



# INTERNATIONAL CENTRE FOR THEORETICAL PHYSICS

PARITY VIOLATIONS IN ELECTRON-NUCLEON SCATTERING  
AND THE  $SU(2)_L \times SU(2)_R \times U(1)_{L+R}$  ELECTROWEAK SYMMETRY

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1. The first part of the document discusses the importance of maintaining accurate records of all transactions and activities. It emphasizes that this is crucial for ensuring transparency and accountability in the organization's operations.

2. The second part of the document outlines the various methods and tools used to collect and analyze data. It highlights the need for consistent and reliable data collection processes to ensure the validity of the results.

3. The third part of the document describes the different types of data that are collected and analyzed. It includes information on both quantitative and qualitative data, as well as the specific variables being measured.

4. The fourth part of the document discusses the various statistical techniques used to analyze the data. It covers both descriptive and inferential statistics, as well as the use of regression analysis and other advanced methods.

5. The fifth part of the document describes the different ways in which the results of the analysis are presented and communicated. It includes information on the use of tables, graphs, and other visual aids to make the data more accessible and understandable.

6. The sixth part of the document discusses the various challenges and limitations associated with data collection and analysis. It highlights the need for careful planning and execution to ensure the quality and reliability of the results.

7. The seventh part of the document describes the different ways in which the results of the analysis are used to inform decision-making and improve organizational performance. It includes information on the use of data-driven insights to identify areas for improvement and to develop effective strategies.

8. The eighth part of the document discusses the various ethical considerations associated with data collection and analysis. It highlights the need for transparency and accountability in the use of data, as well as the importance of protecting the privacy and confidentiality of the information.

9. The ninth part of the document describes the different ways in which the results of the analysis are used to inform policy-making and the development of new programs and initiatives. It includes information on the use of data to identify trends and patterns that can inform the design of effective interventions.

10. The tenth part of the document discusses the various future directions and opportunities for research in this field. It highlights the need for continued innovation and development in data collection and analysis methods, as well as the importance of interdisciplinary collaboration and the integration of data with other fields of study.

11. The eleventh part of the document describes the different ways in which the results of the analysis are used to inform the development of new products and services. It includes information on the use of data to identify customer needs and preferences, as well as the importance of using data to optimize the design and performance of these offerings.

12. The twelfth part of the document discusses the various challenges and opportunities associated with the use of data in the development of new products and services. It highlights the need for a strong data-driven culture and the importance of investing in the necessary infrastructure and talent to support these efforts.

13. The thirteenth part of the document describes the different ways in which the results of the analysis are used to inform the development of new markets and business models. It includes information on the use of data to identify new opportunities and to develop innovative strategies for growth and expansion.

International Atomic Energy Agency  
and  
United Nations Educational Scientific and Cultural Organization  
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PARITY VIOLATIONS IN ELECTRON-NUCLEON SCATTERING  
AND THE  $SU(2)_L \times SU(2)_R \times U(1)_{L+R}$  ELECTROWEAK SYMMETRY \*

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## ABSTRACT

The  $SU(2)_L \times SU(2)_R \times U(1)_{L+R}$  model of electroweak interactions is described with the most general gauge couplings  $g_L$ ,  $g_R$  and  $g_{L+R}$ . The case in which neutrino neutral current interactions are identical to the standard  $SU(2)_L \times U(1)_{L+R}$  model is discussed in detail. It is shown that with the weak angle lying in the experimental range  $\sin^2 \theta_w = 0.23 \pm 0.015$  and  $1 < g_L^2/g_R^2 < 3$  it is possible to explain the amount of parity violation observed at SLAC and at the same time predict values of the "weak charge" in bismuth to lie in the range admitted by the controversial data from different experiments.

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The  $SU(2)_L \times SU(2)_R \times U(1)_{L+R}$  model of electroweak interactions <sup>1)</sup> is usually discussed with the imposed discrete symmetry left  $\leftrightarrow$  right that reduces the number of gauge couplings to just two. In general, the couplings  $g_L$  ( $\equiv SU(2)_L$ ),  $g_R$  ( $\equiv SU(2)_R$ ) and  $g_{L+R}$  ( $\equiv U(1)_{L+R}$ ) can all be different in magnitude as is evident from conventional ideas on grand unified theories <sup>2)</sup>. For example, when  $SO(10)$  descends to  $SU(3)_L \times U(1)_{em}$  through different intermediate sub-symmetries the gauge coupling  $g_{10}$  ( $\equiv SO(10)$ ) splits into four distinct couplings  $g_L$ ,  $g_R$ ,  $g_{1C}$  ( $\equiv U(1)_C$ ) and  $g_{3C}$  ( $\equiv SU(3)_C$ ) at the renormalization point usually taken to be the mass of the weak gauge boson mediating left-handed charged weak interactions.

In this note the  $SU(2)_L \times SU(2)_R \times U(1)_{L+R}$  model for electroweak interactions is described with the most general gauge couplings <sup>3)</sup>  $g_L$ ,  $g_R$  and  $g_{L+R}$ . In order to keep in touch with unification ideas the  $SU(2)_L \times SU(2)_R \times U(1)_{L+R}$  subgroup is extracted from the Pati-Salam group <sup>4)</sup>  $SU(2)_L \times SU(2)_R \times SU(4)_{L+R}^C$  which can be naturally embedded in  $SO(10)$ . This is briefly described.

The equivalent of  $U(1)_{L+R}$  in  $SU(2)_L \times SU(2)_R \times U(1)_{L+R}$  in  $SU(4)_{L+R}^C$  is  $U(1)_{L+R}^C$  ( $\propto \lambda_{15}$  generator of  $SU(4)$ ) and characterizes the (baryon-lepton) number of the theory. The gauge couplings of  $U(1)_{L+R}^C$  and  $U(1)_{L+R}$  are trivially related,  $g_{L+R} = \sqrt{\frac{3}{2}} g_{1C}$ . Spontaneous symmetry breaking of  $SU(2)_L \times SU(2)_R \times SU(4)_{L+R}^C$  to  $SU(3)_{L+R}^C \times U(1)_{em}$  is effected by Higgs scalars  $A \sim (2, 2, 1)$ ,  $B \sim (1, 2, \bar{4})$ ,  $C \sim (2, 1, \bar{4})$ ,  $D \sim (1, 1, 15)$ ,  $E \sim (1, 3, 1)$  with vacuum expectation values  $\langle A \rangle = \text{diag}(a_1, a_2)$ ;  $\langle B \rangle_{24} = b$ ;  $\langle C \rangle_{24} = c$ ;  $\langle D \rangle = \text{diag}(d, d, d, -3d)$ ,  $\langle E \rangle = (0, e, 0)$ . The resulting mass Lagrangian involving only the neutral fields ( $W_L^0, W_R^0, v_{15}^0$ ) has the photon field  $A_\mu$  and two massive neutrals  $N_{1\mu}, N_{2\mu}$  as its physical eigenstates <sup>3)</sup> where

$$A/e = W_L^0/g_L + W_R^0/g_R - \left(\frac{2}{3}\right)^{1/2} v_{15}^0/g_{1C}, \quad (1)$$

$$e^{-2} = g_L^{-2} + g_R^{-2} + \left(\frac{2}{3}\right) g_{1C}^{-2} \quad , \quad (2)$$

$$N_1 = W_{(-)} \cos\beta + Y \sin\beta \quad , \quad (3)$$

$$N_2 = Y \cos\beta - W_{(-)} \sin\beta \quad (4)$$

with masses and the mixing angle defined as

$$M_{1(2)}^3 = \frac{1}{2} (P_1 + P_2) + (-) \frac{1}{2} (P_1 - P_2) \sec 2\beta \quad , \quad (5)$$

$$\tan 2\beta = 2\Delta / (P_2 - P_1) \quad , \quad (6)$$

where  $e$  is the electric charge;  $g^{-2} = g_L^{-2} + g_R^{-2}$ ;  $W_{(-)}/g = W_L^0/g_R - W_R^0/g_L$ ;  $Y/e = \left(\frac{2}{3}\right)^{1/2} g(W_L^0/g_L + W_R^0/g_R)/g_{1C} + V_{15}^0/g$ ;  $4P_1/g^2 = (g_L/g_R + g_R/g_L)^2 a^2 + g_L^2 c^2/g_R^2 + g_R^2 b^2/g_L^2$ ;  $4P_2/g^2 = (3g_{1C}^2/2g^2 + 1)(b^2 + c^2)$ ;  $a^2 = a_1^2 + a_2^2$ ;  $4\Delta/g^2 = (3g_{1C}^2/2g^2 + 1)^{1/2} [g_R b^2/g_L - g_L c^2/g_R]$ . The fermionic current coupling to  $Y^\mu$  is vector, while that coupling to  $W_{(-)}^\mu$ , unlike in the  $g_L = g_R$  case, is now an admixture of vector and axial vector parts. The weak angle  $\sin^2\theta_w$  is defined in the usual way as

$$\sin^2\theta_w = e^2/g_L^2 = (3g_{1C}^2/2g_L^2)/(3g_{1C}^2/2g^2 + 1) \quad (7)$$

Mere substitution of  $g_{L+R} = \left(\frac{3}{2}\right)^{1/2} g_{1C}$  in all the above expressions involving  $g_{1C}$  gives relations that are correct for the more general

$SU(2)_L \times SU(2)_R \times U(1)_{L+R}$  electroweak theory without recourse to any scheme

of unification. The relevant Higgs scalars in this case are

$A \sim (2, \bar{2}, 0)$ ,  $B \sim (1, 2, 1)$ ,  $C \sim (2, 1, 1)$ ,  $E \sim (1, 3, 1)$  with vacuum

expectation values  $\langle A \rangle = \text{diag}(a_1, a_2)$ ;  $\langle B \rangle = (0, b)$ ;  $\langle C \rangle = (0, c)$ ;

$\langle E \rangle = (0, \epsilon, 0)$ .

Eqs.(3) and (4) give the effective "low energy" interaction

Lagrangian for neutral current processes involving neutrinos and electrons as

probes <sup>5)</sup>. For muon neutrinos, the vector ( $g_V^{(f)}$ ) and axial-vector ( $g_A^{(f)}$ )

couplings of the fermion  $f$  ( $f = u, d, e$ ) in units of  $G_F/\sqrt{2}$  are:

$$g_V^u = \left\{ \frac{1}{(1 + g_L^2/g_R^2)} - \frac{4}{3} \sin^2\theta_w \right\} G_V + \frac{(g_L^2 - g_R^2)}{2(g_L^2 + g_R^2)} G_A \quad ; \quad g_A^u = \frac{1}{2} G_A \quad , \quad (8)$$

$$g_V^d = \left\{ \frac{-1}{(1 + g_L^2/g_R^2)} + \frac{2}{3} \sin^2\theta_w \right\} G_V - \frac{(g_L^2 - g_R^2)}{2(g_L^2 + g_R^2)} G_A \quad ; \quad g_A^d = -\frac{1}{2} G_A \quad , \quad (9)$$

$$g_V^e = \left\{ \frac{-1}{(1 + g_L^2/g_R^2)} + 2 \sin^2\theta_w \right\} G_V - \frac{(g_L^2 - g_R^2)}{2(g_L^2 + g_R^2)} G_A \quad ; \quad g_A^e = -\frac{1}{2} G_A \quad . \quad (10)$$

For electron neutrinos scattering over electrons the couplings are modified due to charged current contribution

$$E_V^e = 1 + g_V^e \quad ; \quad E_A^e = 1 + g_A^e \quad . \quad (11)$$

The  $G_V$  and  $G_A$  in Eqs.(8)-(11) are defined as

$$G_V = (a^2 + c^2) \{ (1 + g_L^2/g_R^2) a^2 + b^2 \} / \{ a^2(b^2 + c^2) + b^2c^2 \} \quad , \quad (12)$$

$$G_A = (a^2 + c^2) b^2 / \{ a^2(b^2 + c^2) + b^2c^2 \} \quad . \quad (13)$$

In electron-nucleon scattering the parity violating effects are described by

the cross current terms  $\frac{G_F}{\sqrt{2}} C_{VA}^q \bar{e} \gamma_\mu e \bar{q} \gamma^\mu \gamma_5 q$  and  $\frac{G_F}{\sqrt{2}} C_{AV}^q \bar{e} \gamma_\mu \gamma_5 e \bar{q} \gamma^\mu q$

( $q = u, d$ ) where

$$C_{VA}^u = \{-H_1 + \{2(1 + g_L^2/g_R^2) \sin^2\theta_w - 1\} H_2\} G_A \quad , \quad (14)$$

$$C_{AV}^u = \{-H_1 + \{4/3 (1 + g_L^2/g_R^2) \sin^2\theta_w - 1\} H_2\} G_A \quad , \quad (15)$$

$$C_{VA}^d = \{H_1 - \{2(1 + g_L^2/g_R^2) \sin^2\theta_w - 1\} H_2\} G_A \quad , \quad (16)$$

$$C_{AV}^d = \{H_1 - \{2/3 (1 + g_L^2/g_R^2) \sin^2\theta_w - 1\} H_2\} G_A \quad (17)$$

with  $H_1 = \{(g_L^2 - g_R^2)/2 (g_L^2 + g_R^2)\} (1 + b^2/c^2)$ ;  $H_2 = (1 - g_L^2 c^2/g_R b^2)/(1 + g_L^2/g_R^2)$ .

In deriving Eqs.(14) to (17) the momentum transfer  $q^2$  as compared with the masses  $m_{1(2)}$  has been neglected.

For neutrino neutral current interactions there are two cases of interest. (i) when  $a^2 = 0, G_V$  and  $G_A$  of Eqs.(9) and (10) are independent of  $b^2$  and  $c^2$ . Both are equal to unity. In this case the couplings in Eqs.(8) to (11) simplify to those of the standard  $SU(2)_L \times U(1)_{L+R}$  electroweak theory <sup>6)</sup>. These couplings do not carry any information about the masses of  $N_1$  and  $N_2$  and depend only on the weak angle  $\sin^2\theta_w$ . (ii) When  $b^2 \gg a^2, c^2$ , once again  $G_V$  and  $G_A$  are equal to unity and the  $SU(2)_L \times U(1)_{L+R}$  limit of the theory is achieved. In the second case the mass of  $N_2$  is much heavier than the mass of  $N_1$ .

The fermions in the theory acquire their masses from the vacuum expectation values of the Higgs multiplet A. If  $a^2 = 0$  then all the fermions are massless (or have vanishingly small masses for  $a \approx 0$ ). In Ref.5 the first case was referred to as the "chiral limit". Here the "chiral limit" case is considered in detail and the more general case in which  $a^2 \neq 0$  is left for later. For  $a^2 = 0$ , since all neutrino interactions are identical to the standard  $SU(2)_L \times U(1)_{L+R}$  theory, only the weak angle  $\sin^2\theta_w$  that parametrizes the amplitudes of the various interactions in Eqs.(8) to (11) is an experimentally accessible quantity. Taking the present world averaged <sup>7)</sup> value of  $\sin^2\theta_w = 0.23 \pm 0.015$ , Eq.(7) gives the following constraint on the gauge couplings:

$$(1 + g_L^2/g_R^2 + 2g_L^2/3g_{1C}^2)^{-1} = 0.23 \pm 0.015 . \quad (11)$$

For the case considered this is the maximum information that can be obtained from neutrino neutral current interactions. Further information on the gauge couplings comes from considering parity violating effects in electron nucleon scattering as is evident from the couplings from Eqs.(14) to (17). There are functions of  $\sin^2\theta_w$ , which is known from neutrino interactions,  $b^2/c^2$  and  $g_L^2/g_R^2$  that have now to be determined.

First, the predictions of the parity violating asymmetry for polarized electron-deuteron scattering <sup>8)</sup> are discussed for various values of  $g_L^2/g_R^2$ , since this is the most accurately measured quantity at present. Then the values of the weak charge in bismuth are given as predictions in the light of controversy surrounding the various measurements <sup>9)</sup>.

In discussing these results the approximation  $M_1^2, M_2^2 \gg q^2$  ( $\equiv$  momentum transfer) is implemented. Also, from Eq.(11) positivity of  $g_L^2/g_{1C}^2$  requires  $g_L^2/g_R^2$  to satisfy  $0 < g_L^2/g_R^2 < 3.08$  for the upper limit of  $\sin^2\theta_w = 0.245$  and  $0 < g_L^2/g_R^2 < 3.63$  for the lower limit of  $\sin^2\theta_w = 0.215$ .

The asymmetry  $A^{eD} = (\sigma_R - \sigma_L)/(\sigma_R + \sigma_L)$  for polarized electrons over deuterium is given by <sup>10)</sup>

$$A^{eD} = \frac{9G_F}{10\sqrt{2}\pi\alpha} \left\{ \left( \frac{2}{3} C_{AV}^u - \frac{1}{3} C_{AV}^d \right) + \frac{1 - (1-Y)^2}{1 + (1-Y)^2} \left( \frac{2}{3} C_{VA}^u - \frac{1}{3} C_{VA}^d \right) \right\}, \quad (12)$$

while the weak charge  $Q_w$  for heavy atoms with  $Z$  protons and  $(A-Z)$  neutrons is given by

$$Q_w = -2(A + Z) C_{AV}^u - 2(2A - Z) C_{AV}^d . \quad (13)$$

Table I gives predictions of  $A^{eD}$ ,  $Q_w$ ,  $M_1$  and  $M_2$  for various values of  $\sin^2\theta_w$  and  $g_L^2/g_R^2$  in the range discussed in the text. These values are to be compared with predictions of the  $SU(2)_L \times U(1)_{L+R}$  theory which are:

$\sin^2\theta_w$	0.19	0.2	0.215	0.23	0.245
$A^{eD}/q^2 \cdot 10^{-5}$	-10.2	-9.6	-8.9	-8.2	-73
$Q_w$	-105.6	-108	-113	-118	-123
$M_2 (= M_1, M_2 + \infty)$	96	93.7	91	89	87

From the above numbers predictions of  $A^{eD}$  lie in the allowed experimental range <sup>8)</sup>  $A^{eD}|_{\text{exp}} = -9.5 \pm 1.6 \times 10^{-5} q^2$  ( $Y = 0.21$ ) for values of  $\sin^2\theta_w \lesssim 0.23$ . On the other hand, from Table I, predictions of  $A^{eD}/q^2 \cdot 10^{-5}$  in the

$SU(2)_L \times SU(2)_R \times U(1)_{L+R}$  model can cover values of  $\sin^2 \theta_w > 0.23$  with  $g_L^2/g_R^2 > 1$ .<sup>11)</sup> Another point to observe is that for a fixed value of  $\sin^2 \theta_w$  and  $g_L^2/g_R^2$ ,  $|A^{eD}|$  increases while  $|Q_w|$  decreases with increasing  $b^2/c^2$  ( $M_1$  and  $M_2$  increase with increasing  $b^2/c^2$ ). At present the controversy surrounding the experimental measurements are such that they admit  $Q_w$  from order -40 to order -125. Therefore by varying  $g_L^2/g_R^2$  in the range 1 to 3 and masses ( $M_1, M_2$ ) for a fixed  $\sin^2 \theta_w$  it is possible to accommodate the results of these experiments. For example, with  $\sin^2 \theta_w = 0.23$ ,  $A^{eD}/q^2 \cdot 10^{-5}$  is -9.5 for the sets ( $Q_w = -41$ ,  $M_1 = 81$  GeV,  $M_2 = 152$  GeV,  $g_L^2/g_R^2 = 2$ ), ( $Q_w = -83$ ,  $M_1 = 85$  MeV,  $M_2 = 262$  GeV,  $g_L^2/g_R^2 = 2.5$ ), ( $Q_w = -91$ ,  $M_1 = 85$  GeV,  $M_2 = 450$  GeV,  $g_L^2/g_R^2 = 3.0$ ). In the light of the above discussion more accurate measurements of  $Q_w$  are called for. If  $Q_w$  is found to fall short of the predicted  $SU(2)_L \times U(1)_{L+R}$  value at fixed  $\sin^2 \theta_w$ , this will be "low energy" evidence in favour of the  $SU(2)_L \times SU(2)_R \times U(1)_{L+R}$  structure with the modification of  $g_L \neq g_R$  as the symmetry underlying the electroweak interactions. Measuring the asymmetry  $A^{eD}$  at various values of  $Y$  will also help. Other equally important tests of the theory are measurements of parity violating asymmetries in electron-proton scattering and determining the couplings  $C_{AV}^{u,d}$ ,  $C_{VA}^{u,d}$  (Eqs.(14)-(17)) directly from electron-hydrogen scattering.

Finally, conventional ideas on the evolution of coupling constants in grand unified theories can lead to  $g_L^2 > g_R^2$  at some renormalization point at low energies usually taken to be the mass of the charged weak boson  $W_L$ . For example,  $g_L$  and  $g_R$  are equal when  $SO(10)$  descends to  $SU(2)_L \times SU(2)_R \times SU(4)_{L+R}^C$ . To achieve  $g_L^2/g_R^2 > 1$ , the  $SU(2)_R$  must break earlier than  $SU(2)_L$ . Much earlier breaking of  $SU(2)_R$  over  $SU(2)_L$  can lead to the desired value  $g_L^2 \sim (2 \text{ to } 3) g_R^2$ . In this case  $\langle E \rangle \sim (1, 3, 1)$  will be several orders of magnitude greater than  $\langle E \rangle \sim (1, 2, 4)$ . These ideas, the more general case of  $a^2 \neq 0$ , and variation of  $A^{eD}$  with  $Y$  will be covered in a later publication.

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- 1) J.C. Pati and Abdus Salam, Phys. Rev. D10, 275 (1974);  
R.N. Mohapatra and J.C. Pati, Phys. Rev. D11, 566 (1975);  
R.N. Mohapatra and G. Senjenovic, Phys. Rev. D12, 1502 (1975);  
H. Fritsch and P. Minkowski, Nucl. Phys. B102, 61 (1976);  
J.C. Pati, S. Rajpoot and Abdus Salam, Phys. Rev. D17, 131 (1978).
- 2) S. Rajpoot, Phys. Rev. D22, 2244 (1980);  
T.J. Goldman and D.A. Ross, Phys. Letters B84, 208 (1979);  
R.N. Mohapatra and G. Senjenovic in Workshop on Weak Interactions and Related Topics, Blacksburg, Virginia, December (1979).
- 3) S. Rajpoot, "Left-right asymmetric model for weak and electromagnetic interactions", ICTP, Trieste, preprint IC/78/64 (unpublished).
- 4) J.C. Pati and Abdus Salam, Phys. Rev. D10, 275 (1974).
- 5) J.C. Pati, S. Rajpoot and Abdus Salam, Phys. Rev. D17, 131 (1978).
- 6) S.L. Glashow, Nucl. Phys. 22, 579 (1961);  
S. Weinberg, Phys. Rev. Letters 19, 1264 (1967);  
Abdus Salam in Elementary Particle Theory: Relativity Groups and Analyticity, Ed. N. Svartholm (Wiley, N.Y. 1968).
- 7) J.E. Kim, P. Langacker, M. Levine and H.H. Williams, Rev. Mod. Phys. 53, 211 (1981).
- 8) C.Y. Prescott et al., Phys. Letters B77, 347 (1978).
- 9) P.G.H. Sanders in Unification of Elementary Forces and Gauge Theories, Ed. D.B. Cline and F.E. Mills (Harwood Academic, London 1977), p.153;  
P.E.G. Baird et al., Phys. Rev. Letters 39, 798 (1977);  
L.M. Barkov and M.S. Zolotarev, JETP Letters 27, 375 (1978), also in Neutrino '78, Ed. E.C. Fowler (Purdue Univ., West Lafayette, Indiana), p.423.
- 10) R.N. Cahn and F.J. Gilman, Phys. Rev. D17, 1313 (1978);  
M. Yoshimura, Progr. Theoret. Phys. (Kyoto) 59, 231 (1978).
- 11) Fit to  $A^{eD}$  exist for  $g_L^2/g_R^2 < 1$ . But values of  $\sin^2 \theta_w$  lower than 0.20 are required.

Table I

Predictions of masses  $M_1, M_2$  (in GeV), parity violating effects  $A^{eD}$  (in units of  $q^2 10^{-5}$ ,  $\gamma = 0.21$ ) and  $Q_w$  in electron-nucleon scattering in  $SU(2)_L \times SU(2)_R \times U(1)_{L+R}$  theory.

$\sin^2 \theta_w$ $g_L^2/g_R^2$	0.215						0.230						0.245													
	1.5		2		2.5		3		1.5		2		2.5		3		1.5		2		2.5		3			
	$M_1$	89	80.8	84	85	276	85	81.8	81	80	82	68	76	77.5	80	81.3	84.7	84	84.5	83	82	80	81.3	83	80	
$M_2$	177	135	185	276	276	276	132	152	189	339	110	147	215	656	366	366	146	171	240	734	240	734	240	734	10.9	
$A^{eD}$	-6.0	-9.9	-11.0	-11.2	-11.2	-11.2	-7.0	-9.5	-11.2	-11.2	-11.2	-4.1	-4.1	-4.1	-4.1	-4.1	-6.2	-9.9	-9.9	-10.9	-10.9	-10.9	-10.9	-10.9	-10.9	
$Q_w$	-76.8	-21.5	-51	-51	-51	-51	-40.6	-41	-41	-41	-41	-41	-41	-41	-41	-41	-12	-21.5	-42	-67	-67	-67	-67	-67	-67	
$M_1$	89.5	85	86	86	86	86	86.2	85	83	83.3	81.4	80	80	81.3	81.4	81.4	84	84.5	83	82	80	81.3	83	80	81.3	
$M_2$	205	157	205	287	287	287	177	194	223	366	146	171	240	734	366	366	146	171	240	734	240	734	240	734	10.9	
$A^{eD}$	-8.2	-9.5	-10.5	-11.0	-11.0	-11.0	-7.5	-8.9	-10.2	-10.2	-10.2	-6.7	-6.7	-6.7	-6.7	-6.7	-6.9	-9.0	-9.0	-10.1	-10.1	-10.1	-10.1	-10.1	-10.1	
$Q_w$	-87	-52	-65	-71.5	-71.5	-71.5	-80	-76	-67	-74	-58	-56	-63	-80	-74	-74	-58	-56	-63	-80	-80	-80	-80	-80	-80	
$M_1$	90	89	88	87.5	87.5	87.5	87.5	86	85	84.7	84	84.5	83	82	84.7	84.7	84	84.5	83	82	80	81.3	83	80	81.3	
$M_2$	238	230	250	336	336	336	223	221	262	416	179	255	306	804	416	416	179	255	306	804	306	804	306	804	10.9	
$A^{eD}$	-8.4	-9.2	-9.9	-10.4	-10.4	-10.4	-78	-87	-83	-85	-85	-83	-83	-85	-85	-85	-7.0	-8.0	-9.0	-9.5	-9.5	-9.5	-9.5	-9.5	-9.5	
$Q_w$	-94	-88	-83	-84	-84	-84	-95	-87	-83	-85	-83	-83	-83	-85	-85	-85	-83	-97	-89	-88	-88	-88	-88	-88	-88	
$M_1$	90.3	89.6	89	88	88	88	88	87	86	85	86	85	84	83	85	85	86	85	84	83	82	80	81.3	83	80	81.3
$M_2$	268	266	288	353	353	353	268	273	312	450	270	285	352	868	312	312	270	285	352	868	352	868	352	868	10.9	
$A^{eD}$	-8.5	-9.1	-9.6	-10.3	-10.3	-10.3	-7.9	-8.5	-9.1	-9.1	-9.1	-8.5	-8.5	-9.1	-9.1	-9.1	-7.2	-7.9	-8.5	-9.2	-9.2	-9.2	-9.2	-9.2	-9.2	
$Q_w$	-98.5	-95	-91	-87	-87	-87	-103	-99	-95	-95	-95	-95	-95	-99	-95	-95	-107	-103	-98	-98	-98	-98	-98	-98	-98	

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