  orbitals but on the  $f_{5/2}$  orbital.

It is possible to deduce, from a study of the  $(d, ^3\text{He})$  reaction<sup>19)</sup> on the Cu isotopes, that in these nuclei the number of protons on the  $p$  orbitals lies between 0.9 and 1. We do not have precise numbers for the Zn isotopes from the  $(d, ^3\text{He})$  reaction, but it can be deduced from the results<sup>11)</sup> of the  $(^3\text{He}, d)$  reaction on  $^{68,70}\text{Zn}$  that the number of protons on the  $p$  orbitals lies between 1.5 and 2. In the Ga isotopes, with  $Z=31$ , there is still an important filling of the  $p$  orbitals and the  $f_{5/2}$  occupancy remains weak. It appears therefore that the  $p$  orbitals, empty at  $Z=28$ , begin to fill normally, up to and including the Ga isotopes ( $Z=31$ ). In the Ge and As isotopes, with  $Z=32$  and  $33$ , the  $p$  orbitals though far from being filled, do not continue to fill as



they normally should and the additional protons go entirely on the  $f_{5/2}$  orbital. This first anomaly appears therefore to occur between  $Z=31$  and  $32$ .

On the other hand, when crossing the  $N=40+42$  transition first observed in the  $(t,p)$  reaction<sup>7)</sup>, it appears that one proton which was previously on the  $p$  orbitals goes also to the  $f_{5/2}$  orbital.

We have therefore evidences in our data for two different, but perhaps related, types of anomalies :

i) When increasing  $Z$ , for a constant  $N$  value, the  $p$  orbitals begin to fill normally, at least for  $N < 40$ , then these orbitals apparently completely stop filling between  $Z=31$  and  $32$  and all the additional protons go on the  $f_{5/2}$  orbital.

ii) When increasing  $N$ , for a constant  $Z$  value, the populations of the  $p$  and  $f_{5/2}$  orbitals change only when crossing the transition between  $N=40$  and  $42$  : a proton which was on the  $p$  orbital then jumps to the  $f_{5/2}$  orbital.

## 5.2. Comparison with model wave functions.

A very simple model, based on configuration mixing of protons on the  $p_{3/2}$  and  $f_{5/2}$  orbitals, has already been proposed<sup>2,3)</sup> for the  $G_{g.s.}$  and for the  $G_{g.s.}$  and  $G_{0^+}$  wave functions. It has been used successfully to reproduce or predict many experimental results<sup>20)</sup>. The main features are summarized below :

i) Using the occupation numbers determined in the  $^{71}\text{Ga}(d,^3\text{He})^{70}\text{Zn}$  reaction<sup>5)</sup> it has been possible to get the coefficients of the  $^{71}\text{Ga}_{g.s.}$  wave function

$$\psi(^{71}\text{Ga}_{g.s.}) = \sqrt{0.87} (p_{3/2})^3 + \sqrt{0.13} p_{3/2} \cdot (f_{5/2})^2_0$$

ii) Using the known ratio of the spectroscopic factors for the two  $0^+$  levels of  $^{72}\text{Ge}$  it is then possible to determine (see ref.3).

$$\psi(^{72}\text{Ge } g.s.) = \sqrt{0.37} (p_{3/2})_0^4 + \sqrt{0.63} (p_{3/2})_0^2 (f_{5/2})_0^2$$

$$\psi(^{72}\text{Ge } 0_2^+) = \sqrt{0.63} (p_{3/2})_0^4 - \sqrt{0.37} (p_{3/2})_0^2 (f_{5/2})_0^2$$

iii) It is then possible (see ref. 3) using the known ratio<sup>6)</sup> of the cross sections of the two  $0^+$  levels of  $^{72}\text{Ge}$  in the (p,t) reaction, to determine

$$\psi(^{74}\text{Ge } g.s.) = \sqrt{0.03} (p_{3/2})_0^4 + \sqrt{0.97} (p_{3/2})_0^2 (f_{5/2})_0^2$$

$$\psi(^{74}\text{Ge } 0_2^+) = \sqrt{0.97} (p_{3/2})_0^4 - \sqrt{0.03} (p_{3/2})_0^2 (f_{5/2})_0^2$$

It is interesting to see whether or not these wave function, determined before the experiments described in the present paper, are able to reproduce the measured occupation numbers. If we compare the experimental and model values for the p (p1/2+p3/2) and f5/2 orbitals, we get a rather good agreement (see table 10). It is clear however that our simplifying hypothesis that the p1/2 and g9/2 orbitals are empty is not absolutely correct. The probability of occupation of the g9/2 orbital is however very small and we shall continue to neglect it. It proves that a very simple modification permits to account for the p1/2 occupation number. The results called "improved model" in table 10 are simply obtained by admitting that in the second term ( $p^2(f_{5/2})_0^2$ ) of the Ge wave functions the p particles are not all p3/2, but that a fraction (1/3 in  $^{72}\text{Ge}$ , 1/4 in  $^{74}\text{Ge}$ ) is in fact p1/2. This minor improvement has only minor effects on the results reported previously<sup>20)</sup>.

It is attractive to try to determine the coefficients of the  $^{73}\text{Ga}_{g.s.}$  wave function

$$\Psi(^{73}\text{Ga}_{g.s}) = \alpha (p_{3/2})^3 + \beta \cdot p_{3/2} (f_{5/2})^2$$

Unfortunately the value of the  $^{74}\text{Ge}_{g.s}(d, ^3\text{He})^{73}\text{Ga}_{g.s}$  spectroscopic factor proves not to depend sensitively upon the values of the  $\alpha$  and  $\beta$  coefficients. We may however proceed like in the case of the wave function of  $^{74}\text{Ge}_{g.s}$  (see ref.3) and try to reproduce the quite strikingly reduced value of the overlap of the ground states wave functions observed<sup>7)</sup> in the  $^{71}\text{Ga}(t,p)^{73}\text{Ga}$  reaction. A good agreement (0.27 to be compared to an experimental value of 0.31) is obtained using the same coefficients as in the  $^{74}\text{Ge}_{g.s}$  wave function, namely

$$\Psi(^{73}\text{Ga}_{g.s}) = \sqrt{0.03} (p_{3/2})^3 + \sqrt{0.97} \cdot p_{3/2} (f_{5/2})^2$$

With these coefficients the spectroscopic factor for the  $^{74}\text{Ge}_{g.s}(d, ^3\text{He})^{73}\text{Ga}_{g.s}$  is computed as 1.56 to be compared with an experimental value of 1.33.

The wave functions discussed above are, at least, a parametrization of the experimental results. They permit to see that the main change occurring between  $^{72}_{40}\text{Ge}$  and  $^{74}_{42}\text{Ge}$ , as well as between  $^{71}_{40}\text{Ga}$  and  $^{73}_{42}\text{Ga}$ , corresponding to the  $N=40 \rightarrow 42$  transition, is the near disappearance of the first term of the wave functions, containing respectively 4 and 3  $p_{3/2}$  protons in the Ge and Ga isotopes.

## 6. Summary and conclusion.

The study of the  $^{69,71,73,75}\text{Ga}$  isotopes by means of the  $(d, ^3\text{He})$  reaction at 26 MeV has permitted to measure the spectroscopic factors for many levels and to determine the level schemes of the practically unknown  $^{73}\text{Ga}$  and  $^{75}\text{Ga}$ .

The occupation numbers measured here for the even-even  $^{70,72,74,76}\text{Ge}$  isotopes and previously for the odd nuclei  $^{69,71}\text{Ga}$  and  $^{75}\text{As}$  reveal, instead of the usual smooth behaviour as a function of  $N$  and  $Z$ , two striking anomalies.

When increasing  $Z$ , for a constant  $N$  value ( $<40$ ), the  $p$  orbitals begin to fill normally, then completely stop filling, though far from being filled, between  $Z=31$  and  $32$ , and all the additional protons go on the  $f_{5/2}$  orbital.

When increasing  $N$ , for a constant  $Z$  value, the populations of the  $p$  and  $f_{5/2}$  orbitals change only when crossing the transition between  $N=40$  and  $42$ , then a proton which was on the  $p$  orbital jumps to the  $f_{5/2}$  orbital.

This last anomaly is clearly related to the structural transition observed<sup>7)</sup> between  $N=40$  and  $42$  for the Ge and Ga isotopes, in a comparison of the  $(p,t)$  and  $(t,p)$  reactions.

We do not know yet the exact origin of the observed anomalies, but they could well be related to changes of the nuclear shape.

The occupation numbers measured are rather well reproduced by a slightly improved version of our model describing to Ga ground states and the  $O^+$  levels of the Ge isotopes as configuration mixing of protons in the  $p$  and  $f_{5/2}$  orbitals. The main change in these wave functions both for Ge and Ga, when crossing the  $N=40 \rightarrow 42$  transition, is the near disappearance of the term containing more than 2 particles in the same orbital. Such an effect could be an indication that the transition is a "spherical-deformed" one, as suggested on the basis of the comparison of the  $(p,t)$  and  $(t,p)$  results, because in a deformed nucleus (Nilsson model for example) no more than 2 particles can couple on a given intrinsic orbital.

## REFERENCES

\* presently at Institut de Physique de Nantes, BP 1044, 44 Nantes and Institut de Physique Nucléaire 91406 Orsay, France.

- 1) W.G. Monahan, R.G. Arns, Phys. Rev. 184, (1969) 1135  
K.E.G. LEBNER, G. Danhauser, D.J. Donahue, O. Hüscher,  
R.L. Hershberger, R. Lutter, W. Klinger, W. Wittman, Z. Physik  
A274 (1975) 251 J. Haderman and A.C. Rester, Nucl. Phys. A231 (1974) 120
- 2) D. Ardouin, R. Tamisier, G. Berrier, J. Kalifa, G. Rotbard,  
and M. Vergnes, Phys. Rev. C11, (1975) 1649  
D. Ardouin, R. Tamisier, M. Vergnes, G. Rotbard, J. Kalifa  
G. Berrier, B. Grammaticos, Phys. Rev. C12 (1975) 1745
- 3) M. Vergnes, G. Rotbard, D. Ardouin, Structure of the low lying  
 $0^+$  levels in the Ge isotopes, Orsay, Internal report :  
IPNO-PhN-76-20
- 4) G. Gneuss, L.V. Bernus, U. Schneider and W. Greiner, in proceeding of the  
Colloque sur les noyaux de transition, Orsay, June 1971 ( Institut de Phy-  
sique Nucléaire d'Orsay, Orsay 1971) p. 53
- 5) G. Rotbard, M. Vergnes, G. La Rana, J. Vernotte, J. Kalifa, G. Berrier,  
F. Guilbaut, R. Tamisier, J.F.A. Van Hienen, Phys. Rev. C16 (1977) 1825
- 6) F. Guilbaut, D. Ardouin, R. Tamisier, P. Avignon, M. Vergnes, G. Rotbard,  
G. Berrier, R. Seltz, Phys. Rev. C15 (1977) 894  
F. Guilbaut, D. Ardouin, J. Uzureau, P. Avignon, R. Tamisier, G. Rotbard,  
M. Vergnes, Y. Deschamp, G. Berrier, R. Seltz, Phys. Rev. C16 (1977)  
1840
- 7) M.N. Vergnes, G. Rotbard, F. Guilbaut, D. Ardouin, C. Lebrun, E.R. Flynn,  
D. Hansen, S.D. Orbeser, Phys. Letters and private communication

- 8) R.R. Betts, S. Merlechai, D.J. Pullen, B. Rosner and W. Scolz, Nucl. Phys. A230 (1974) 235, M. Schrader, H. Reiss, G. Rosner and H.V. Klapdor, Nucl. Phys. A263 (1976) 193
- 9) H. Wapstra and K. Bos, Atomic Data and Nuclear Data Tables 19 (1977) 215
- 10) P.D. Kunz, Univ. of Colorado, 1967 (unpublished)
- 11) B. Zeidman, R.H. Siemssen, G.C. Morrisson and L.L. Lee, Jr, Phys. Rev. C9 (1974) 409, A. Riccato and P. David, Nucl. Phys. A 228 (1974) 461
- 12) F.D. Becchetti and G.W. Greenlees, in Polarization Phenomena in Nuclear Reactions (H.H. Barschall and W. Heaberli, eds) p 682, the university of Wisconsin Press, Eddison, Wis. (1971)
- 13) C.M. Percy and F.G. Percy, Atomic Data and Nuclear Data Tables 17 (1976) 1
- 14) R.L. Auble, Nuclear Data Sheets 17 (1976) 193  
T. Paradelis, A. Xenouillis, C.A. Kalfas, Z. Physik A275 (1975) 269
- 15) W.H. Zoller, W.B. Walters, G.E. Gordon, Nucl. Phys. A142 (1970) 177
- 16) B.R. Erdal, L. Westgaard, J. Zylicz, E. Roekz and the Isolde Collaboration, Nucl. Phys. A194 (1972) 449
- 17) K. Aleklet, E. Lund, G. Nyman and G. Rudstam, Nucl. Phys. A285 (1977) 1
- 18) M.H. Mac Farlane and J. B. French, Review of Modern Physics, 32 (1960) 567
- 19) J.C. Hiebert and E. Newman, Nucl. Phys. A113 (1968) 176
- 20) M. Vergnes, Proceedings of "Colloque Franco-Japonais and INS symposium" Tokyo-Dogashima, Sept. 1976, Ed. By Institute for Nuclear Study, University of Tokyo, p. 61-75

TABLE 1 - ISOTOPIC COMPOSITION  
OF THE TARGETS

target \ isotope	$^{70}\text{Ge}$	$^{72}\text{Ge}$	$^{73}\text{Ge}$	$^{74}\text{Ge}$	$^{76}\text{Ge}$	thickness $\mu\text{g}/\text{cm}^2$
$^{70}\text{Ge}$	84.62	5.54	1.47	6.36	2.01	52
$^{72}\text{Ge}$	1.04	96.23	.77	1.63	.33	60
$^{74}\text{Ge}$	1.71	2.21	.9	94.48	.70	60
$^{76}\text{Ge}$	.81	1.21	.50	1.98	95.5	67
natural	20.52	27.43	7.76	36.54	7.76	60

TABLE 2 - Q VALUES FOR  $\text{Ge}(d^3\text{He})\text{Ge}$  REACTION

Reaction	$^{70}\text{Ge}(d^3\text{He})^{69}\text{Ge}$	$^{72}\text{Ge}(d^3\text{He})^{71}\text{Ge}$	$^{74}\text{Ge}(d^3\text{He})^{73}\text{Ge}$	$^{76}\text{Ge}(d^3\text{He})^{75}\text{Ge}$
Previously known Q values a) (in keV)	$-3.035.4 \pm 3.2$	$-4.236.5 \pm 3.0$	$-5.486 \pm 40$	$-6.460 \pm 200$
measured Q (in keV)	$-3.030 \pm 7$	$-4.241 \pm 7$	$-5.515 \pm 7$	$-6.545 \pm 7$

a) from ref. 9

TABLE 3 : OPTICAL AND BOUND STATE POTENTIAL PARAMETERS USED IN THE  
DWBA ANALYSIS

	V	$r_0$	a	w	$4W_D$	$r'_0$	$a'$	$r_{oc}$
$d^a$ )	$81-.22E+22/A^{1/3}$	1.15	.81	0	$57.6+.96E$	1.34	.68	1.15
$^3He^b$ )	$151.9-.17E+50(N-2)/A$	1.20	.72	$41.7-.33E+$ $44(N-2)/A$	0	1.4	.88	1.3
P		1.25	.65	0	0			1.25

a) from ref.13

b) from ref.12



TABLE 4 : RESULTS FROM THE  $^{70}\text{Ge}(d^3\text{He})^{69}\text{Ga}$  REACTION

Previous work a)		present work			
$E_x$ (keV)	$J^\pi$	$E_x$ (keV)	1	$J^\pi$ assigned	$C^2_{gs}$ b)
0	$3/2^-$	0	1	$3/2^-$	1.63
318.5	$1/2^-$	317	1	$1/2^-$	.49
573.8	$5/2^-$	571	3	$5/2^-$	1.14
871.8	$3/2^-$	873	1	$3/2^-$	.58
1027.	$1/2^-$	1029	1	$1/2^-$	.10
1106.3	$5/2^-$	1108	3	$5/2^-$	.10
1336.0	$7/2^-$	1335	3	$7/2^-$	.49
1487.7	$7/2^-$	1488	3	$7/2^-$	.24
1525.4	$(3/2, 5/2)^-$				
1723.4	$5/2^-$				
1764.9	$9/2^-$				
1891.1	$3/2^-$	1890	1	$3/2^-$	.145
1923.2	$7/2^-$	1923	3	$7/2^-$	.23
1972.0	$9/2^+$	1970	4	$9/2^+$	.26
1978.	$(1/2^-, 3/2^-)$		+		
2002.	$(1/2^-, 3/2^-)$		1	$1/2^-, 3/2^-$	.033, .026
2022.4	$5/2^-, 7/2^-$				
2042.8	$(5/2^-, 5/2^-)$				
2197					
2220	$1/2^+$				
		2250	(1)	$(1/2^-, 3/2^-)$	(.037, .03)
2352					
2426		2425	3	$7/2^-, (5/2^-)$	1.42, (.81)
2457	$3/2$	2461	(3)	$(7/2^-, 5/2^-)$	(.23, .13)

a) from ref. 14

b) When there are two possible  $J^\pi$  assignments, the corresponding spectroscopic factors are given in the same order.

Table 5 - RESULTS FROM THE  $^{72}\text{Ge}(\text{d},^3\text{He})^{71}\text{Ga}$  REACTION

Previous works a)		Present work			
$E_x$ (keV)	$J^\pi$	Ex (keV)	I	$J^\pi$ assigned	$C^2S^b$
0	$3/2^-$	0	1	$3/2^-$	2.14
389.9	$1/2^-$	388	1	$1/2^-$	.04
487.3	$5/2^-$	487	3	$5/2^-$	1.14
511.5	$3/2^-$	510	1	$3/2^-$	.21
910.5	$3/2^-, (1/2^-)$	(910)			<.01
964.7	$5/2^-$	964	3	$5/2^-$	.20
1107.5	$7/2^-$				
1109	$1/2^-$	1113	1	$1/2^-$	.39
1395.2	$(5/2^-, 7/2^-)$	1396	3	$7/2^-, (5/2^-)$	.52, (.92)
1476.1	$5/2^-, 7/2^-$	1476	3	$7/2^-, 5/2^-$	.12, .21
1493.8	$9/2^+$	1495	4	$9/2^+$	.24
1498.7	$5/2^-, 7/2^-$				
1631.5	$3/2^- (1/2^-)$	1634			very weak
1702.1					
1719.7	$(5/2^-, 7/2^-)$				
		1907	3	$7/2^-, (5/2^-)$	.87, (1.59)
		1995	3	$7/2^-, (5/2^-)$	.37, (.65)

a) from ref. 16

b) When there are two possible  $J^\pi$  assignments, the corresponding spectroscopic factors are given in the same order.

TABLE 6 - RESULTS FROM THE  $^{74}\text{Ge}(d, ^3\text{He})^{73}\text{Ga}$  REACTION

Previous works				Present work		
$E_X^a$ (keV)	$J^\pi$ a)	$E_X^b$ (keV)	Ex (keV)	1	$J^\pi$ assigned	$C^2S^C$
0	$3/2^-$	0	0	1	$3/2^-$	1.33
			198	3	$5/2^-, (7/2^-)$	1.87 (1.06)
219	$3/2^-$	216	214	1	$3/2^-$	.07
498		496	495	3	$5/2^- (7/2^-)$	.32, (.18)
647						
915	$3/2^-$	911	912	1	$3/2^-$	.04
956			952	3	$7/2^-, (5/2^-)$	.50 (.89)
1117			1112	1	$1/2^- (3/2^-)$	.43, (.35)
1235			1233	(4)	$(9/2^+)$	(.37)
1396						
1528		1	1534	3	$7/2^-, (5/2^-)$	1.79(3.15)
1578						
1618			1620	3	$7/2^-, (5/2^-)$	.50, (.91)
1771			1777	(3)	$(7/2^-, 5/2^-)$	(.21, .36)
1800	$3/2^-$					

a) From ref. 7

b) From ref. 16

c) When there are two possible  $J^\pi$  assignments, the corresponding spectroscopic factors are given in the same order.

TABLE 7 : Results from the  $^{76}\text{Ge}(\text{d}, ^3\text{He})^{75}\text{Ga}$  REACTION

Present work				
Exc <sup>a)</sup> (keV)	Exc	1	J <sup>π</sup> assigned	C <sup>2</sup> S
	0	1	$3/2^-$	
	180	1	$3/2^-, 1/2^-$	.06, .07
228	232	3	$5/2^-, (7/2^-)$	2.44, (1.35)
432		(1)		< .05
		(3)		< .1
606		(1)		< .03
		(3)		< .1
	887	3	$7/2^-, (5/2^-)$	.39, (.69)
	1174	3	$7/2^-, 5/2^-$	.10, .18
	1263	1	$1/2^-, (3/2^-)$	.40, (.32)
	1517	(4)	$(9/2^+)$	.25
	1553	3	$7/2^-, 5/2^-$	.10, .17
	1629	3	$7/2^-, (5/2^-)$	.43, (.73)
	1942	1	$3/2^-, 1/2^-$	.11, .09
	1976			
	2023	3	$7/2^-, (5/2^-)$	2.7, (5.1)
	2090			

a) from ref. 17

Table 8 : Summed spectroscopic strengths, centroids of the observed strengths (in keV) and proportion of the observed strengths (and of the total strengths for  $7/2^-$ ) in the strongest level.

Shell \ N	38	40	42	44
2p <sub>1/2</sub>	.59,439,.83	.43,1042,.91	.43,1117,1	.40,1236,1
2p <sub>3/2</sub>	2.36,331,.69	2.35,46,.91	1.44,36,.91	1.25,148,.88
1f <sub>5/2</sub>	1.24,618,.92	1.34,559,.85	2.20,242,.85	2.44,232,1
1f <sub>7/2</sub>	1.77,1952,.46 (.10)	1.88,1755,.35 (.11)	3.00,1468,.6 (.22)	2.72,1823,.73 (.34)
1g <sub>9/2</sub>	.25,1972,1.	.24,1494,1	(.37),(1235)(1)	.25,1517,1
p <sub>1/2</sub> +p <sub>3/2</sub> +f <sub>5/2</sub>	4.19	4.12	4.07	4.09

Table 9 : Comparison of the  $1f_{5/2}$  and the  $2p$  occupation numbers obtained by means of  $(d, ^3\text{He})$  reaction on  $^{69,71}\text{Ga}$ ,  $^{70-76}\text{Ge}$  and  $^{75}\text{As}$  targets. The main feature seems to be that the additional proton (when the target varies from Ga to Ge and from Ge to As) goes on the  $1f_{5/2}$  orbit and that another proton goes from the  $p$  to the  $f$  orbit when  $N$  changes from 40 to 42.

$Z \backslash N$	38	40	42	44	
Ga 31	2.54	2.76			
Ge 32	2.95	2.78	1.87	1.65	$1 = 1$
As 33			1.80		
Ga 31	.38	.25			
Ge 32	1.24	1.34	2.20	2.40	$1 = 3$
As 33			3.42		

Table 10 : Comparison of experimental and calculated occupation numbers

		$\langle f_{5/2} \rangle$	$\langle p \rangle$	$\langle p_{1/2} \rangle$	$\langle p_{3/2} \rangle$
72	Exp	1.34	2.78	0.43	2.35
	Old Model	1.26	2.74	0	2.74
	Model Improved	1.26	2.74	0.42	2.32
74	Exp	2.2	1.87	0.43	1.44
	Old Model	1.94	2.06	0	2.06
	Model Improved	1.94	2.06	0.48	1.58

### Figure captions

---

- Fig. 1 : Typical energy spectra of emitted  ${}^3\text{He}$  from the  ${}^{74,76}\text{Ge}(\text{d}, {}^3\text{He}){}^{73,75}\text{Ga}$  reaction. Peaks without indication of excitation energy result from  $(\text{d}, {}^3\text{He})$  reaction either on other Ge isotopes or on light impurities. The broad peak on each spectrum results from the  ${}^{16}\text{O}(\text{d}, {}^3\text{He}){}^{15}\text{N}_{\text{g.s.}}$  reaction.
- Fig. 2 : Angular distributions of the  ${}^3\text{He}$  particles in the  ${}^{70}\text{Ge}(\text{d}, {}^3\text{He}){}^{69}\text{Ga}$  reaction. The curves are the results of D.W.B.A. calculations.
- Fig. 3 : Angular distributions of the  ${}^3\text{He}$  particles in the  ${}^{72}\text{Ge}(\text{d}, {}^3\text{He}){}^{71}\text{Ga}$  reaction. The curves are the results of D.W.B.A. calculations.
- Fig. 4 : Angular distributions of the  ${}^3\text{He}$  particles in the  ${}^{74}\text{Ge}(\text{d}, {}^3\text{He}){}^{73}\text{Ga}$  reaction. The curves are the results of D.W.B.A. calculations.
- Fig. 5 : Angular distributions of the  ${}^3\text{He}$  particles in the  ${}^{76}\text{Ge}(\text{d}, {}^3\text{He}){}^{75}\text{Ga}$  reaction. The curves are the results of DWBA calculations.
- Fig. 6 : Comparison of levels schemes for the Ga isotopes obtained in one-proton transfer reactions on even nuclei. For each isotope the right-side bars represent spectroscopic strengths  $(2J+1)\text{C}^2\text{S}$  for stripping reaction (ref.11), the left-side bars represent spectroscopic strengths  $\text{C}^2\text{S}$  for pick-up reaction (this work). Solid bars correspond to  $l=1$  transfers, open bars to  $l=3$  transfers, crosses to  $l=4$  transfers. The total length of a line corresponds to a spectroscopic strength value of 5. Levels carrying the major part of each angular momentum transfer are connected by dotted lines

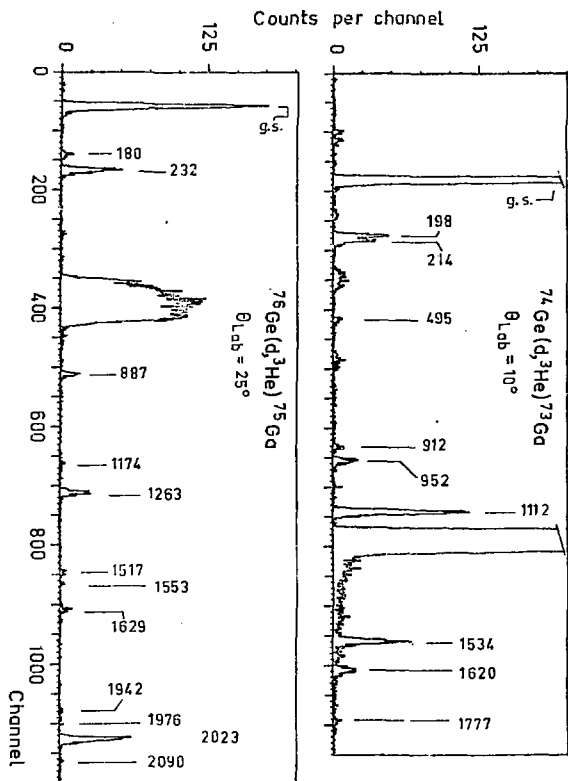


Fig. 1.



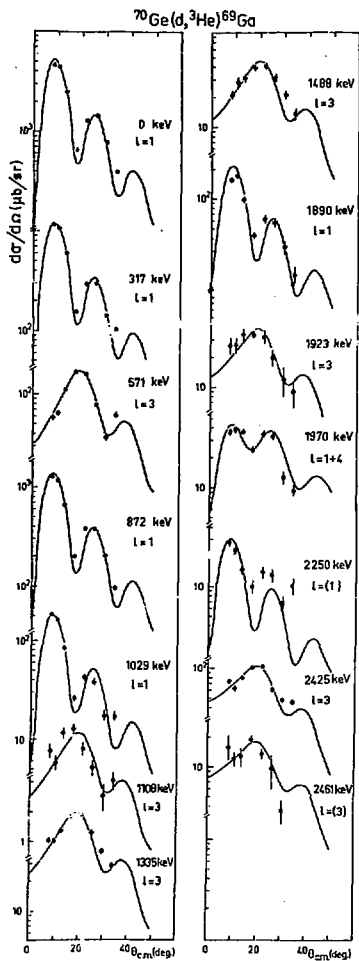


Fig. 2.

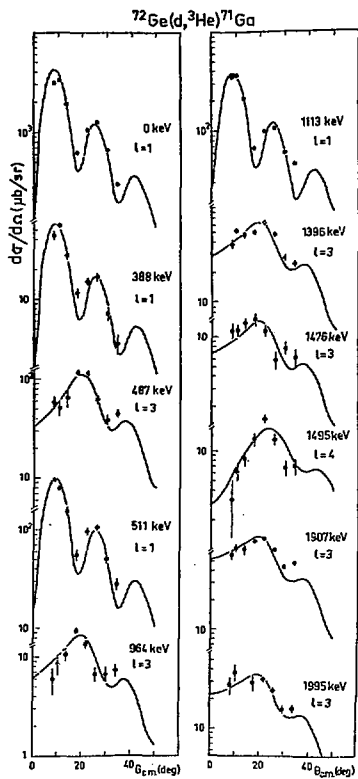


Fig. 3.

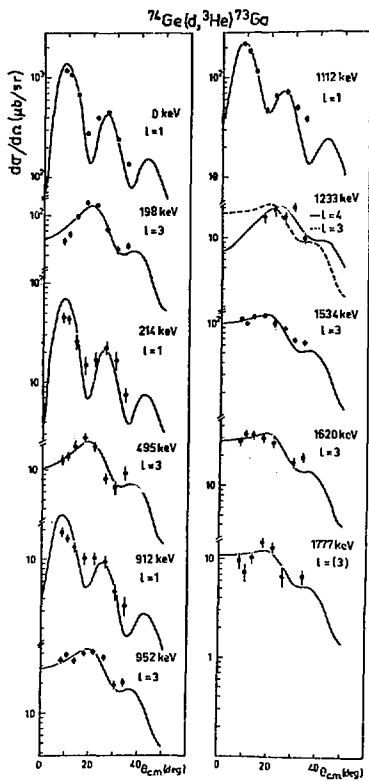


Fig. 4.

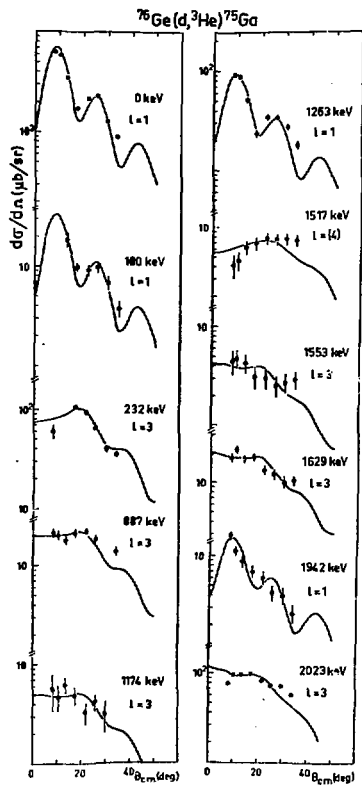


Fig. 5.

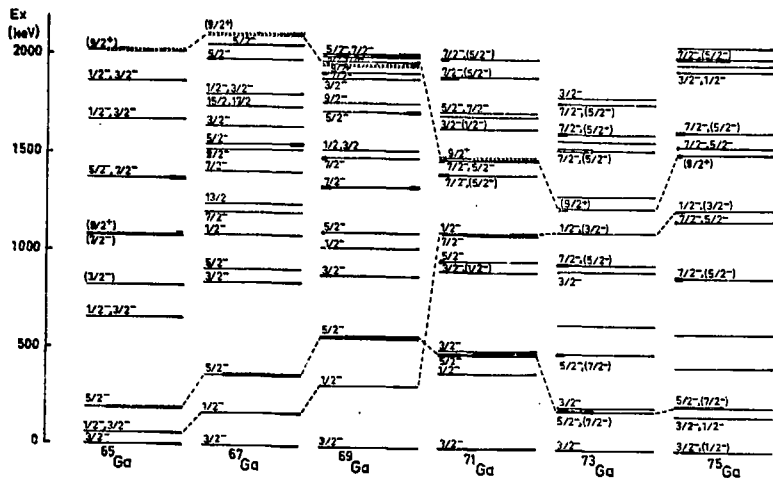


Fig. 6.