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INTERNAL FRICTION DUE TO DOMAIN-WALL MOTION  
IN MARTENSITICALLY TRANSFORMED A15 COMPOUNDS

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## Resume -

Abstract - A lattice instability in Al5 materials in some cases leads to a cubic-to-tetragonal martensitic transformation at low temperatures. The transformed material orients in lamellae with c axes alternately aligned along the  $\langle 100 \rangle$  directions producing domain walls between the lamellae. An internal-friction ( $\delta$ ) feature below  $T_m$  is attributed to stress-induced domain-wall motion. The magnitude of the friction increases as temperature is lowered below  $T_m$  as  $(1-c/a)$  increases, and behaves as  $(1-c/a)^2$  from  $T_m$  down to the superconducting critical temperature where the increasing tetragonality is inhibited. The effect of strain in the lattice is to decrease the domain-wall internal friction, but not affect  $T_m$ . Neutron-induced disorder and the addition of some third-elements in alloying decrease both  $\delta$  and  $T_m$ , with some elements reducing only the former. Less than 1 at. % H is seen to completely suppress both  $\delta$  and  $T_m$ . Martensitically transformed  $V_2Zr$  demonstrates low-temperature internal-friction and modulus behavior consistent with easy  $\beta/m$  wall motion relative to the easy  $m/m$  motion of the Al5's. For the  $V_2Zr$ , a peak in  $\delta$  is observed, qualitatively in agreement with expected  $\beta/m$  wall motion.

## INTRODUCTION

Although there has been a very large amount of work expended on studies of martensitic transformations, the understanding of the microscopic mechanisms involved so far is quite poor. To quote Planes et al. /1/ "In fact, only certain transitions - those found in the Al5 compounds - can be explained in terms of microscopic properties of their constituents (it is believed that Al5 compounds undergo a band Jahn-Teller transition /2-4/." Even with that, the microscopic mechanism giving rise to internal friction associated with the transformation is not known. This paper reviews some of the data on internal friction due to martensitic transformations in Al5's, how various material treatments affect the friction, a "microscopic" theory to explain the friction, and how the data and the theory compare.

Some of the Al5 compounds undergo a cubic-to-tetragonal martensitic transformation. This transformation is at temperature  $T_m$  below liquid-nitrogen temperature and above the superconducting critical temperature  $T_c$ . As with many martensitic transformations, it is associated with a lattice instability (the instability of the  $\{110\} \langle 110 \rangle$  mode with decreasing temperature and the vanishing of the shear modulus  $(1/2)(C_{11}-C_{12})$  at  $T_m$  /5-6/. In  $Nb_3Sn$  the tetragonal-phase material is composed of twinned domains with c axes lying along  $\langle 100 \rangle$  directions, and with the habit plane of the twin boundary along (110). At  $T_m$ , the c axis is reduced and the a and b axes equally lengthened. The tetragonality of the material increases, however, as the temperature is lowered below  $T_m$  as c/a decreases with decreasing temperature down to  $T_c$  where further change in c/a is arrested /2/. For  $Nb_3Sn$  at  $T_c$ ,  $c/a = 0.9939$  with  $T_m$  at 43 K /7/. On the other hand,  $V_3Si$  has the c axis larger than the a and b axes and a c/a of 1.0022 with a  $T_m$  of 21 K /7/. Note that the "tetragonality"  $|(1-c/a)|$  of  $Nb_3Sn$  is roughly 3 times that of  $V_3Si$  at their respective  $T_c$ 's.

The Al5 superconductor  $Nb_3Sn$  is currently the prime material for the construction of magnets for applications such as confining magnets for fusion, and bending magnets for the Superconducting Supercollider. Since these applications require large stresses on the conductors, knowledge of the low-temperature modulus values and mechanical behavior is needed. The modulus data that are taken concomitantly with

the  $Q^{-1}$  data are, therefore, of scientific and engineering interest. As the transformation to the tetragonal phase is thought to be intimately coupled with both mechanical behavior and to the superconducting critical properties, these studies take an added interest.

Figure 1 shows the internal friction of  $Nb_3Sn$  from 10-400 K. Specimens were polycrystalline 10- $\mu m$  layers of  $Nb_3Sn$  sandwiching a 10- $\mu m$  Nb substrate and cut into foils. Standard electrostatic drive in flexure was used at frequencies between 100 and 2000 Hz. The high-temperature peaks will be discussed later. The feature of note is the 2.5 order of magnitude increase in  $Q^{-1}$  between  $T_m$  (here 49 K) and  $T_c$  (18.1 K). (Data were taken for temperature ramps in both direction and no hysteresis or time dependence of  $Q^{-1}$  was ever detected. All data are shown for increasing temperature.) It is this feature that provides the means of studying various chemical and mechanical effects on the martensitic transformation.

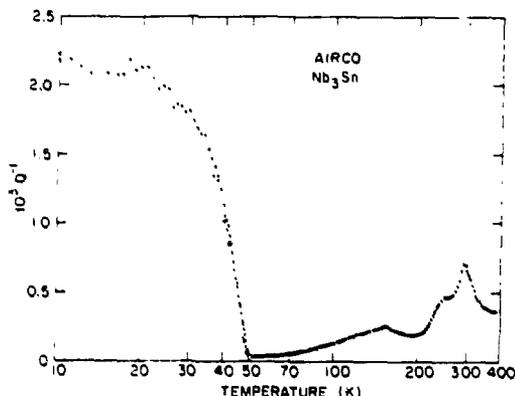


Fig. 1.  $Q^{-1}$  vs. temperature for "pure"  $Nb_3Sn$  foil.

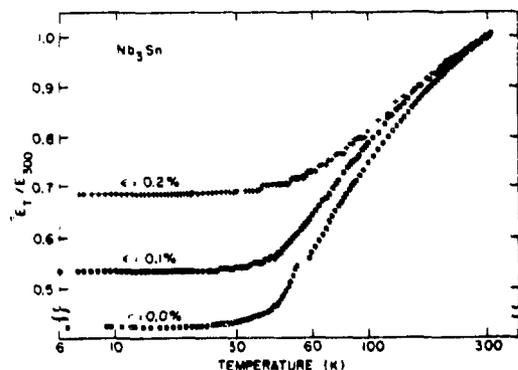


Fig. 2. Effect of internal strain in  $Nb_3Sn$  on the reduced modulus  $E(T)/E(300)$  as a function of temperature.

One of the first parameters investigated was the effect of strain on the transformation. Strain due to unrelieved deformation in the substrate was investigated as shown in the modulus measurements of Figure 2. Note that the modulus softens near  $T_m = 49$  K to a value of  $\sim 40\%$  of the room-temperature value in the strain-free specimen. This modulus softening reflects the instability of the  $\{110\}\langle 110 \rangle$  mode mentioned earlier. With increasing internal strain ( $\epsilon = 0.1$  and  $0.2\%$ ) the amount of softening is reduced significantly. Figure 3 shows the effects of this strain on the internal friction. The reduction in the friction with strain is considerable, but the main point to make is that even though the modulus and the internal friction are changed, the transformation temperature  $T_m$  is essentially unaltered, as is expected from a Landau-type theory of the transformation /8/.

The internal friction is attributed to the stress-induced motion of the martensitic/martensitic (m/m) domain walls with an attendant hysteretic loss. Microscopically, one envisions the reorientation of c axes from one  $\langle 100 \rangle$  orientation to the twin  $\langle 100 \rangle$  orientation as the twin boundary moves. In this way each atom (or unit cell) can be thought of as a "reorienting dipole". This interpretation is developed more fully in the Appendix. An important feature of that development is the prediction that the magnitude of the internal friction should vary as  $(c/a-1)^2$ . Two sets of "pure"  $Nb_3Sn$  data are fit with this expression with the data normalized at 18 K. There is one free parameter,  $T_m$ . Since  $c/a$  decreases with temperature, we use previously determined values /7/ in the fitting. The results are shown in Figure 4. The  $T_m$  value of 49 K, determined from the apparent highest-temperature of onset of the internal friction does not fit well. The value  $T_m = 44.5$  K was found to give the best fit. Note that is near the value of 43 K usually associated with

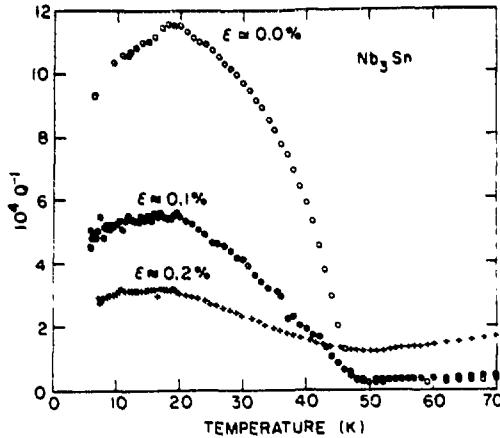


Fig. 3. Effect of strain on  $Q^{-1}$  as a function of temperature in  $Nb_3Sn$ .

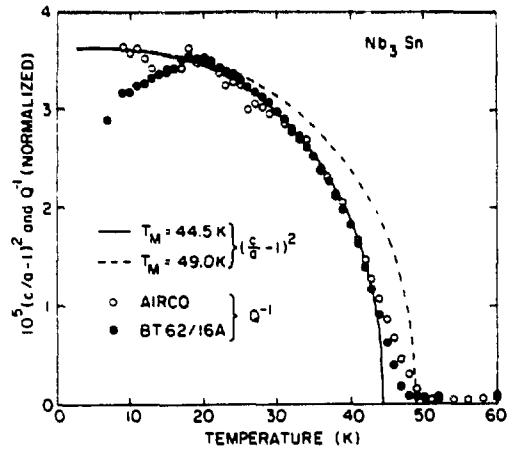


Fig. 4. Parametrized fit of  $Q^{-1} \alpha (c/a-1)^2$  for the low-temperature internal friction of two  $Nb_3Sn$  specimens.

this transformation from X-ray work [7]. The region 44-49 K would then seem to be a temperature range denoting onset (49 K) and completion (44 K) of the cubic-to-tetragonal transformation. Below 44 K, all changes in  $Q^{-1}$  are attributed to changes in  $c/a$ . We will see that this transformation region below  $T_m$  can be broadened by different treatments.

Al5 compounds with maximized critical properties are characterized as highly ordered compounds. The question has arisen of what the effects of disorder are on the compound's properties. Since these materials are envisioned to be used in radiation environments, for instance, the radiation-damage-induced disorder effects become of paramount importance. Figures 5 and 6 show the effects of 400 K reactor-spectrum neutron irradiation to  $Nb_3Sn$ . The primary defect produced affecting disorder from this irradiation is the antisite defect (A-B interchange in the  $A_3B$  compound) [9]. In Figure 5 there are three main things to note with regard to the disorder effects on the log decrement  $\delta$ . The first is the decrease in  $\delta$  with fluence. The second is the decrease in  $T_m$  with fluence. Recall that internal strain reduced  $\delta$  but did not affect  $T_m$  at all. It is then clear that disorder plays a very different role in changing the characteristics of the transformation, most probably through the

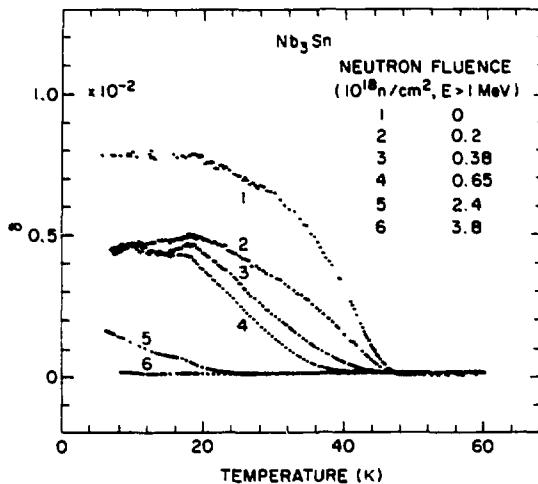


Fig. 5. Log decrement  $\delta$  vs. temperature of  $Nb_3Sn$  for several reactor-spectrum fluences.

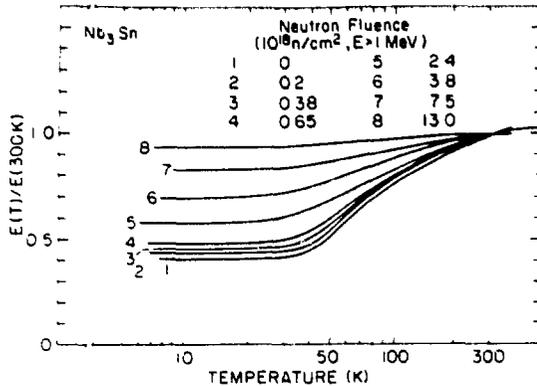


Fig. 6. Reduced modulus  $E(T)/E(300\text{ K})$  vs. temperature of  $\text{Nb}_3\text{Sn}$  for several reactor-spectrum fluences.

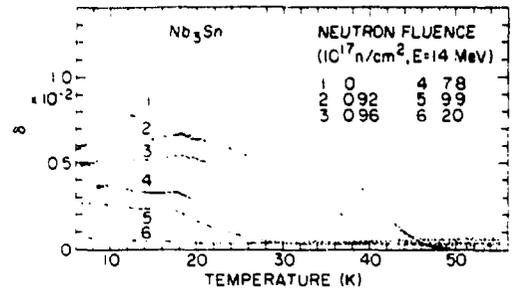


Fig. 7. Log decrement  $\delta$  vs. temperature of  $\text{Nb}_3\text{Sn}$  for several fluences of 14-MeV neutrons.

electronic properties of the material which to first approximation are not affected by stress.  $T_m$  is seen to decrease monotonically (still present in the curve marked 6 if the scale is expanded and located at  $\sim 21$  K). For fluences higher than  $3.8 \times 10^{18}$  n/cm $^2$ ,  $T_m$  would, by extrapolation, lie below  $T_c$ . Since  $c/a$  cannot change below  $T_c/2$ , the transformation cannot, therefore, take place. Thus, disorder induced by neutron irradiation can completely arrest the martensitic transformation.

In addition to a reduction of  $\delta$  and  $T_m$  with disorder, it is also noted from Figure 5 that as fluence (and disorder) increase, the shape of the  $\delta$  curve between onset at high temperature and  $T_c$  changes from convex-right to convex-left: in other words, the  $(1-c/a)^2$  dependence no longer holds. Indeed, the entire range for the  $0.65 \times 10^{18}$  n/cm $^2$  fluence takes on the character of the 44-49 K region of the unirradiated case. We think this is significant and that a fluctuation of disorder in the specimen creates the situation where a larger temperature range is spanned before the completion of transformation is realized. For curves 5 and 6 this temperature span clearly encompasses  $T_c$ .

The effect of increasing disorder on the mode softening and therefore the dynamic Young's modulus is shown in Figure 6. All the moduli are normalized to their respective values at 300 K. Softening of 60% for the "virgin" specimen is seen to decrease to only 6% for the  $13 \times 10^{18}$  n/cm $^2$  case. For the two highest fluences shown, there was no martensitic transformation. This significant increase in the low-temperature modulus in radiation environments could have important consequences in fusion applications. For the effect of pure 14-MeV neutrons on the transformation, Figure 7 shows the internal friction changes with fluence. Similar behavior to reactor-spectrum irradiation (Figure 5) is seen, but with an interesting difference. The changes of the superconducting  $T_c$  scale with damage energy when comparing the two types of neutron spectra (14-MeV neutron  $\sim 6$  times more effective /10/), whereas the comparison here would give a value closer to 2.

Although  $\text{Nb}_3\text{Sn}$  is now the leading A15 candidate for high-field utilization, it is certain that for almost all applications the superconducting properties will be enhanced by the addition of one or more alloying addition, creating a "pseudobinary" compound. The question of how these additions might affect the martensitic transformation and therefore the basic critical properties, then arises.

The effects of adding Ti to the  $\text{Nb}_3\text{Sn}$  compound on the low-temperature internal friction are seen in Figure 8. Here it is noted that 3 at. % in the matrix completely suppresses the transformation by reducing  $T_m$  below  $T_c$ . As with neutron irradiation, Ti alloying reduces  $T_m$  and the magnitude of  $Q^{-1}$ . Both  $Q^{-1}$  and  $T_m$

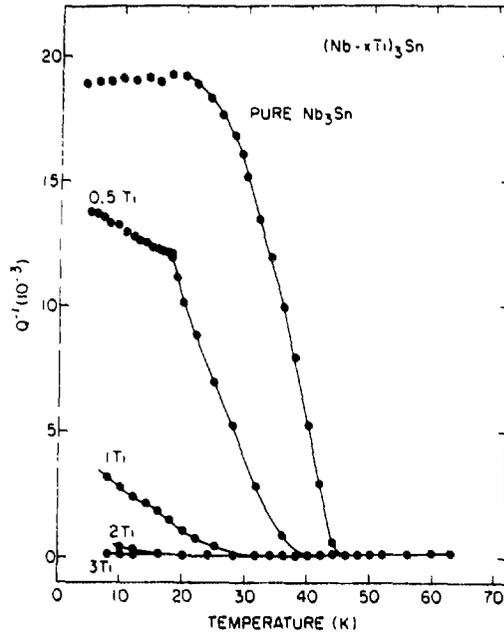


Fig. 8. Low-temperature  $Q^{-1}$  vs. temperature for  $Nb_3Sn + xTi$  for several values of  $x$ .

are similarly reduced by the alloying of a few percent of Ta but with  $T_m$  completely suppressed at the 7-at. % level, in comparison with 3 at. % for the Ti. It is to be noted that the introduction of Ti or Ta reduce both  $T_m$  and  $Q^{-1}$  due to domain-wall motion. The effects of Ti addition to the modulus is seen in Fig. 9 where the results are quite similar to those of the neutron-irradiated specimens.

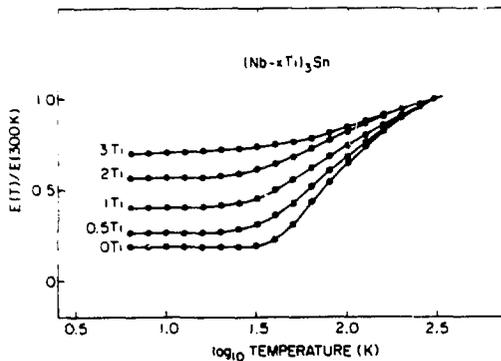


Fig. 9. Reduced modulus  $E(T)/E(300 K)$  vs. temperature for several concentrations of Ti in  $Nb_3Sn$ .

In continuing the study of third-element additions, an interesting departure from the behavior seen above was found. For the additions of Zr, the results shown in Fig. 10 were found. Here the low-temperature  $Q^{-1}$  is monotonically reduced by increasing levels of Zr, but  $T_m$  is unaffected. Further, the change in the curvature of  $Q^{-1}$  between  $T_m$  and  $T_C$ , seen earlier in the neutron-irradiated cases (and also in Fig. 8 for the Ti), is not evident here. This change in curvature was earlier attributed to a spread in the temperature range over which the transformation was taking place. For the Zr alloy, where  $T_m$  is not affected, this broadening of  $T_m$  does not obviously take place. Results similar to those of Zr are shown in Fig. 11 for Hf additions. The modulus curves for both of these alloys (Zr and Hf) are quite similar to those of Ti in Fig. 9, and are not shown.

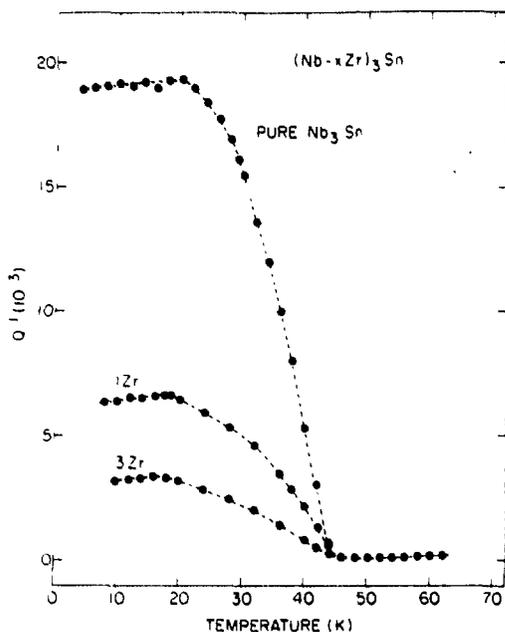


Fig. 10. Low-temperature  $Q^{-1}$  vs. temperature for  $Nb_3Sn + xZr$  for several values of  $x$ .

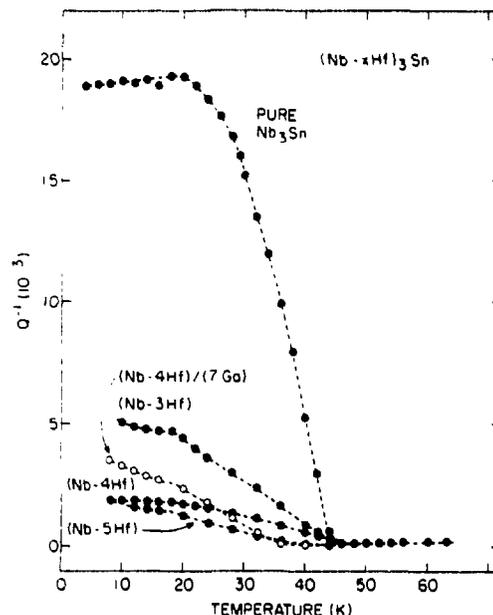


Fig. 11. Low-temperature  $Q^{-1}$  vs. temperature for  $Nb_3Sn + xHf$  for several values of  $x$ .

The difference in behavior of  $Q^{-1}$  and  $T_m$  for Ti and Ta additions on the one hand, and for Hf and Zr on the other are quite instructive. Where disorder is present in A15 compounds, whether by alloying, radiation damage, or deviation from stoichiometry, it is well known that the electrical properties (including the superconductivity critical properties) are much more sensitive to disorder on the A site than the B site./9/ The connection is then made to the alloying results here that it is probable that since Ti and Ta reduce  $T_m$ , but Hf and Zr do not, that Ti and Ta occupy the Nb sites, while Hf and Zr probably occupy the Sn sites since their presence does not suppress  $T_m$ . The EXAFS and TEM evidence for site occupation confirms the conjecture for the Ti and Ta: no definitive results for Hf or Zr are yet available. The major point regarding this is that we have here a possible new tool for identifying the site occupancy of dilute alloying additions, based upon internal-friction measurements.

Since the internal friction from the domain-wall motion is a clear indicator of the presence of transformed material, we also have a tool to test for the presence of the transformation in other A15 materials. Specimens of  $V_3Ga$  and  $Nb_3Ge$  have been tested. Fig. 12 shows the results for  $V_3Ga$ . First, the degree of modulus softening is about half of that of  $Nb_3Sn$ . The specimen is strain free and is near stoichiometry and perfect long-range order as attested by its value of  $T_c$ . Thus, we conclude from the lack of a low-temperature internal-friction feature (characteristic of twin-boundary motion) that  $V_3Ga$  probably does not undergo a martensitic phase transformation. Similar lack of internal friction in  $Nb_3Ge$  is rather inconclusive due to the substrate-induced strains and disorder in the specimens /11/.

There has been some work in the internal-friction effects of hydrogen in the A15's. Berry et al. /12/ investigated a relaxation peak associated with the presence of hydrogen. LeHuy et al. /13/ studied the effects of hydrogen charging on the martensitic transformation. The effects they found were very similar to those found by adding Ti or Ta: i.e., reduction of internal friction in the transformed regime and the reduction of  $T_m$ . The striking feature, however, is the complete suppression of  $T_m$  below  $T_c$  for hydrogen concentrations less than 1 at. % (see Fig. 13).

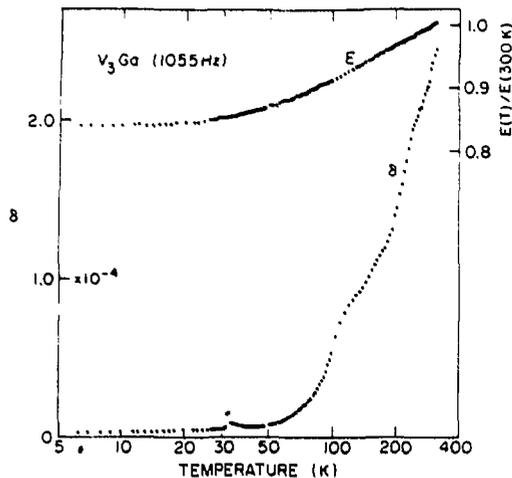


Fig. 12. Log decrement  $\delta$  and reduced modulus  $E(T)/E(300 \text{ K})$  for  $V_3Ga$ .

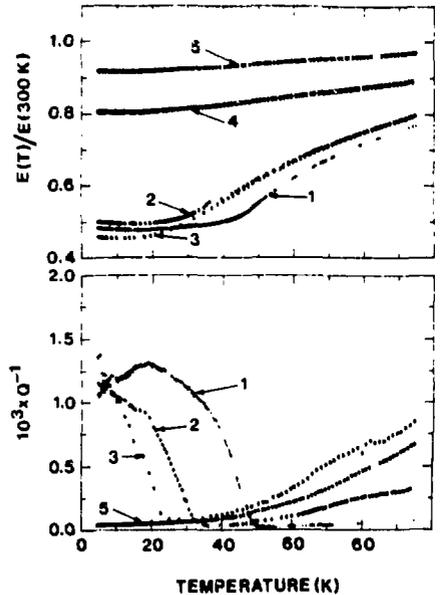


Fig. 13. Reduced modulus  $E(T)/E(300 \text{ K})$  vs. temperature (top) and  $Q^{-1}$  vs. temperature (bottom) for  $Nb_3Sn$  with various amounts of hydrogen: (1) None, (2) 0.2 at.%, (3) 0.15 at.%, (4) 1.8 at.%, and (5) 3.0 at. % (from LeHuy et al. /12/).

A departure from previous behavior is also noted that the reduction of softening (Fig. 13, top) does not scale with the reduction of  $T_m$  as with the metallic alloys. There are clearly different effects being manifested by the hydrogen inclusions that are not seen in other treatments. This would seem to be an interesting and fruitful area for further study.

For the A15 materials, we have only been concerned with internal friction due to the motion of twin boundaries that comprise the walls between differently oriented tetragonal domains. The presumption is that these boundaries move more easily under stress and/or have a much larger area than do any tetragonal/cubic ( $\beta/m$ ) domain walls. Dejonghe et al. /14/ succinctly outlined the type of internal-friction response to be expected from the several possible types of domain-wall motion in thermoelastically transforming specimens. The A15 results fit the case of easy  $m/m$  boundary motion, with little or no  $\beta/m$  contribution. The other major possibility for friction involves the case where  $\beta/m$  motion is predominant: cases where the threshold stress for  $m/m$  motion is higher than that for  $\beta/m$ , or due to the lack of  $m/m$  interfaces.

For the case of  $\beta/m$  interface motion, instead of constant (or increasing with  $c/a$ ) friction below  $T_m$ , a (ill defined) peak is expected below  $T_m$ . Also other effects such as heating-rate dependencies, hysteresis, etc. are to be expected. An example of this kind of phenomenon is shown in Fig. 14 for  $V_2Zr$  (Laves phase or C15 structure) which undergoes a cubic-to-rhombohedral transformation at a 116 K. The data here were taken for an increasing temperature ramp of  $\sim 1 \text{ K/min}$ . Two features are to be noted that contrast with the A15 results. The "peak" in the interval friction argues for  $\beta/m$  domain-wall motion, with no evidence for any  $m/m$  contribution. Also, the modulus begins to show hardening due to the transformed material, which is fully in keeping with expected behavior. Recall, that the A15's show no such hardening below  $T_m$ , and this lack of hardening is ascribed to a modulus effect due to the easy motion of the  $m/m$  domains. The hardening in the

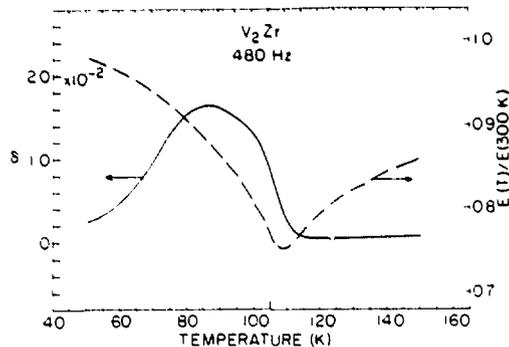


Fig. 14. Log decrement  $\delta$  vs. temperature for  $V_2Zr$  in region 2 the martensitic transformation. Reduced modulus  $E(T)/E(300 K)$  is also plotted.

$V_2Zr$ , then, is further evidence of the lack of a m/m loss mechanism being present in this system. This  $V_2Zr$  system also displays a marked hysteretic and heating dependence of the internal friction, that is consistent with  $\beta/m$  wall motion (L. Snead, to be published).

### CONCLUSIONS

The martensitic phase transition  $Nb_3Sn$  and its alloys has been shown to give rise to a large internal friction ( $Q^{-1}$ ). Presumably other A15 compounds, such as  $V_3Si$ , which have this type of transition will also manifest this internal friction. (However, the magnitude of  $Q^{-1}$  seems to vary with  $(c/a - 1)^2$ ; thus the magnitude for  $V_3Si$  should be a factor of about 8 smaller than that for  $Nb_3Sn$ .) The characteristics of the internal friction, such as the dependence on  $(c/a - 1)^2$ , are consistent with it being caused by the stress-induced motion of the boundaries (domain walls) between different variants of the tetragonal phase. Furthermore, these domain walls seem to be able to move relatively freely under the influence of the stress, but further understanding of the dynamics of domain-wall motion require additional experiments to characterize the stress-amplitude and frequency dependence

of the internal friction. Both the internal friction strength and the softening of the elastic modulus associated with the martensitic phase transition were shown to depend sensitively on the state of stress, the degree of disorder, the presence of solutes, and other factors; thus they will provide useful tools for the further investigation of this interesting phase transition in an important class of intermetallic compounds.

### ACKNOWLEDGMENTS

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### APPENDIX A. Simple Model for the Low-Temperature Internal Friction and Modulus Defect in A15 Compounds

Consider a sample consisting of material transformed into the tetragonal phase, with volume fraction  $f_t$ , as well as, possibly, some untransformed material in the cubic phase, with volume fraction  $(1-f_t)$ . The transformed material consists of domains of the three possible variants of the tetragonal phase (i.e., with the  $c$  axis along either the  $x$ ,  $y$ , or  $z$  axes); the volume fraction of each of the different types of domain will be denoted by  $f_x$ ,  $f_y$ , and  $f_z$ , with  $f_t = f_x + f_y + f_z$ . We assume, for simplicity, that the applied stress used in the measurement of the

dynamic modulus does not alter the total amount of transformed material, so that  $f_t$  is a constant. Furthermore, we assume that the elastic strain induced in an individual domain is much smaller than the tetragonality  $(c/a-1)$  caused by the martensitic transformation.

Again for simplicity, consider the effect of an oscillating uniaxial tensile stress along the z axis:

$$\sigma_{zz} = \sigma_0 e^{i\omega t} . \quad (1)$$

This will induce a component of strain along the z axis, which also oscillates (but not necessarily in phase with  $\sigma_{zz}$ ):

$$\epsilon_{zz} = \langle E^{-1} \rangle_0 \sigma_{zz} + \Delta f_z \left( \frac{c}{a} - 1 \right) , \quad (2)$$

where the first term represents the instantaneous elastic strain and the second is the contribution due to domain-wall motion.  $E_0$  is the unrelaxed Young's modulus, while the angular brackets represent a volume average over the various domains as well as the untransformed material.  $\Delta f_z$  is the time-dependent change in the volume fraction of z axis domains produced by the consumption or creation of adjacent x- and y-axis domains by domain-wall motion. The internal friction,  $Q^{-1}$ , and Young's modulus  $E$ , are obtained by standard methods /15/ from the in-phase and out-of-phase components of  $\epsilon_{zz}/\sigma_{zz}$ :

$$Q^{-1} = \frac{-2\pi \left( \frac{c}{a} - 1 \right) \text{Im} (\Delta f_z / \sigma_{zz})}{E^{-1}} , \text{ and} \quad (3)$$

$$E^{-1} = \langle E^{-1} \rangle_0 + \left( \frac{c}{a} - 1 \right) \text{Re} (\Delta f_z / \sigma_{zz}) . \quad (4)$$

The required change in z-domain volume fraction,  $\Delta f_z$ , is a complex quantity with the relative contribution of its real and imaginary parts dependent on the details of domain-wall dynamics, about which more later. If however, in general the dynamic response of the domain populations to an applied stress will be of the form:

$$\Delta f_z \propto F(\sigma_{zz}) \cdot R(\omega) \cdot A ,$$

where  $F(\sigma_{zz})$  is the (thermodynamic) force on a domain wall caused by the stress  $\sigma_{zz}$ ,  $R(\omega)$  is a frequency-dependent response function which depends on the mechanism of domain-wall motion, and  $A$  is the domain-wall area per unit volume. The force  $F$  is found from the change in the elastic thermodynamic potential of the crystal caused by the displacement of the wall separating two types of domain (e.g., x domain and a z domain); this may be found using the explicit expressions for the elastic thermodynamic potentials of the three types of domain given by Pietrass./16/ Thus:

$$F(\sigma_{zz}) = g \sigma_{zz} \left( \frac{c}{a} - 1 \right) v_d^{2/3} ,$$

where  $g$  is a numerical factor which depends on the geometrical shape of the domains, and  $v_d$  is the average domain volume. Consequently, the internal friction and Young's modulus are given by:

$$Q^{-1} = - \frac{2\pi \left( \frac{c}{a} - 1 \right)^2 f_t v_d^{1/3}}{E^{-1}} \text{Im} R(\omega) \quad (5)$$

and

$$E^{-1} = \langle E_0^{-1} \rangle + \alpha \left( \frac{c}{a} - 1 \right)^2 f_c v_d^{1/3} \operatorname{Re} R(\omega), \quad (6)$$

where  $\alpha$  is a numerical factor which depends on the domain shape. It is seen from Eq. (5) that the internal friction is proportional to  $(c/a-1)^2$ , and this is observed experimentally as shown in Figure 4. Basically, the factor  $(c/a-1)^2$  arises because the strain produced when a domain wall moves is proportional to  $(c/a-1)$ . The product of these two factors enters into  $Q^{-1}$ , which is therefore proportional to  $(c/a-1)^2$ . Note that the fact that the temperature dependence of  $Q^{-1}$  is essentially accounted for by that of  $(c/a-1)^2$  implies that the frequency response function  $R(\omega)$ , and hence the domain-wall mobility, must depend only weakly on temperature.

A specification of the frequency dependence of the internal friction,  $Q^{-1}$ , and the modulus defect,  $\langle E_0^{-1} \rangle^{-1} - E$ , requires an explicit model for the domain-wall dynamics so that the response function  $R(\omega)$  can be evaluated. For example, if domain walls are reasonably mobile over most of their extent, except for certain edges, corners, etc., where they are highly pinned (by, for example, interactions with grain boundaries, intersecting with other domain walls, etc.), and if there is no critical stress which must be overcome prior to motion, as discussed by DeJonghe et al. /14/, then a damped-harmonic-oscillator model of domain-wall dynamics may be appropriate. (A recent theoretical study of domain-wall motions in Al<sub>5</sub> compounds by Barsch and Krumhansl /17/ suggests that these walls behave as solitons, and thus they should not have strong "Peierls-Nabarro"-type critical stresses required to set them moving.) In such a harmonic model, domain walls will be characterized by an effective mass  $m$ , resonance frequency  $\omega_0$ , and viscous-damping coefficient  $\kappa$  (to account for damping by electron scattering, phonon emissions, etc.), the dynamics will then be characterized by:

$$m\ddot{x} + \kappa \dot{x} + m\omega_0^2 x = F(t) \quad (7)$$

where  $x$  is the boundary displacement caused by a force  $F$ . Such dynamics lead to the response function:

$$R(\omega) = \frac{m(\omega_0^2 - \omega^2) - i \kappa \omega}{m^2(\omega_0^2 - \omega^2)^2 + \kappa^2 \omega^2}. \quad (8)$$

The frequency dependence levels of the internal friction and modulus defect for the damped-harmonic-oscillator model of domain-wall dynamics are then obtained by combining Eq. (8) with Eqs. (5) and (6). Further experiments are required to test the predictions of this model.

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