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Scaling Phenomenon in Relativistic Nucleus-Nucleus Collisions\*

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Abstract

We introduce new scaling variables for proton and pion production in relativistic nucleus-nucleus collisions which are the generalizations of the Feynmann scaling variable. They allow a simple description of the cross sections at the forward and backward angles.

\* \* \* \*

Recent experimental and theoretical studies<sup>1-6</sup> of nucleus-nucleus collisions in the energy range of a few GeV per nucleon indicates that the use of the Feynmann variable  $x_F$  should lead to scaling in the case of forward pion production.<sup>1,2</sup> However,  $x_F$  scaling was not observed in proton production<sup>3,4</sup> or in backward pion production.<sup>5</sup> It is desirable to look for new scaling variables so that the experimental data can be better represented and the underlying physics of the scaling phenomenon understood.

The proper scaling variable depends on the reaction mechanism. In the reaction  $A+B \rightarrow C+X$ , the two dominant processes<sup>7</sup> of interest are the direct fragmentation and the hard-scattering process. In the direct projectile fragmentation process the subsystem C is emitted directly from the beam particle B without scattering, while the complementary partner interacts with the target nucleus A. The cross section is proportional to the probability  $C_{C/B}(x_D, \vec{C}_T)$  of finding a subsystem C in the projectile B with transverse momentum  $\vec{C}_T$  and fractional momentum  $x_D$  defined by

$$x_D = \frac{C_0 + C_Z}{B_0 + B_Z} = x_F x_{\max} \tag{1}$$

where we have used A, B, and C to denote also the four-vectors of A, B, and C, respectively. In terms of the relativistic invariant  $s = (A+B)^2$  and the usual  $\lambda$ -function,<sup>2</sup> we have

$$x_{\max} = \frac{s-D^2 + C^2 + \lambda(s, D^2, C^2)}{s-A^2 + B^2 + \lambda(s, A^2, B^2)} \tag{2}$$

and D is the missing mass of X. Thus,  $x_D$  is a good "direct fragmentation"

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scaling variable when the direct fragmentation process dominates and when the bombarding energy is high enough. We show in Fig. 1 the experimental data of Anderson, et al.<sup>3</sup> for the reaction  $\alpha + {}^{12}\text{C} \rightarrow \text{p}+\text{X}$ . As one observes, the experimental data scales with  $x_D$  when  $x_D \geq 0.20$  and  $p_\alpha \geq 1.74$  GeV/c/N, for different values of  $p_T$ . The analogous scaling variable  $x_D$  for target

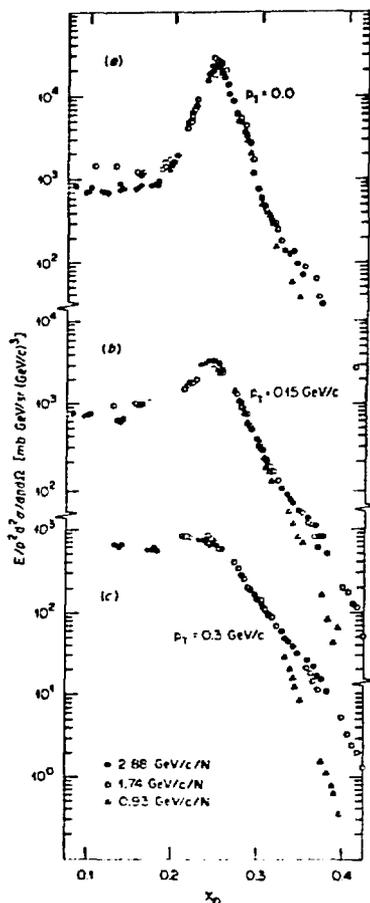


Fig. 1. Experimental invariant cross section for  $\alpha + {}^{12}\text{C} \rightarrow \text{p}+\text{X}$ . Data are from Ref. 3.

"hard-scattering" scaling variable  $x_H$ . Indeed, when the data of  $\text{p} + \text{Cu} \rightarrow \text{p}+\text{X}$  ( $180^\circ$ ) are plotted with respect to  $x_H$ , we see that the experimental data scales well with  $x_H$  (Fig. 2), in contrast to the absence of scaling with respect to  $x_F$  observed earlier.<sup>5,6</sup> For forward pion production, the experimental data of  $\alpha + {}^{12}\text{C} \rightarrow \pi^- + \text{X}$  also scale with  $x_H$ . In this case,  $x_H$  is approximately equal to  $x_F$  in the region of interest and thus there is also  $x_F$  scaling for forward pion production.<sup>1</sup>

fragmentation can be obtained from Eqs. (1) and (2) by replacing  $C_Z \rightarrow -C_Z$ ,  $x_F \rightarrow |x_F|$  and interchanging  $B_O \leftrightarrow A_O$ ,  $B_Z \leftrightarrow -A_Z$ . The experimental data<sup>4</sup> for backward proton production also scales well with  $x_D$  for target fragmentation.

In the hard-scattering process, the target A and projectile B emit subsystems a and b which scatter to produce particle C via the basic process  $a+b \rightarrow C+d$ . Upon examining the six-fold hard-scattering integral,<sup>2</sup> one finds that for projectile fragmentation the integral depends predominantly on the variable

$$x_H = \frac{\gamma^2 + \sqrt{\gamma^4 - b^2(u' + C_T^2)}}{u' + C_T^2} \left[ \frac{m_a(A_O + A_Z)}{m_A(B_O + B_Z)} - x_D \right] \quad (3)$$

where

$$\gamma^2 = \frac{1}{2}[d^2 - a^2 - u'] \quad (4)$$

and

$$u' = (m_a A' / m_A - C)^2. \quad (5)$$

For target fragmentation, the corresponding variable is obtained by replacing  $C_Z \rightarrow -C_Z$ , and interchanging  $a \leftrightarrow b$ ,  $A_O \leftrightarrow B_O$ ,  $A_Z \leftrightarrow -B_Z$ .

As a pion is not a normal constituent of a nucleus, we consider pions to be produced only by the hard-scattering mechanism. The experimental data should scale with the

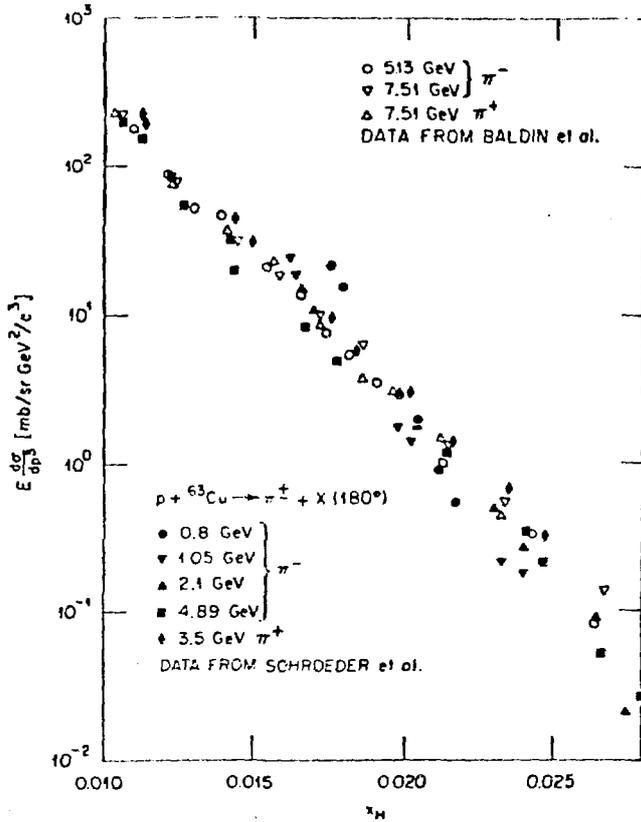


Fig. 2. Experimental invariant cross section for  $p + \text{Cu} \rightarrow \pi^\pm + X$  ( $180^\circ$ ). Data are from Refs. 5 and 7.

In proton production the hard-scattering process becomes more important as  $p_T \gg 0.1$  GeV/c. However, in this case  $x_H \approx x_D$ , and hence,  $x_D$  scaling persists even for large values of  $x_D$  as we observe in Fig. 2.

It is easy to show that in the projectile fragmentation region,  $x_D$  and  $x_H$  approaches  $x_F$  when  $s \gg D^2 - A^2$  and in the target fragmentation when  $s \gg D^2 - B^2$ . We see that  $x_D$  and  $x_H$  are simple generalizations of  $x_F$  for the case when the rest masses are not small compared to  $s$ .

In conclusion, we have obtained scaling variables which allow the experimental data to scale properly for proton and pion production at the forward and backward angles. Their introduction also clarifies the underlying physics of the scaling phenomenon in nucleus-nucleus collision.

References

1. J. Papp, Ph.D. Thesis, University of California, Berkeley, 1975, LBL-3633; J. Papp, et al., Phys. Rev. Lett. 34, 601 (1975).
2. I. A. Schmidt and R. Blankenbecler, Phys. Rev. D15, 3321 (1977).
3. L. M. Anderson, Jr., Ph.D. Thesis, University of California, Berkeley, 1977, LBL-6769; L. M. Anderson, et al., LBL-9493, 1979.
4. J. V. Geaga, et al. (private communication).
5. L. S. Schroeder, et al., Phys. Rev. Lett. 43, 1787 (1979).
6. R. H. Landau and M. Gyulassy, Phys. Rev. C19, 149 (1978).
7. C. Y. Wong and R. Blankenbecler (to be published and contributed paper to this Workshop).
8. A. M. Baldin, et al., Yad. Fiz. 20, 1201 (1974) [Sov. J. Nucl. Phys. 20, 629 (1975)].