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FUSION REACTION SPECTRA
PRODUCED BY ANISOTROPIC FAST IONS
IN THE PLT TOKAMAK

By

W.W. Heidbrink

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ABSTRACT

For "beam-target" fusion reactions, collimated measurements of the energy spectrum of one of the reaction products can provide information on the degree of anisotropy of the reacting beam ions. Measurements of the spectrum of 15 MeV protons produced by reactions between energetic ^3He ions and relatively cold deuterons during fast wave minority heating in the PLT tokamak indicate that the velocity distribution of fast ^3He ions is peaked perpendicular to the tokamak magnetic field.

W. W. Hedbrink

1. INTRODUCTION

Several authors [1,2] have related the energy distribution of neutrons produced by thermonuclear reactions to the temperature of the reactants, but no analytical treatments and only one set of numerical calculations [3] relating the distribution function of non-thermal reactants to the energy spectrum of fusion reaction products has been published. In actual controlled fusion experiments, however, the largest fusion reaction rates [4] and the most easily measured fusion spectra are achieved in plasmas with non-thermal populations. Measurements of these spectra can provide information about the "tail" (non-thermal part) of the distribution function that may be difficult to obtain using other diagnostic techniques. To date, there have been only a few spectral measurements of fusion neutrons made with narrowly collimated detectors [5-9], in part due to the massive collimators required to reject scattered neutrons when using conventional detection techniques. Recently, it has demonstrated the feasibility of charged fusion product detection in magnetic fusion experiments using surface barrier detectors [10,11]. With these detectors, measurements of tokamak fusion spectra with compact collimation and ~ 100 keV energy resolution are possible [10,12].

This paper presents analytical expressions for the fusion energy distribution produced in reactions between a bi target ions and a monoenergetic, possibly anisotropic, beam for the case of a tri- α reaction that is isotropic in the center-of-mass (cm) frame. It then applies these expressions to recent measurements of the 15 MeV proton spectrum produced during fast wave minority heating in the PLT tokamak [13]. The measurements reported here improve the energy resolution of 15 MeV proton spectral measurements made previously on PLT-14, where the highest proton energies were cut off by the finite width of the surface barrier detector. When the full energy of all the protons is measured, the asymmetric, downward-shifted spectrum reported previously becomes a spectrum with two peaks separated by about 2 MeV. Analysis of this spectrum in terms of a model two-component distribution function that has one component purely perpendicular and the other purely isotropic in velocity space indicates that $\sim 90\%$ of the high energy ^3He ions created by the waves have velocities perpendicular to the tokamak toroidal field.

2. THEORY

For a reaction $2(1,3)4$ where particles 1,2,3,4 are the projectile, target, and products,

respectively, the energy of particle 3 using non-relativistic kinematics is [1]

$$E_3 = \frac{m_4}{m_3 + m_4} (Q + K) + V \cos \theta \sqrt{\frac{2m_3 m_4}{m_3 + m_4} (Q + K) + \frac{1}{2} m_3 V^2}, \quad (1)$$

where Q is the fusion energy, $K = \frac{1}{2} m_1 m_2 v^2 / (m_1 + m_2)$ is the relative kinetic energy, $\vec{v} = \vec{v}_1 - \vec{v}_2$ is the relative velocity, $\vec{V} = (m_1 \vec{v}_1 + m_2 \vec{v}_2) / (m_1 + m_2)$ is the cm velocity, and θ is the angle between \vec{V} and the cm velocity of particle 3. Our objective is to deduce the energy distribution of product 3, $F(E_3)$, given the reactant distributions $f_1(\vec{v}_1)$ and $f_2(\vec{v}_2)$ and the reaction probability $\sigma v(v, \theta)$. We assume that the fusion cross section is isotropic in angle, i.e., $\sigma = \sigma(v)$, which is valid for the $d(t, n)$ and $d(^3\text{He}, p)\alpha$ fusion reactions below the resonance energy [15,16]. The $d(d, p)$ and $d(d, n)$ fusion reaction cross sections are of the form [2]

$$\sigma_{dd}(v, \theta) \approx A(v) (1 + B \cos^2 \theta), \quad (2)$$

where $B \sim 0.1 - 0.3$ so our treatment is only approximately valid for these reactions. In laboratory plasmas, the fusion energy Q is several orders of magnitude larger than the reactant kinetic or cm energy so we order the equation in half-integer powers of the small parameter $\epsilon = m_3 V^2 / Q$ and neglect terms that enter in order $\epsilon^{\frac{3}{2}}$. For most cases of interest $\sigma(v)$ is a rapidly increasing function of the relative velocity so that the weighting factor $\sigma v f_1(\vec{v}_1) f_2(\vec{v}_2)$ is largest when v is maximized. For ion distributions f_1 and f_2 with comparable velocities, such as in a thermonuclear plasma, v is largest when the reactants collide head on. This implies that most reactions occur with the cm velocity $V \sim 0$, which from Eq. (1) implies that the resulting fusion-product energy distribution is peaked about $E_3 = m_4(Q + K) / (m_3 + m_4)$ [1]. Here, however, we consider the special case of "beam-target" reactions for which $v_1 \gg v_2$, which implies $\sigma(v) \approx \sigma(v_1)$ independent of \vec{v}_2 . Under these conditions, it is only the distribution function of the beam and the cross section that determine the fusion-product energy distribution. The general expression for the fusion-product energy distribution function $F(E_3)$ becomes

$$\int_{E_l}^{E_u} F(E_3) dE_3 \propto \int \sigma(v_1) v_1 f_1(\vec{v}_1) H(\vec{v}_1) d\vec{v}_1, \quad (3)$$

$$\text{where } H(\vec{v}_1) = \begin{cases} 1, & \text{if } E_l < E_3(\vec{v}_1) < E_u; \\ 0, & \text{otherwise.} \end{cases}$$

Due to a particle's fast gyromotion in a magnetically confined plasma, the particle distribution function is independent of direction in the plane perpendicular to the magnetic

field, $f(\vec{v}_\perp, v_\parallel) = f(v_\perp, v_\parallel)$. We denote the angle made by the magnetic field vector and the beam particle velocity by χ_1 and the angle between the field and the velocity vector of the fusion product by χ_3 . The cm angle θ can be reexpressed in terms of the laboratory angle ϕ between the projectile velocity \vec{v}_1 and the product velocity \vec{v}_3 according to

$$\cos \theta = \cos \phi - V \sqrt{\frac{m_3(m_3 + m_4)}{2m_4Q}} \sin^2 \phi + O(\epsilon). \quad (4)$$

Substituting into Eq. (1) yields

$$E_3 = \frac{m_4}{m_3 + m_4} (Q + K) + V \sqrt{\frac{2m_3m_4}{m_3 + m_4}} (Q + K) \cos \phi + \frac{1}{2} m_3 V^2 (1 - 2 \sin^2 \phi) + O(Q\epsilon^{\frac{3}{2}}). \quad (5)$$

The next step is to carry out the angular integration in Eq. (3). Define a reduced fusion-product energy distribution function $\hat{F}(E)$. For the special case of a monoenergetic beam, $f_1(\vec{v}_1) = \delta(v - v_b)g(\vec{v}_1/v_1)$. Since \hat{F} is a monotonic function of the lab frame angle ϕ , $\hat{F}(E) \propto (dE/d\phi)^{-1}g(\phi)$. For an isotropic monoenergetic beam $g(\phi) = \sin \phi$ and

$$\int_{E_i}^{E_u} \hat{F}(E) dE = \ln \left(\frac{1 + k_0 \frac{(E_u - E_0^i)}{\Delta E}}{1 + k_0 \frac{(E_l - E_0^i)}{\Delta E}} \right) / \ln \left(\frac{1 + k_0}{1 - k_0} \right), \quad (6)$$

$$\text{for } |E - E_0^i| < \Delta E,$$

$$\text{where } E_0^i = \frac{m_4}{m_3 + m_4} (Q + K) + \frac{1}{2} m_3 V^2,$$

$$\Delta E = V \sqrt{\frac{2m_3m_4}{m_3 + m_4}} (Q + K), \quad \text{and}$$

$$k_0 = V \sqrt{\frac{2m_3(m_3 + m_4)}{m_4Q}}.$$

For a monoenergetic beam that is unidirectional in pitch angle but isotropic in gyro angle

$$\int_{E_l}^{E_u} \hat{F}(E) dE = \frac{1}{\pi} \left[\sin^{-1} \left(\frac{E - E_0^a}{k_1 \Delta E} \right) + k_2 \sqrt{1 - \left(\frac{E - E_0^a}{k_1 \Delta E} \right)^2} \right]_{E=E_l}^{E=E_u} \quad (7)$$

$$\text{for } |E - E_0^a| < k_1 \Delta E,$$

$$\text{where } E_0^a = E_0^i + \Delta E \left[\cos \chi_1 \cos \chi_3 - \frac{k_0}{2} (\cos^2 \chi_1 \sin^2 \chi_3 + \sin^2 \chi_1 \cos^2 \chi_3) \right]$$

$$k_1 = \sin \chi_1 \sin \chi_3 (1 + k_0 \cos \chi_1 \cos \chi_3), \quad \text{and}$$

$$k_2 = \frac{1}{2} k_0 \sin \chi_1 \sin \chi_3 / (1 + k_0 \cos \chi_1 \cos \chi_3).$$

The accuracy of Eq. (7) was tested by integrating it numerically over $\sin \chi_1 d\chi_1$ to recover the isotropic distribution Eq. (6). The final result for the fusion-product energy distribution function is found by taking the weighted average of reduced distribution functions

$$F(E_3) = \int dE_1 \sigma(E_1) E_1 f_1(E_1) \hat{F}(E_3, E_1). \quad (8)$$

If the beam distribution function $f_1(E_1)$ decreases rapidly with energy [e.g., if $f_1(E_1)$ is a Boltzmann distribution], then the weighting factor $\sigma(E_1) E_1 f_1(E_1)$ peaks strongly for some energy $E_1 = E_{peak}$ and the fusion-product energy distribution function is approximately

$$F(E_3) \simeq \hat{F}(E_3, E_{peak}). \quad (9)$$

The relation Eq. (9) is useful for qualitative interpretation of 15 MeV proton spectra produced during ICRF heating.

The reduced distribution functions Eqs. (7) and (6) are plotted in Figs. 1a and 1b. The physical origin of the twin lobes (Fig. 1a) for a perpendicular beam distribution viewed in the perpendicular plane is that the probability of a reaction is constant over a gyro period but more of the orbit forms an angle θ near $|\cos \theta| = 1$ than near $\sin \theta = 0$ (Fig. 1c).

3. EXPERIMENT

In the experiment, ^3He minority ions were heated in a bulk deuterium plasma by magnetosonic fast waves [13]. 15 MeV protons produced by the $d(^3\text{He}, p)\alpha$ fusion reaction were detected with a proton spectrometer used previously on PLT [14]. The spectrometer was modified to use a surface barrier detector with a depleted region of 1800 μm , so that protons with energies up to 20 MeV deposited their full energy in the depleted region of the detector. The previous apparatus only collected the full energy of protons with less than 15.5 MeV. The spectrometer was collimated to measure perpendicular protons (collimator FWHM = 6.5°) produced in the plasma between major radii of approximately 102 cm and 140 cm, with nearly constant detection efficiency over this range [14]. The ^3He cyclotron layer was at major radii of 125–143 cm for these discharges.

The measured 15 MeV proton spectra exhibit a broad, two-lobed structure (Fig. 2a) for discharges characterized by plasma currents of 500–550 kA, toroidal fields of 28–32 kG, line-average electron densities of $1.7\text{--}3.0 \times 10^{13} \text{ cm}^{-3}$, ICRF powers of 100–500 kW at 30 MHz, and $d(^3\text{He}, p)\alpha$ reaction rates of $\gtrsim 10^{11} \text{ sec}^{-1}$. In contrast, co-injection of a 40 keV deuterium neutral beam into a deuterium and ^3He plasma in the absence of ICRF

produced a relatively narrow 15 MeV proton spectrum with a single peak (Fig. 2b). The width of the proton spectrum during ICRF was found to depend less sensitively on electron density, ICRF power, toroidal magnetic field, and ${}^3\text{He}$ density than the $d({}^3\text{He,p})\alpha$ reaction rate (Fig. 3). Operation of the spectrometer was restricted to a relatively narrow parameter regime by the requirement that the reaction rate be sufficiently large for statistically significant measurements but sufficiently small to avoid appreciable pulse pile-up. The ratio of counts in the low energy peak to the number of counts in the central minimum was 1.68 ± 0.29 for discharges with full spectral width ≥ 2.7 MeV; the ratio of counts in the high energy peak to counts in the central minimum was 1.38 ± 0.22 .

4. DISCUSSION

A twin-lobed spectrum cannot be produced by an isotropic beam. Although these spectral measurements of protons at a single angle of escape do not provide enough information to determine uniquely the direction of anisotropy of the ${}^3\text{He}$ tail, they are consistent with theoretical predictions of a perpendicular anisotropic tail [14,17]. The spacing of the lobes implies that perpendicular ${}^3\text{He}$ ions with energy of ~ 40 keV in the case of the most closely spaced peaks and ~ 300 keV in the case of the most widely spaced peaks made the dominant contribution to the observed proton spectra. Theoretically, the ${}^3\text{He}$ distribution is predicted to be perpendicular for energies $\gtrsim 20Z_{eff}^3 T_e \sim 30$ keV [17]. The instrumental resolution was too poor in these experiments to determine the minimum energy at which anisotropy exists. The ratio of counts between lobes to the number of counts in the peaks implies that the isotropic contribution to the observed spectrum is less than 10% of the perpendicular contribution.

The observation that the proton spectral width is less sensitive to the parameters affecting ${}^3\text{He}$ tail heating than the $d({}^3\text{He,p})\alpha$ reaction rate (Fig. 3) is consistent with theoretical expectations. Asymptotic analysis [18] of Eq. (8) using an analytical fit to the cross section σ [19] and the assumed ${}^3\text{He}$ distribution function $f_1(E_1) \propto \exp(-E/T)$, where T is the tail temperature, indicates that the energy E_{peak} for which the weighting factor $\sigma E f$ is maximized depends on tail temperature according to $E_{peak} \simeq 14(\text{keV})^{\frac{1}{2}} T^{\frac{3}{2}}$. This implies that the spectral width scales approximately as $T^{\frac{1}{2}}$. In contrast to this weak algebraic dependence on tail temperature, the analysis predicts a strong exponential dependence of the $d({}^3\text{He,p})\alpha$ reaction rate R_{dHe} on tail temperature, $R_{dHe} \sim \exp[-43(\text{keV}/T)^{\frac{1}{2}}]$. The reaction rate also depends on the number density of ${}^3\text{He}$ tail ions, while the proton spectrum produced by the minority tail depends on tail temperature alone. Combining expressions,

the spectral width W is expected to scale with reaction rate R and ^3He density n as

$$W_2 = W_1 [1 + 0.023 T_1^{\frac{1}{2}} \ln(\frac{n_2 R_1}{n_1 R_2})]^{-1}. \quad (10)$$

The predictions of Eq. (10) are plotted in Fig. 3 using the measured value of the reaction rate and a single normalization ($W_1 = 3.0 \text{ MeV}$, $R_1 = 4 \times 10^{11} \text{ sec}^{-1}$, $n_1 \simeq 1.0 \times 10^{12} \text{ cm}^{-3}$, $T_1 \simeq 40 \text{ keV}$ is implied by $W_1 = 3.0 \text{ MeV}$). A major uncertainty in the application of Eq. (10) is determination of the ^3He density, which was estimated from the rise in electron density when neutral ^3He was puffed into the vacuum vessel $\sim 50 \text{ ms}$ prior to the ICRF pulse, but which differs from this value due to ^3He pumping and desorption [20]. The measured scaling of spectral width with reaction rate is consistent with the theoretical prediction of Eq. (10) within the experimental error (Fig. 3). When the ^3He gas puff was reduced so that the density rise was below the minimum detectable level ($\Delta \bar{n}_e \lesssim 0.2 \times 10^{12} \text{ cm}^{-3}$) (Fig. 3d), the spectral width broadened slightly, implying that the tail temperature continued to rise with decreasing ^3He concentration; but the reaction rate fell, implying that the reduction in number density of ^3He ions had a stronger effect on the reaction rate than the increase in tail temperature.

The probable explanation for the asymmetric, downward-shifted proton spectra observed previously in PLT [14] is that the thinner detector used in those experiments failed to collect the full energy of the protons in the upper lobe of the distribution (Fig. 4).

5. CONCLUSION

Measurements of the spectrum of 15 MeV protons produced during fast wave minority heating in the PLT tokamak indicate that $\gtrsim 90\%$ of $\sim 200 \text{ keV}$ ^3He ions near the major radius of the device are anisotropic in velocity space. The width of the proton spectrum is increased by increasing the RF power, by reducing the electron or ^3He density, and by adjusting the toroidal field so that the ^3He resonance layer is in the center of the discharge, but measurements of the $d(^3\text{He}, p)\alpha$ reaction rate are much more sensitive to changes in tail temperature than are the spectral measurements. The tail temperature implied by the spectral measurements is typically between 30 and 50 keV.

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Figure Captions

Fig. 1a. Spectrum of protons emitted perpendicular to the magnetic field ($\chi_3 = \pi/2$) by $d(^3\text{He},p)\alpha$ fusion reactions between an anisotropic ($\chi_1 = \pi/2$), monoenergetic (200 keV) ^3He beam and a cold deuterium plasma. The asymmetry between the higher energy and lower energy peaks originates in the transformation from the cm frame to the laboratory frame.

Fig. 1b. Spectrum of protons emitted perpendicular to the magnetic field by $d(^3\text{He},p)\alpha$ fusion reactions between an isotropic monoenergetic (200 keV) ^3He beam and a cold deuterium plasma.

Fig. 1c. Physical explanation for the twin-lobed structure of a proton spectrum produced by an anisotropic perpendicular beam. Although the probability that a reaction occurs is constant during a beam ion's circular gyromotion, $\vec{v}_1 \cdot \vec{v}_3$ does not vary uniformly during a gyro period, causing more ions to be emitted with a maximal Doppler shift than without any shift.

Fig. 2a. Proton spectrum during ^3He minority ICRF heating (240 kW) in a discharge with $I_\phi = 500$ kA, $n_e = 2.7 \times 10^{13} \text{cm}^{-3}$, and $B_\phi = 30.5$ kG. The curve is the spectrum produced by an anisotropic perpendicular ^3He beam with maximum energy of 400 keV and temperature of 30 keV. The absolute accuracy of the energy measurement is $\pm 2.5\%$; the resolution of the spectrometer is 0.5 MeV (full line-width).

Fig. 2b. Proton spectrum during co-injection of a 40 keV deuterium neutral beam into a deuterium and ^3He plasma in the absence of ICRF. The curve is the spectrum produced by an isotropic 40 keV deuterium beam with a classical slowing-down distribution ($f(v) \propto v^{-3}$).

Fig. 3. 15 MeV proton spectral width and $d(^3\text{He},p)\alpha$ reaction rate versus line-average electron density (a), toroidal field (b), ICRF power (c), and estimated line-average ^3He density (d) with the other parameters held constant. $I_\phi \simeq 500$ kA. The dashed curve through the reaction rate data is the fit used to calculate the spectral width predicted by the asymptotic analysis of Sec. 4 (solid curves).

Fig. 4. A good fit to the asymmetric proton spectrum measured previously [14] is found by assuming that the true proton spectrum was produced by an anisotropic perpendicular ^3He beam with maximum energy 400 keV and temperature 50 keV but that

this spectrum was distorted by a thin detector with the model response

$$E_{det} = \begin{cases} E_p, & \text{if } E_p \leq 15.4 \text{ MeV}; \\ 3(15.4 \text{ MeV} - 2E_p), & \text{if } E_p > 15.4 \text{ MeV}. \end{cases}$$

The model detector response is based on calculations summarized in Fig. 2.5 of [21]. The counts below 12.5 MeV in the data are thought to be protons that lose energy in the walls of the collimator.

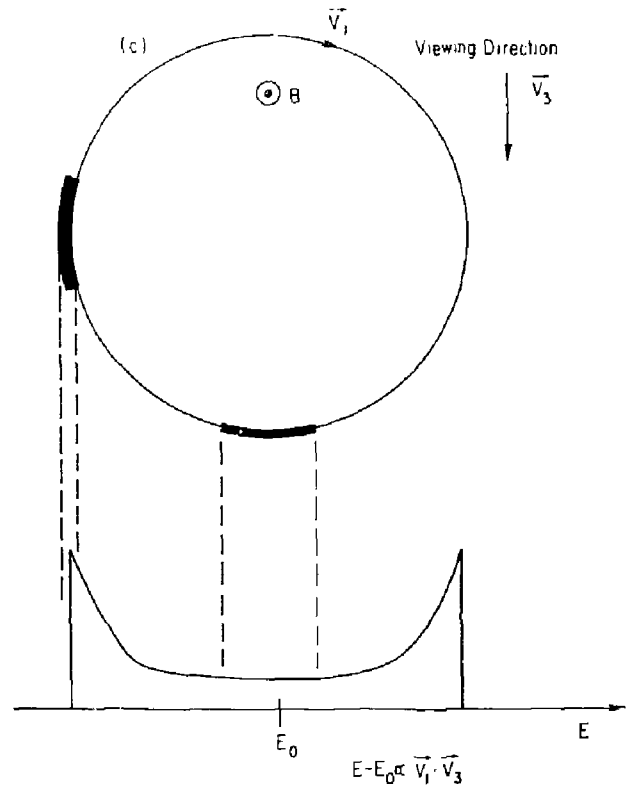
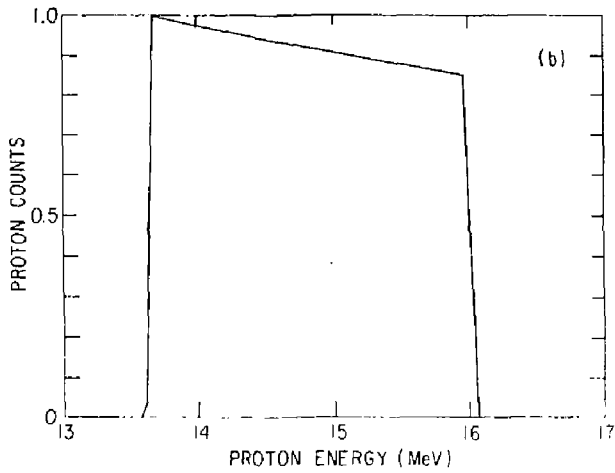
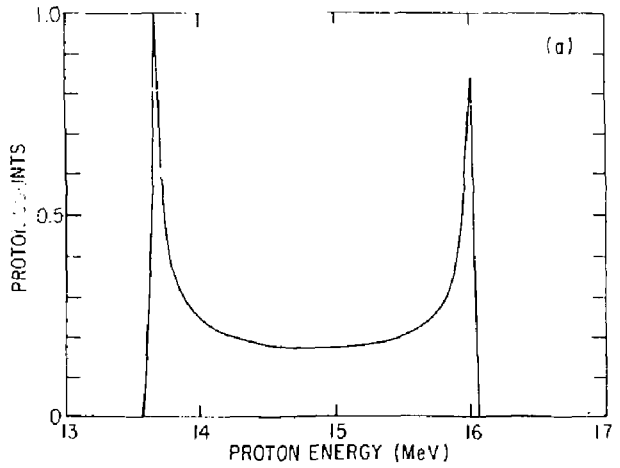


Fig. 1

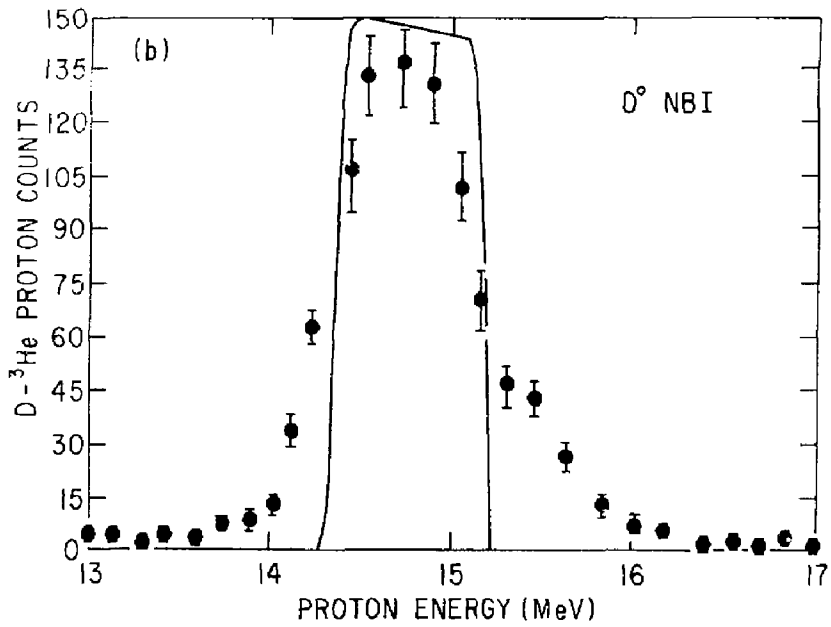
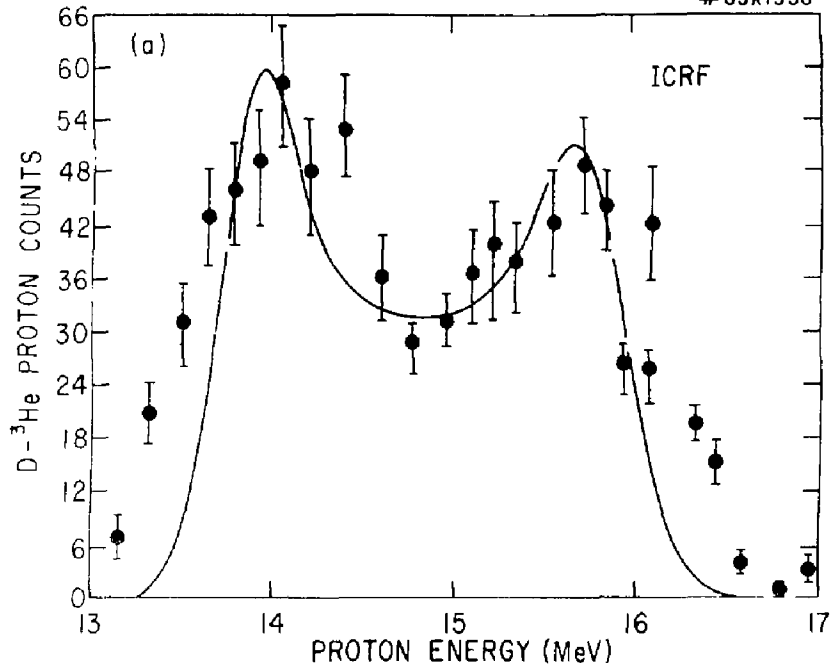


Fig. 2

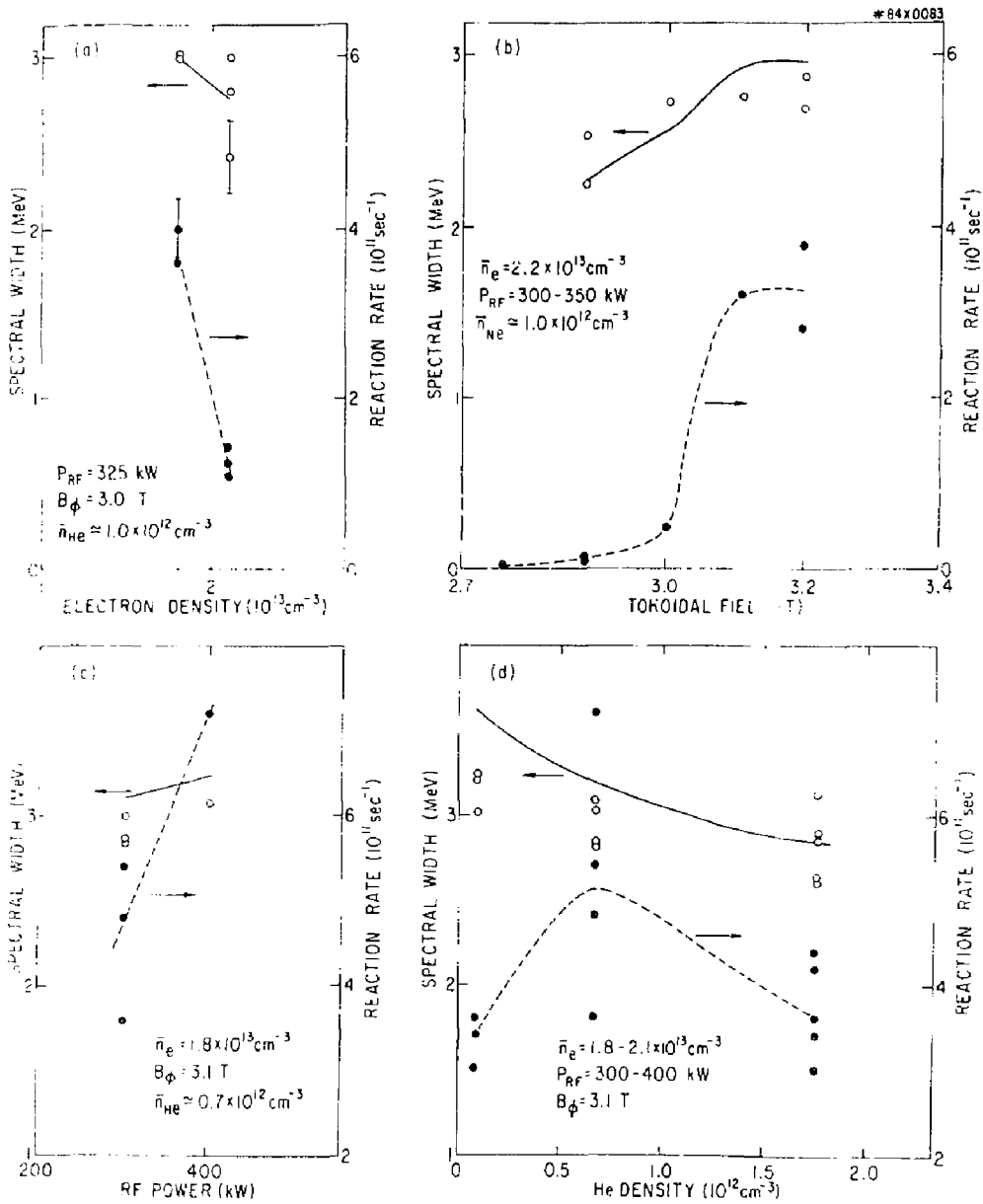
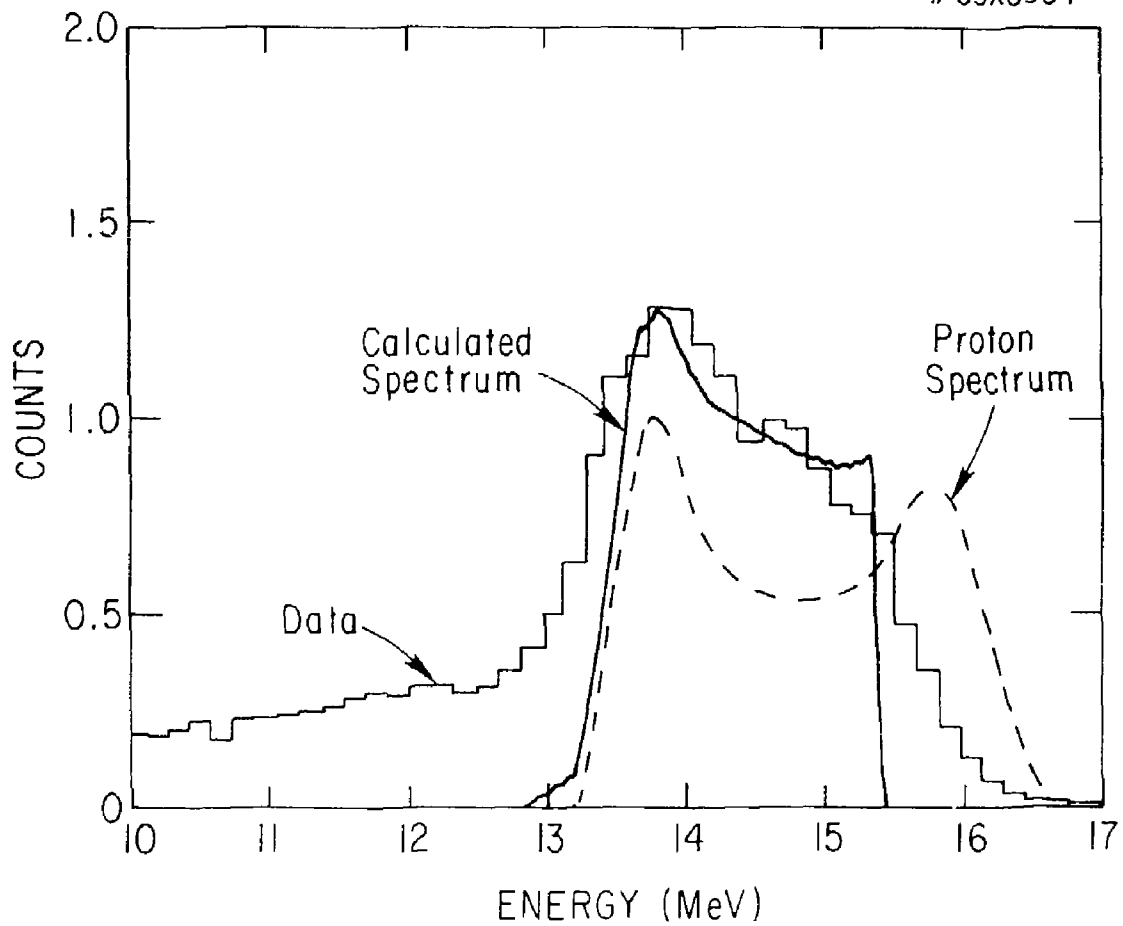


Fig. 3

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