

**THE FORMATION AND REACTIVITY OF THE μ^+ MOLECULAR ION NeMu^+**

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Abstract

Evidence for the formation and reactivity of the positive muon molecular ion NeMu^+ at room temperature in a low pressure Ne moderator to which trace amounts of Xe, CH_4 , NH_3 or He have been added, is reported. A two component relaxation of the diamagnetic muon spin rotation (μSR) signal is seen upon the addition of trace amounts of Xe to Ne; a fast relaxing component with bimolecular rate constant $(3.6 \pm 0.6) \times 10^{-10} \text{ cc atom}^{-1} \text{ s}^{-1}$ is thought to be due to thermal muonium formation in a charge exchange process while the other slow relaxing component is attributed to a muon transfer reaction, as in proton transfer studies. With CH_4 or NH_3 added to Ne there is, at most, only a very slow relaxation seen, even though thermal muonium formation is expected, in analogy with Xe. These latter results may be due to very fast, possibly tunneling assisted, muon transfer reactions, the first time that such processes have been at all characterized.

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1. Introduction

The study of both molecular ion bound states and ion-molecule reactions, particularly those involving the rare gas hydrides, has long been of interest to the chemical physics community [1-15]. The positive muon (μ^+) and its muonium atom ($Mu = \mu^+e^-$), with a mass only 1/9 that of the proton, can be considered a useful complement to the proton in atomic and molecular physics studies [16-23]; the most recent example being the calculations of Fournier and Govers of the rovibrational levels of the μ^+ analogs of HeH^+ ($HeMu$) $^+$ and NeH^+ ($NeMu$) $^+$ [16]. In fact, within the Born-Oppenheimer approximation, the positive muon (Mu atom) is chemically identical to the proton (H atom) and its unprecedented light mass provides for the possibility of observing very large isotope effects [16, 19, 24]. In particular, a study of rare gas "muides" of the positive muon, in comparison with their protonic cousins, should provide important information on both the nature of the intramolecular potential as manifest in the spectrum and lifetimes of bound and quasi-bound rovibrational levels, and on the dynamics of specific ion-molecule reactions.

In a muon spin rotation (μSR) experiment, evidence pertaining to the formation and reactivity of μ^+ molecular ions in general can be obtained from a measurement of the amplitudes and relaxation rates of the corresponding μSR signal in a given moderator. This idea was first explored in some preliminary experiments at the now defunct 184" cyclotron in Berkeley [25] with further measurements carried out at TRIUMF in ~1978 where the molecular ions $NeMu^+$ and $HeMu^+$ were tentatively identified [17, 18]. Hughes in fact first predicted that diamagnetic muon relaxation in pure He could be due to a spin rotation interaction of $HeMu^+$ and he estimated the corresponding magnetic field to be ~30 G [22]. This would correspond, however, to a relaxation rate about an order of magnitude faster than is actually observed [17]. In refs. [17] and [18], the magnetic field, limited to <75 G, was sufficiently low and inhomogeneous over the large stopping volume of the target that a reliable measurement of the diamagnetic muon relaxation rate was compromised. We have recently constructed a set of 1.5 m diameter Helmholtz coils capable of homogeneous fields up to 300 G which allow a much more precise determination of such rates. The first studies with this apparatus characterizing

the existence and reactivity of the NeMu^+ molecular ion are reported herein. Comparison with the thesis data of ref. [17] is also made. The results are of importance not only to the theoretical concepts referred to above but also to an understanding in general of the actual diamagnetic environment of the positive muon as a result of its various thermalization processes in matter [20, 26].

2. The μSR signal in gases

Positive muons are produced with kinetic energies of about 4 MeV (or greater) and 100% longitudinally spin polarized in the decay of positive pions ($\pi^+ \rightarrow \mu^+ \nu_\mu$). After traversing beam line and gas target windows and a defining muon counter, the μ^+ enters the gas with about 2.5 MeV of energy, far greater than energies of atomic interest. Most of the muon's energy is lost in Bethe-Bloch ionization of the stopping medium until a kinetic energy of ~ 35 keV is reached. At this point, muonium formation begins to be important and the muon enters into a series of charge exchange cycles with the moderator M,



where, in analogy with proton charge exchange studies [27], σ_{10} is the cross section for electron capture (forming the muonium atom) and σ_{01} is the cross section for electron loss [17,20]. There are about 80 of these charge exchange cycles as the incident muon loses about 30 keV of energy, ultimately emerging with an energy of ~ 30 eV depending on the specific values of the cross sections σ_{10} and σ_{01} near the end of the charge exchange region. At these energies, the muon will either be bound in the paramagnetic muonium atom or still be free in the gas. These species then thermalize via elastic and inelastic scattering processes with the moderator gas and it is during this last stage of energy loss that hot atom or hot ion reactions are likely, placing the muon in a diamagnetic environment (e.g., as a molecular ion). The total slowing-down time in a gas like Ne or Ar is ~ 30 ns at 1 atm. pressure [17,20]. Much later, with a mean life $\tau_\mu = 2.2 \mu\text{s}$, the muon decays emitting a positron preferentially along its spin direction ($\mu^+ \rightarrow e^+ \nu_e \bar{\nu}_\mu$). It is this decay positron which is detected in the experiments.

The basic experimental technique has been described in detail elsewhere [17, 20, 21] and only its salient features will be mentioned here. The muon beam was stopped in a gas target containing 99.99% pure Ne at pressures near 1 atm to which trace amounts (~100 ppm) of Xe, He, NH₃ or CH₄ were added. The concentrations of these reactant gases were determined by dilution, having first measured their pressures in a small standard volume (~10 cc), and then sweeping them into the much larger target vessel (~30 l) with moderator gas. This target vessel was placed in the centre of a Helmholtz coil arrangement which provided a magnetic field transverse to the muon spin in the range ~1 G to ~300 G. In a diamagnetic environment the muon spin precesses essentially as a free muon (chemical shifts in a μ SR experiment are on the order of 10 ppm [28], too small to be measured with standard techniques) with a gyromagnetic ratio $\gamma_{\mu} = 13.55 \text{ kHz G}^{-1}$, whereas paramagnetic Mu precesses essentially as an S=1 electron, with $\gamma_{\text{Mu}} = 1.39 \text{ MHz G}^{-1}$. In a given magnetic field then, Mu precession is 103 times faster than diamagnetic muon precession so that these different magnetic environments can easily be distinguished; in practice, experiments are usually conducted in a field of about 8 G for the observation of Mu precession and in >100 G field for the observation of diamagnetic muon precession. In this article we report on measurements of muon precession in diamagnetic environment only. Since decay positrons are emitted preferentially along the muon spin direction, a counter telescope fixed in the plane of precession registers events with maximum probability each time the muon spin sweeps past, giving rise to a μ SR "signal", S(t). In practice, two separate counter telescopes were utilized, giving independent sets of data in both "Top" and "Bottom" histograms. Examples are shown in fig. 1 (a typical result from the top set of counters) for diamagnetic muon precession in pure Ne at 1300 torr pressure in a field of 288 G and in fig. 2 for the same Ne doped with 0.26 torr (200 ppm) of Xe.

Data of the type seen in fig. 1 can be fit to a single exponential (λ_1) in the usual manner [17, 20], but in the case of fig. 2 it is clear that there is a second component present which necessitates a fit to a more general form of the μ SR signal S(t), given by

$$S(t) = A_1 e^{-\lambda_1 t} \cos(\omega t + \phi) + A_2 e^{-\lambda_2 t} \cos(\omega t + \phi) . \quad (2)$$

where A_1 , λ_1 and A_2 , λ_2 are the amplitudes and relaxations for both components and ω , ϕ are the corresponding Larmor frequencies ($\omega = 2\pi\nu$) and initial phases (actually found to be the same for both components), respectively. The solid lines shown in figs. 1 and 2 are χ^2 fits to the data. It is important to note that there can be only one muon in the system at a time and hence there can be no possibility of any muon-muon interactions giving rise to spin relaxation.

3. Results

It can be seen in fig. 1 that there is a very slight relaxation ($\lambda_1 = 0.024 \pm 0.002 \mu s^{-1}$) of the muon signal in pure Ne but, as in ref. [17], this is probably still dominated by field inhomogeneity effects. The Helmholtz coils have been designed to give a homogeneity of 0.01% over the large muon stopping region but the harsh magnetic environment at the end of the beam line reduced this to about 0.1%. We are currently trying to improve this situation. While it has not yet been possible then to measure intrinsic muon relaxation in pure gases, we are able to examine the effect of trace amounts of added reactants (X) as manifest in an increased relaxation rate relative to the background value λ_0 seen in the absence of reactant. Results have been obtained for Xe and CH_4 added to Ne at 1300 torr and 1500 torr total pressures, for Xe added to Ne at 900 torr and also for Xe/He mixtures added to Ne at 1300 torr total pressure. Reference is also made to earlier data [17] obtained for pure He and for NH_3 added to Ne. Representative results of the fits of eq. (2) to the present data obtained by adding Xe and Xe/He to Ne at 1300 torr total pressure are given in table 1. The effect of added Xe is dramatically illustrated by the comparison of figs. 1 and 2. There are, as noted above, two relaxations apparent in fig. 2, a slow relaxation ($\lambda_1 = 0.035 \pm 0.008 \mu s^{-1}$) and a much faster one ($\lambda_2 = 2.80 \pm 0.24 \mu s^{-1}$). Similar results were obtained at different Xe concentrations. These data represent the first observation of two markedly distinct diamagnetic muon relaxation rates in a gas sample. Although the value of λ_1 is admittedly near the lower limit of detectability, it is larger than that seen in

pure Ne (fig. 1) and moreover exhibits a trend with increasing Xe concentration (fig. 3).

There is an additional effect apparent in comparing figs. 1 and 2, namely in the initial amplitude of the μ SR signal. Upon the addition of 200 ppm Xe, the initial amplitude ($A_1 + A_2$) is reduced by almost a factor of three (table 1). This is due to epithermal Mu formation in the charge exchange process $\mu^+ + \text{Xe} \rightarrow \text{Mu} + \text{Xe}^+$, as discussed in detail in ref. [20]. The observed diamagnetic amplitude decreases with increasing Xe concentration becoming asymptotic to zero (after $\sim 10\%$ corrections for muon stops in the walls of the target vessel) at concentrations ~ 400 ppm, corresponding to the 100% Mu fraction seen in the pure gas [20]. Very similar results were seen with added CH_4 and NH_3 although in these cases the diamagnetic amplitudes were asymptotic to $\sim 10\%$ of their maximum values corresponding again to the same fractions observed in pure gases. It should be emphasized that the relaxations λ_1 and λ_2 are due to thermal processes since these occur on time scales much longer than the thermalization time of ~ 30 ns.

Averaged results of the relaxations found in top and bottom histograms (table 1) are plotted as a function of Xe concentration for both λ_1 and λ_2 in figs. 3 and 4, respectively. As in muonium reaction studies [19, 21], these data can be described by the straight line

$$\lambda = \lambda_0 + k [X] \quad (3)$$

where λ_0 is the background relaxation referred to above, $[X]$ is the concentration of the added reactant and k is the bimolecular rate constant. The fit to the slow relaxation data in fig. 3 gives $k_1 = (1.8 \pm 0.4) \times 10^{-12}$ cc atom $^{-1}$ s $^{-1}$ while the fast relaxation data in fig. 4 gives $k_2 = (3.0 \pm 0.3) \times 10^{-10}$ cc atom $^{-1}$ s $^{-1}$ for the solid line fit shown. Similar experiments were carried out for CH_4 added to Ne but in this case only a single very slow relaxation essentially consistent with zero was observed ($k_1 \sim (0.5 \pm 0.3) \times 10^{-12}$ cc molec $^{-1}$ s $^{-1}$). Similarly, in our earlier study of NH_3 added to Ne [17] only a single slow relaxation was seen; these data are given in fig. 5 ($k_1 = (5 \pm 2) \times 10^{-12}$ cc molec $^{-1}$ s $^{-1}$). It is to be noted in fig. 3 that the value of λ_0 is the same as

in pure Ne ($\lambda_0 = 0.024 \pm 0.002 \mu\text{s}^{-1}$) while in fig. 4 it is a factor of about 30 larger when taken as the intercept consistent with the best straight line fit ($\chi^2 = 1.4$). If the fit (dashed line) is forced to include the pure Ne value for λ_0 (which seems physically correct) we find $k_2 = (4.2 \pm 0.3) \times 10^{-10} \text{ cc atom s}^{-1}$ but at the expense of essentially having to ignore the first data point and with a considerably worse fit ($\chi^2 = 6.6$). This could mean that there has been an error in determining the concentration of this first point or possibly that there is an additional much faster component present in the data. We prefer to quote at this time an average of the above two values (with an expanded error) giving $k_2 = (3.6 \pm 0.6) \times 10^{-10} \text{ cc atom}^{-1} \text{ s}^{-1}$ for the fast relaxing component of fig. 2, pending a series of further experiments at lower Xe concentrations over a range of different total pressures.

The present relaxation data for Xe and CH_4 differ considerably though from that reported in an earlier study [17,18]. As noted above, the apparatus used then gave a considerably less homogeneous and also lower magnitude ($\sim 70 \text{ G}$) magnetic field. The lower field in particular rendered the observation of very fast diamagnetic muon relaxation rates (as in fig. 4) virtually impossible. Nevertheless, despite the difficulties in that earlier study we can be confident of certain trends in comparison with the present data; in particular, the absence of any fast muon relaxation in the case of NH_3 added to Ne (fig. 5). A summary of rate constants found from the muon relaxation data in Xe, CH_4 and NH_3 doped Ne is given in table 2.

4. Discussion

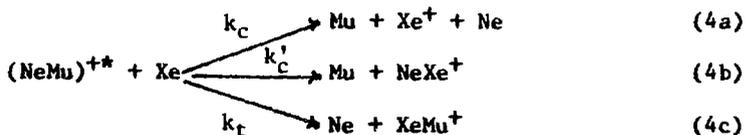
There are two quantities relevant to an understanding of these data: the proton affinity (PA) and ionization potential (IP) of the reactant X in comparison with the IP of Mu itself (13.6 eV). These values are compared in table 3. Consider now the consequences of the collision of a free muon at thermal energies with any of the reactants of table 3. Muonium must form since the energy defect for the charge exchange process $\mu^+ + X \rightarrow \text{Mu} + X^+$ is exothermic ($\Delta E < 0$) in every case. Although such

charge exchange processes are not "resonant" in the sense of $\Delta E = 0$, we still expect 100% thermal Mu formation for $X = \text{Xe}$, CH_4 , or NH_3 , consistent with the extrapolation of large proton charge exchange cross sections to the thermal energy regime for these cases [20,27]. Moreover, the polarizabilities of Xe, NH_3 and CH_4 are all large [29] and the (Langevin) rates for the collision process $\mu^+ + X$ for a free muon are all expected to be $\sim 10^{-8} \text{ cc atom}^{-1} \text{ s}^{-1}$; hence the probability of thermal Mu formation should be very similar for all three reactants. Muonium precesses in the (288 G) magnetic field 103 times faster than the free muon, and thus thermal Mu formation will lead to loss of phase coherence in the observed μSR signal and hence a relaxation of this signal. The fact that a fast relaxation is seen only for the case of Xe in Ne establishes that the muon cannot be free in the gas but must be bound in a diamagnetic environment, most likely as the NeMu^+ molecular ion. Other diamagnetic species are possible, XMu^+ with reactant X and in the case of the molecular reactants, molecules like MuCH_3 may be formed as a consequence of hot atom reactions. However, these possibilities are regarded as extremely unlikely in view of the much higher chance of collisions with the Ne moderator ($\sim 10^4$) during the thermalization processes of the muon in the gas. Moreover, in the pure gases, no diamagnetic signal is seen in Xe and in the cases of CH_4 and NH_3 hot atom reactions clearly have low probabilities [20].

4.1 Reactivity of the NeMu^+ ion

The binding energy of the μ^+ in NeMu^+ (and in HeMu^+) can be estimated from the known values for NeH^+ and HeH^+ [10] using a simple harmonic zero point mass correction [17]. However, accurate values have been calculated in ref. [16] and these are given in table 4 along with the corresponding values for the hydride ions. Note the enormous isotope effect of the much lighter mass muon ($m_\mu = 1/9 m_p$). This has the consequence that the rovibrational level density in NeMu^+ (HeMu^+) is about an order of magnitude less than in their protonic analogs.

The two-component relaxation seen for Xe in Ne in fig. 2 can be understood in terms of the following reaction scheme,



where $k_c(k'_c)$ and k_t are meant to denote bimolecular rate constants for charge exchange and muon transfer processes, respectively. The difference between channels (4a) and (4b) is in the formation, or not, of a bound NeXe^+ complex. Such complexes are expected to have binding energies ~ 1 eV [30] and a two-body final state is perhaps more likely from the point of view of available phase space. Although we could not distinguish (4a) from (4b), the production of muonium by either channel (or both) results in the immediate loss of phase coherence as the muon is transferred from the diamagnetic molecular ion environment to paramagnetic muonium. As such it provides a ready explanation for the very fast relaxation seen upon $\text{NeMu}^+ + \text{Xe}$ collisions (fig. 2) with the corresponding rate constant k_2 (fig. 4) being identified with either k_c or k'_c or their sum. On the other hand, reaction (4c), the muon analog of a proton transfer reaction, is the precursor for the observed slow relaxation component of fig. 2. One would indeed not expect this latter process to give rise to any appreciable relaxation of the μSR signal because the muon again finds itself in a diamagnetic environment. Thus, μSR does not provide a direct observation of the process corresponding to k_t . However, table 1 shows the amplitudes A_1 and A_2 to be comparable, indicating that the branching ratio of reactions (4a) and/or (4b) and (4c) is about 0.5, from which it may be inferred that $k_t \approx (k_c + k'_c)$. Indeed, it is frequently the case that charge transfer and proton transfer proceed with comparable rates at low energies [31]. On the other hand, as noted already, there is a discernable trend to increasing λ_1 with increasing Xe concentration in fig. 3, giving rate constant k_1 . This relaxation could conceivably be due to a spin rotation interaction of $\text{XeMu}^+ - \text{Xe}$ collision complexes, in analogy with NMR studies in other rare gas systems [32]. It must be understood that $k_1 \neq k_t$; k_t corresponds to the relatively fast but not directly observable muon transfer reaction (4c), whereas k_1 corresponds to the subsequent slow relaxation of the XeMu^+ molecular ion which is only just observable. In order to be able to make more

definitive statements of the meaning of k_1 , we will have to improve the effective homogeneity of our apparatus by something like a factor of ten.

From the values in tables 3 and 4 it can be seen that reaction (4a) from the ground state of the NeMu^+ ion is endothermic by 0.4 eV (the corresponding HeMu^+ would be endothermic by 0.1 eV). Hence, any observed fast relaxation in collisions with Xe due to this reaction must be due to NeMu^+ in an excited state (as denoted by the *), with an excitation energy > 0.4 eV (it is unlikely that electronically excited Xe^* would play any role). On the other hand, reaction (4b) would be exothermic even from the ground state by ~ 0.6 eV, depending on the binding energy of the NeXe^+ ion [30]. Regardless of the nature of the final state in (4a) or (4b) it seems likely that NeMu^+ would form in a long-lived ($\tau > \tau_\mu = 2.2 \mu\text{s}$) excited state. This is typical of a variety of formation processes of rare gas hydrides [5-7,31]. From the calculations of ref. [16] there are a large number of bound states which satisfy this requirement as well as a long-lived $v=0$ $J=1$ quasibound state ($\tau = 4.2 \times 10^{-6}$ s). The radiative lifetime of the bound states are all expected to be much longer than the muon lifetime, of order 100 μs in both HeMu^+ and in NeMu^+ , based on the calculations of ref. [13], [14] and [16] and on the measured values of refs. [5] and [6].

Corroborating evidence for the formation and reactivity of $(\text{NeMu}^+)^*$ in an excited state was obtained by adding trace amounts of He to the Ne/Xe reaction mixture, illustrated by the μSR signal in fig. 6. This was obtained at 1300 torr Ne total pressure with added Xe and He at 200 ppm and 100 ppm, respectively. In comparison with fig. 2, one notes a dramatic decrease in the amplitude of the fast component. The relaxations, however, are essentially (within 2 standard deviations) unchanged. Similar effects were seen in a 35 ppm Xe/Ne mixture to which 17 ppm He was added. Results for the corresponding amplitudes are given in table 1. These particular mixtures were chosen to reflect essentially equal rates for $\text{NeMu}^+ - \text{Xe}$ and $\text{NeMu}^+ - \text{He}$ collisions. The results are understandable in terms of efficient vibrational-translational (V-T) energy transfer in a competition between $\text{NeMu}^+ - \text{Xe}$ and $(\text{NeMu}^+)^* - \text{He}$ collisions, placing the

(NeMu⁺)^{*} in a non-relaxing state at a lower excitation energy. Such processes are known in general to be very efficient for small light atoms [1,33], particularly for He atoms; the simplistic explanation in the present case being that the velocity of the faster-moving He atom is better matched to the vibrational period of the molecular ion than is the Ne atom. Indeed, in ref. [17], it was found that even in the case of Xe added to He itself there was essentially zero diamagnetic muon relaxation, in marked contrast to Ne (fig. 2), which can again be understood in terms of an efficient V-T energy transfer, in this case of (HeMu⁺)^{*}-He collisions.

The experimentally averaged thermal rate constant $k_2 = (3.6 \pm 0.6) \times 10^{-10} \text{ cc atom}^{-1} \text{ s}^{-1}$ for the process $(\text{NeMu})^{+*} + \text{Xe} \rightarrow \text{Mu} + \text{Xe}^+$ (fig. 4) is about a factor of three lower than the classical Langevin rate, k_L (table 2). It is well known though that the Langevin limit is for a particularly simple type of ion-molecule interaction (induced dipole) and there can be many additional factors involved, affecting even the classical reaction rate [1, 2, 34]. Moreover, the overall reaction rate reflects the particular topology of a given reaction channel and can generally be expected to be different (usually smaller) than the maximum encounter rate. Indeed the present result of $k_L/k_2 \sim 3$ for reaction (4a) and/or (4b) is not atypical of a wide variety of thermal ion molecule reactions in that experimentally determined rate constants agree with the calculated Langevin values to within a factor of 2 or 3 [2-4, 7, 35]; in most cases, in fact, k_L gives the maximum thermal rate constant found experimentally.

The most surprising result emerging from the present experiments is the lack of any fast relaxation seen for NeMu⁺ in the presence of either X=CH₄ or NH₃ (fig. 5). In the case of the analog of (4a), reaction with CH₄ is endothermic by 0.8 eV but with NH₃ it is exoergic even from the g.s. of (NeMu)⁺; the analogs of (4b) would presumably be exoergic from the (NeMu)⁺_{g.s.} in both cases (if the products are indeed formed). At this point it is worth recalling that observation of the collision process $(\text{NeMu})^{+*} + \text{X}$ is possible only if it results in Mu formation ($k_2 = k_c + k_c'$); the competitive channel (k_t) forming the XMu⁺ molecular ion (4c) leads to a very small relaxation (with Xe). In fact, for both X = CH₄ and NH₃,

the measured rate constant corresponding to this slow relaxation is effectively consistent with zero, particularly in the case of CH_4 (table 2). The fact that there is no fast component seen for both $\text{X}=\text{C}_2\text{H}_2$ and NH_3 is a strong indication of the existence of very fast muon transfer reactions. In order for us not to be able to observe the expected Mu formation channel, μ^+ transfer from NeMu^+ to CH_4 (or NH_3) must occur on a time scale < 100 ns at the lowest concentrations. This corresponds to a bimolecular rate constant $k > 7 \times 10^{-9}$ cc molec $^{-1}$ s $^{-1}$, which is at least a factor of 5 faster than the Langevin rate, k_L (table 2); the corresponding cross section would be of order 100 \AA^2 .

Classically, a trend to increased muon transfer in the order $\text{X}=\text{NH}_3 > \text{CH}_4 > \text{Xe}$ is expected on the basis of the proton affinities given in table 3 (the corresponding muon affinities can be expected to show the same trends); i.e., in the direction of increasing exothermicity, in analogy with proton transfer reactions [3,4,7], particularly from rare gas hydride ions. However, the dramatic dichotomy seen in the present study between $\text{X}=\text{Xe}$ on the one hand and $\text{X}=\text{CH}_4$ and NH_3 on the other cannot be explained on this basis. Although polyatomic molecules generally have larger PA's and hence tend to exhibit faster ion-molecule reaction rates than diatomics or atoms do, these are still rarely faster than the Langevin rates [4,7]. It is to be noted though that molecular quadrupole moments and even intrinsic dipole moments can have important effects on the classical charge-induced dipole interaction [36,37], the NH_3 molecule itself being a case in point. Even in these cases, though variational theories can yield upper bounds for rate constants well in excess of the Langevin ones [36], the best agreement with experiment in the thermal energy regime is again within a factor of two of the simple Langevin rate. To our knowledge there is no precedent for a proton (muon) transfer reaction in the gas phase at thermal energies which is $> 5 \times$ faster than the Langevin rate (protonation reactions in liquid media, particularly the Gertenhaus mechanism in water, can be regarded as special cases of intra molecular proton transfer reactions which are known to be very fast in certain systems [38]). All of the above-mentioned calculations are classical in origin and the fact that we see such an enhanced transfer rate in the case of the positive muon may indicate a significant effect

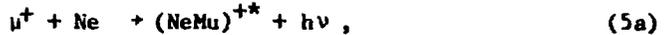
of muon tunneling in the $\text{NeMu}^+ + \text{CH}_4$ (NH_3) collision process. The utility of the light muon mass as a probe of quantum tunneling in muonium reactivity is well established [19,24] but the above processes may represent the first time that similar effects have been characterized in muon transfer reactions.

There are a number of other possible explanations that should also be considered, all of which seem less likely to us though than a fast muon transfer reaction. Vibrational excitation and curve crossing (surface hopping) phenomena can have dramatic effects on both charge exchange and proton transfer reactions at different kinetic energies [31], particularly vibrational excitation at low (thermal) energies, promoting resonant ($\Delta E=0$) charge transfer. By contrast, vibrational excitation is expected to have relatively little effect on proton (muon) transfer at these energies. As alluded to above, highly rovibrational excited states of $(\text{NeMu})^{+\ast}$ [16] may well facilitate resonant charge transfer in the $(\text{NeMu})^{+\ast} + \text{X}$ collision process, regardless of whether a Ne molecular ion bound state is again formed in the product channel (4b) or not. Perhaps there is a very efficient V-T (or V-V) energy transfer in the case of collisions of both NH_3 and CH_3 with $(\text{NeMu})^{+\ast}$, as is known to be the case for several small molecules in other reactive systems [39]. If this were true, however, the corresponding cross sections would have to be considerably larger than those in $(\text{NeMu})^{+\ast}\text{-He}$ collisions since we still observe a fast relaxation (with reduced amplitude) in $(\text{NeMu})^{+\ast}/\text{Xe}/\text{He}$ mixtures, as discussed already (fig. 6). Such large cross sections seem unlikely in view of the previously mentioned efficiency for He in promoting V-T relaxation [33] (although V-V transfer is of course not possible in collisions with He). It is also conceivable that radiation damage effects initiated by fragmentation reactions of energetic charged particle beams in molecular gases [40] could sufficiently affect the environment of the muon that thermal Mu formation in subsequent collisions (e.g., with radiation produced H_2) would no longer be possible. However, in view of the intensity of our ~ 3 MeV beam ($<10^5 \mu^+$ per second) such a process would seem to be extremely unlikely. Finally, if the muon were bound in a diamagnetic chemical bond as a result of hot atom reactions during its slow-

ing-down process forming, e.g., MuCH_3 (or MuNH_2), subsequent collisions with CH_4 (or NH_3) at thermal energies would not effect any change in the muon polarization, except possibly on the very slow time scale of NMR relaxation times seen in similar systems [32,41]. Again though, as noted earlier, such a process is regarded as very unlikely in the present study where only ~ 100 ppm amounts of CH_4 (or NH_3) have been added to Ne moderator, compared to earlier studies in the pure molecular gases where $\sim 90\%$ of incident muons thermalize as paramagnetic muonium [20].

4.2 Formation of the NeMu^+ ion

The mechanism of the formation of NeMu^+ (and other rare gas "muides") is not clear at this time but it seems that there are basically only two possibilities,



These reactions are only likely to occur with appreciable probabilities well after the charge exchange regime, in the energy range from ~ 20 eV to $k_B T$ [20]. In the case of reaction (5a), which might involve a termolecular encounter, the relative energy must be low enough to allow sufficient time for reaction to occur. In particular, recent studies of orbiting resonances in the He-H^+ system [12] suggest that HeMu^+ (and hence probably also NeMu^+) would form with appreciable cross section only at kinetic energies < 0.5 eV. Larger molecular complexes of the rare gas hydrides are also well known [15], but their formation is regarded as extremely unlikely in the present context (similar complexes formed in negative muon capture [42] proceed by a totally different mechanism). Consideration of the energetics for $\text{Mu} + \text{Ne}$ and $\text{Mu} + \text{Ne}^+$ (and similarly for He) indicate further that reaction (5b) is only likely to occur if the Ne(He) atom has been placed in an excited state by collision with the Mu atom, notably in a metastable S state. In this case, the reaction scheme depicted below is expected to occur at low (~ 20 eV) incident Mu energies,



Further experiments, particularly on the pressure dependence of the

signal amplitudes in Ne/Xe mixtures (so that both a paramagnetic μ and diamagnetic muon fraction can be seen) are required. It may even be possible in future experiments to detect the optical transition from the $\text{Ne}^*(3S)$ state, using single photon uv detectors.

5. Concluding remarks

Further work is in progress, including a study of both the temperature and pressure dependence of the reactivity with Xe, CH_4 , and NH_3 , in helium, neon and argon moderators. Experiments in both pure and mixed molecular gases are also planned with improved field homogeneity in order to properly compare NMR [31,41] and μSR relaxation phenomena. Here it is the slow time scale that is of interest (cf. fig. 3) and since proton relaxations in gases are proportional to γ_p^2 (or γ_p^4 for certain spin rotation interactions), there should be a large enhancement seen if a proton is replaced by a positive muon ($\gamma_\mu/\gamma_p = 3.18$). As such, the study of slow μSR relaxation phenomena in gases is capable of providing valuable further tests of the basic theory of NMR relaxation.

It is hoped that the present results will stimulate some theoretical calculations of ion-molecule reactions involving the positive muon; in particular, whether the proposed mechanism of significant muon tunneling is correct or not. These reactions may be very suitable as an example of H-L-H (heavy-light-heavy) systems which are currently being studied via hyper-spherical and Delve's coordinate transformations [43]. It would also be of considerable interest to have some theoretical guidance on the formation process of $\text{Ne}\mu^+$ and indeed on the formation of positive muon molecular ions in general.

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**TABLE 1: The Amplitudes (A) and Relaxations (λ) of the μ SR Signals
Seen Upon the Addition of Trace Xe and He to Ne, 1300 Torr**

<u>[Xe]^{a)}</u>	<u>[He]^{a)}</u>	<u>A₁^{b),c)}</u>	<u>λ_1 (μs⁻¹)^{b)}</u>	<u>A₂^{b)}</u>	<u>λ_2 (μs⁻¹)^{b)}</u>
0.0	0.0	.316 \pm .002	.023 \pm .002		
1.4 \pm 0.1(33)	0.0	.109 \pm .005	.030 \pm .01	.147 \pm .006	1.24 \pm .07
5.7 \pm 0.1(135)	0.0	.049 \pm .003	.030 \pm .006	.121 \pm .004	2.63 \pm .17
8.5 \pm 0.2(200)	0.0	.041 \pm .002	.041 \pm .006	.081 \pm .004	3.28 \pm .27
11.4 \pm 0.2(268)	0.0	.038 \pm .002	.043 \pm .006	.045 \pm .004	4.34 \pm .76
1.4 \pm 0.1(33)	0.7 \pm 0.1(17)	.124 \pm .005	.028 \pm .01	.109 \pm .006	1.80 \pm .20
8.5 \pm 0.2(200)	4.3 \pm 0.1(100)	.032 \pm .003	.038 \pm .008	.035 \pm .008	4.9 \pm 2.5

a) The concentration of added Xe or He in units of 10¹⁵ atoms cc⁻¹, calculated from measured volumes and assuming the validity of the ideal gas law. values in ppm given in parenthesis.

b) Obtained from the results of the fits of eq.(1) to the data, reported in most cases as a weighted average of results from both the Top and Bottom histograms.

c) The amplitude of the slowly relaxing signal has been corrected for muons scattered into the walls of the target vessel. See discussion in ref. [20].

**TABLE 2: Rate Constants k for the Reactions
(NeMu)^{+*} + X, for X = Xe, CH₄ or NH₃**

<u>Reactant, X</u>	<u>k_{exp} (10⁻¹⁰ cc atom⁻¹ s⁻¹)^{a)}</u>	<u>k_L (10⁻¹⁰ cc atom⁻¹ s⁻¹)^{b)}</u>
Xe	k ₂ = (3.6 \pm 0.6) c) k ₁ = (.018 \pm .004)	11.0
CH ₄	k ₁ = (.005 \pm .003) d)	12.5
NH ₃	k ₁ = (.05 \pm .02) e)	13.3

a) Experimentally determined rate constant.

b) Classical Langevin rate constant.

c) An average of the two fits shown in fig. 4, as discussed in the text.

d) Consistent with zero.

e) From fig. 5 (taken from ref. [17]).

TABLE 3: A Comparison of Ionization Potentials and Proton Affinities for Different Reactants

<u>Reactant(X)</u>	<u>I.P.(eV)^{a)}</u>	<u>ΔE(eV)^{b)}</u>	<u>P.A.(eV)^{c)}</u>
Xe	12.2	1.4	5.1
CH ₄	12.6	1.0	5.9
NH ₃	10.8	2.8	8.9

- a) Taken from the Handbook of Chemistry and Physics, 57th ed., 1976.
 b) Exothermicity for the charge exchange process, $\mu^+ + X \rightarrow \mu + X^+$
 c) Proton Affinity, from the data of Bohme et al., ref. [4]

TABLE 4: Dissociation Energies (eV) for the First Two Vibrational ($v=0,1; J=0$) levels of NeMu⁺ and NeMu⁺

<u>Ion</u>	<u>D_e</u>	<u>D₀</u>	<u>D₁</u>
HeH ⁺ a)	2.037	1.842	1.482
HeMu ⁺ b)	2.037	1.532	0.734
NeH ⁺ c)	2.265	2.085	1.76
NeMu ⁺ b)	2.265	1.786	0.975

- a) From ref. [13].
 b) From ref. [16].
 c) From refs. [9] and [11].

Figure Captions

1. The μ SR signal in pure Ne at 288 G and 1300 torr pressure. The solid line is a χ^2 fit to the data assuming a single relaxation.
2. The μ SR signal at 288 G in Ne at 1300 torr with 200 ppm of added Xe. The solid line is a χ^2 fit to the data assuming two different relaxations, giving λ_1 (slow) = $0.035 \pm 0.008 \mu\text{s}^{-1}$ and λ_2 (fast) = $2.80 \pm 0.24 \mu\text{s}^{-1}$.
3. A plot of the observed relaxation λ_1 (slow) for Ne/Xe mixtures as a function of Xe concentration at 1300 torr total pressure. The points are an average of fits obtained from "Top" and "Bottom" histograms. The solid line is the best straight line fit to the data.
4. A plot of the observed relaxations λ_2 (fast) for Ne/Xe mixtures as a function of Xe concentration. The solid line is the best straight line fit ignoring the " λ_0 " value for pure Ne while the dashed line is the best fit including this value. The squares represent fits to the fast relaxation at 1300 torr pressure while the diamonds were obtained at 1500 torr total pressure. Additional points obtained at 900 torr pressure agree within errors and are not shown.
5. A plot of the relaxation of the μ SR signal seen in Ne/NH₃ mixtures at 930 torr and 70 G as a function of NH₃ concentration, assuming a single relaxation. The solid line is the best straight line fit to the data (taken from ref. [17]).
6. As in fig. 2 but with an additional 100 ppm of added He. Note the change in amplitude of the early time (fast) signal in comparison with fig. 2.

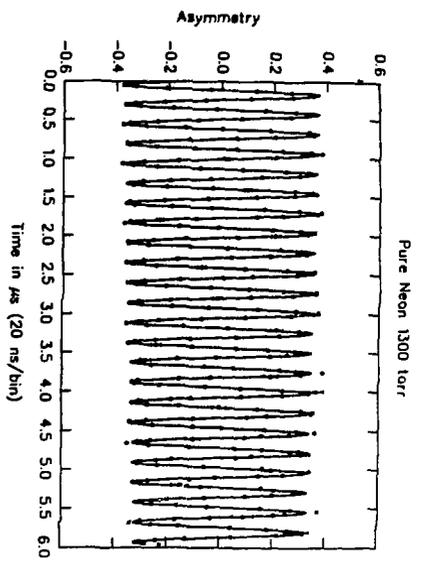


Fig. 1

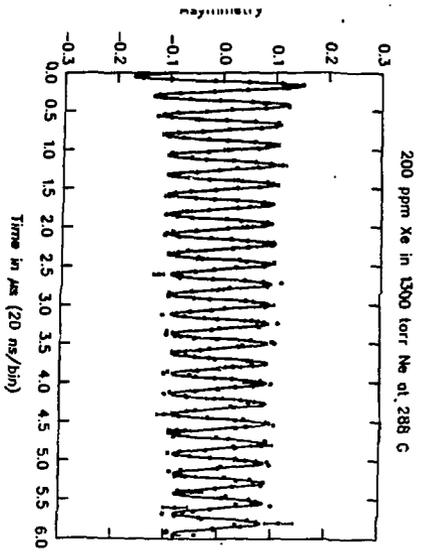


Fig. 2

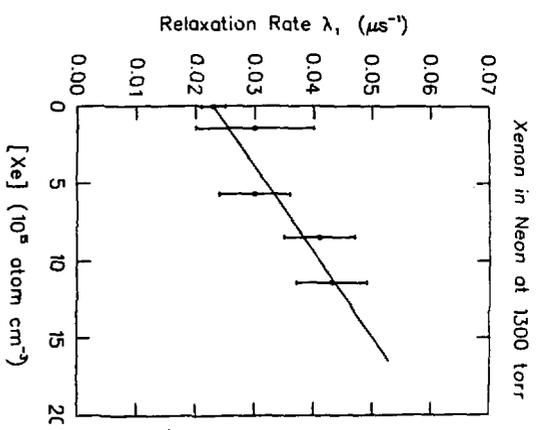


Fig. 3

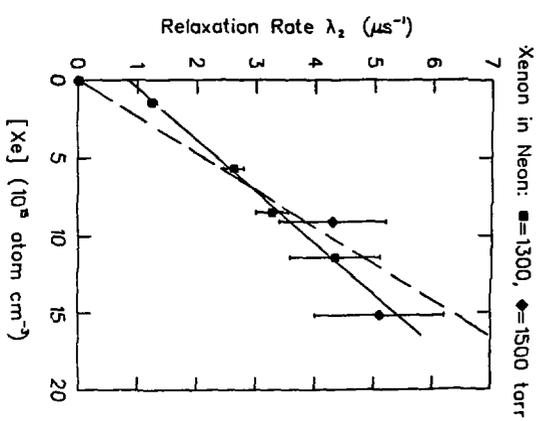


Fig. 4

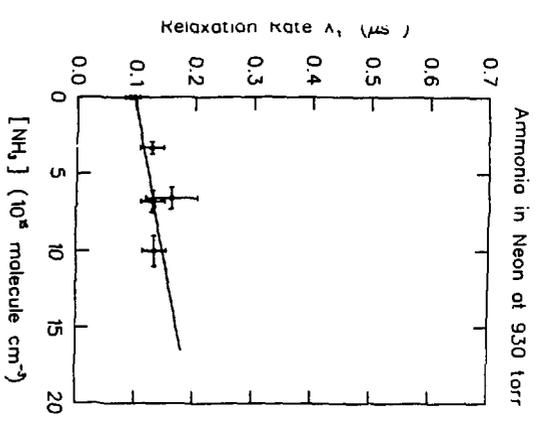


Fig. 5

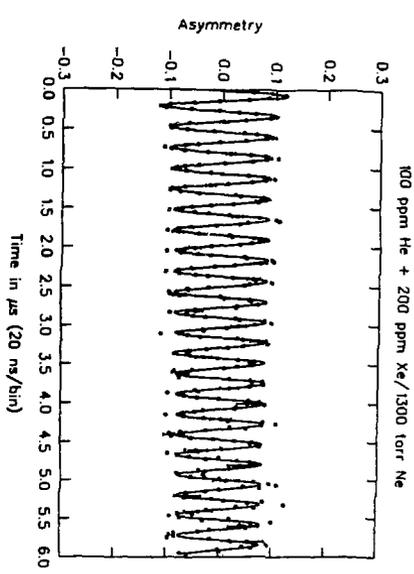


Fig. 6