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MAGNETIC STRUCTURES: NEUTRON DIFFRACTION STUDIES

BOUREE-VIGNERON F.
Laboratoire Leon Brillouin, Centre d'Etudes Nucleaires de Saclay,
91 - Gif-sur-Yvette (FR)

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MAGNETIC STRUCTURES : NEUTRON DIFFRACTION STUDIES

F. BOUREE- VIGNERON

**Laboratoire Léon Brillouin (CEA-CNRS), CEN-SACLAY
F-91191 GIF-SUR-YVETTE Cedex**

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ABSTRACT

Neutron diffraction is often an unequivocal method for determining magnetic structures. Here we present some typical examples, stressing the sequence through experiments, data analysis, interpretation and modelisation.

Two series of compounds are chosen:

a) RT_2X_2 (R = Rare Earth, T = 3d metal and X = Si or Ge),

b) RBe_{13} (R = Rare Earth).

Depending on the nature of the elements R, T, X, the magnetic structures produced can be commensurate, incommensurate or even show a transition between two such phases as a function of temperature.

A model, taking magnetic exchange and anisotropy into account, will be presented in the case of commensurate-incommensurate magnetic transitions in RBe_{13} .

1. INTRODUCTION

The only direct method to determine magnetic structures (ferromagnetic or antiferromagnetic, colinear or non-colinear, commensurate or incommensurate ...) is magnetic neutron diffraction .

The interaction between an atom and a thermal neutron may be accounted for by a scattering amplitude

$$b + 2\mathbf{BI} \cdot \mathbf{S} + (\gamma r_0/2) \mathbf{M}_\perp \cdot \mathbf{S}.$$

The first and second term in this expression are of nuclear origin: b is the isotropic nuclear scattering length ($b \sim 10^{-12}$ cm); $2\mathbf{BI} \cdot \mathbf{S}$ expresses the interaction between the spin of the nucleus \mathbf{I} and the spin of the neutron \mathbf{S} . In the general case of an unpolarised sample ($\langle \mathbf{I} \rangle = 0$), this term gives only rise to incoherent scattering.

The third term $(\gamma r_0/2) \mathbf{M}_\perp \cdot \mathbf{S}$ corresponds to the dipolar interaction between the magnetic moment of the neutron and the electronic magnetic moment of the atom \mathbf{M} (spin

and orbital contributions). M_{\perp} denotes the component of M perpendicular to the scattering vector K : $M_{\perp} = (K/K) \wedge (M \wedge (K/K)) f(K)$ with $f(K)$, magnetic form factor.

Let us notice that the nuclear scattering amplitude b ($\sim 10^{-12}$ cm) and the magnetic scattering amplitude $(\gamma r_0/2)M_{\perp}S$ are of the same order of magnitude: when M is in Bohr magnetons units, $(\gamma r_0/2)$ is equal to $0.27 \cdot 10^{-12}$ cm. As a consequence, the magnetic scattering can be easily measured with neutrons.

Thermal neutrons display interferences when scattered from ordered condensed matter systems, thus allowing to determine either crystallographic or magnetic structures.

This elastic coherent scattering is accounted for by nuclear and magnetic structure factors:

$$F_N = \sum_i b_i \exp(2i\pi K \cdot r_i)$$

and

$$F_M = 0.27 \cdot 10^{-12} \sum_i [[(M_i \cdot K/K) K/K] - M_i] f_i(K) \exp(2i\pi K \cdot r_i)$$

With a non polarised incident neutron beam, the neutron intensity diffracted at a 2θ angle ($2d_K \sin\theta = \lambda$) is proportional to $F_N^2 + F_M^2$

The neutron diffraction experiments can be done either on single crystals (four-circles diffractometer) or polycrystalline materials (two-axis diffractometers). Here we shall be concerned with powder diffraction only.

On Figure 1, the scheme of a two-axis diffractometer is drawn: G4.1 located on a neutron guide beam at the ORPHEE reactor in Saclay. A Position Sensitive Detector is available (800 cells over a 80 degrees - 2θ range); the usual wavelength is 2.438\AA .

In the next paragraphs, we are not going to present a systematic study of all types of systems studied in magnetic neutron diffraction. We will show the different steps of a neutron diffraction magnetic structure determination : experiment, data analysis, magnetic structure determination and modelisation. For this purpose, we have chosen two series of compounds :

- a) RT_2X_2 with R = Rare Earth, T = 3d transition metal, X = Si or Ge
- b) RBe_{13} with R = Rare Earth.

2. TbNi₂Ge₂

2.1 Definition

TbNi₂Ge₂ belongs to the RT₂X₂ series of compounds (with R = Rare Earth, T = *nd* transition metal and X = Si or Ge) with the tetragonal ThCr₂Si₂-type crystallographic structure (space-group I4/mmm). Many of these compounds have been magnetically studied over the last ten years[1]. They offer a great variety of magnetic behaviours, as a function of the elements R, T and X. As an indication, Table I gives the results obtained for the R =Tb / T = Mn, Fe, Co, Ni, Cu / X = Si, Ge compounds. All of them, except TbFe₂Ge₂, show a long range antiferromagnetic order; for these compounds, the Néel temperature T_N has two distinct orders of magnitude: ~500 K if the 3d transition metal is magnetic (Mn) or ≤50 K if T is non magnetic (Fe, Co, Ni, Cu). Figure 2 gives two magnetic structures in the series: TbNi₂Si₂ and TbCo₂Si₂.

For TbNi₂Ge₂ the only available data have been obtained in a powder neutron diffraction experiment [2]: two magnetic transition temperatures are given, respectively equal to 16 K and 9 K. The magnetic structures of the compound have not been solved; the authors only indicate that they are incommensurate.

2.2 Experiment

Neutron data were collected on a powder sample, at T=300 K and T ≤20K, with the 3T2 and G4.1 2-axis diffractometers respectively. The wavelength, angular range and step of the scans were respectively equal to : 1.2263 Å, 6° < 2 θ < 116°, 0.05° (High Resolution Powder Diffractometer 3T2) and 2.438 Å, 2° < 2 θ < 82°, 0.10° (G4.1).

2.3 Data analysis

The Rietveld[3] profile refinement technique was used for the determination of the crystallographic and magnetic structures. In this procedure a Gaussian profile has been assumed. Two types of parameters are considered:

(1) Those describing the characteristics of the diffractometer: Z (zero position), U V W (Full Width at Half Maximum parameters: $FWHM^2 = U \text{tg}^2\theta + V \text{tg}\theta + W$) and P (asymmetry parameter).

(2) Those characteristic of the sample : S (overall scale factor), G (preferential orientation parameter), a b c α β γ (crystallographic unit cell parameters), x y z ...,n...(positional parameters and occupation number of the atoms in the nuclear unit cell), M_x M_y M_z ...(magnetic moment components) and Debye-Waller factors (either isotropic or anisotropic)

Magnetic structures can be commensurate or incommensurate.

2.3.1 T=300K / Crystalline Structure

The neutron diffraction data at room temperature (3T2) have been analysed within the I4/mmm crystallographic ThCr_2Si_2 -type structure with Tb in (2a) 0. 0. 0., Ni in (4d) 1/2 0. 1/4;0. 1/2 1/4 and Ge in (4e) 0. 0. $\pm z$ ($z \sim 3/8$). The results are given in Table II (the subsequent nuclear scattering amplitudes have been used : $b_{\text{Tb}}=0.738$, $b_{\text{Ni}}=1.030$ and $b_{\text{Ge}}=0.819 \cdot 10^{-12}$ cm).

2.3.2 Magnetic Structures

At low temperatures, additional diffraction peaks appear (figures 3a,b,c), which are of magnetic origin and cannot be explained in terms of the tetragonal unit cell. No magnetic contribution is observed at the nuclear Bragg positions.

The first step in a magnetic structure determination is to index these peaks i.e. to determine the magnetic unit cell, or the propagation vector of the magnetic structure.

The additional Bragg peaks observed at T=12K (figure 3b) can be accounted for by a magnetic cell a a 4c i.e. a propagation vector $\tau = 1/4 c^*$.

At T=1.45K, all the peaks in the diffraction diagram (figure 3c) cannot be indexed with the only propagation vector $\tau = 1/4 c^*$. Another magnetic propagation vector is necessary : $\tau' = 1/2 (a^*+b^*+c^*)$.

A first result, which is obtained in this study, is that the magnetic structures of TbNi_2Ge_2 are commensurate, contrary to what is indicated in the literature[2].

Another step in a magnetic neutron diffraction study is to get the value of the magnetic ordering transition temperature(s). To do that, the only way to proceed is to

follow the thermal variation of the magnetic intensities. Figure 4 is showing this evolution for the main magnetic Bragg peaks: 110, 111, 112 (magnetic unit cell : 2a 2a 2c) and 101 (a a 4c). We get $T_N=17K$ and $T_{N'}=10.25K$ in good agreement with the results of H. Pinto et al [2] ($T_N=16K$ and $T_{N'}=9K$).

The last, but not least step, is the study of the magnetic intensities. In the present case, we must distinguish two cases: (1) $T = 12K$ and (2) $T = 1.45K$.

T=12K / The neutron diffraction diagram is obtained in the 2-82° 2θ range but due to Al sample-holder contamination at high 2θ values (111 and 200 Al Bragg peaks) or absence of peaks at low angles, the Rietveld method is only applied from 2θ = 10° to 61.5° (G4.1).

Table III gives the indices of the observed peaks : two conventions are used, either the commensurate magnetic cell a a 4c, either the propagation vector (0 0 1/4).

We can notice that within the second convention the selection rules are : $h k l^{\pm}$ only with $h+k+l$ odd ; no $00l^{\pm}$ peak. These rules correspond to a longitudinal sine-wave modulated structure (M // c) represented on Figure 5. The analysis of magnetic intensities yields $M = 8.8 \pm 0.2\mu_B$ at 12K.

T=1.45K / The neutron diagram has been obtained in the same experimental conditions as above (T=12K). All additional peaks can be accounted for:

(a) either with $\tau = 1/4c^*$: we have $100^{\pm}, 100^{\pm 3}, 102^{-3}, 102^{-}, 102^{+}, 111^{-3}, 111^{-}, 111^{+}, 102^{+3}, 111^{+3}$ i.e. 1st and 3rd order satellites of hkl with $h+k+l$ odd. No $00l^{\pm}$ contribution is observed.

(b) either with $\tau'=1/2(a^*+b^*+c^*)$. In the magnetic unit cell 2a 2a 2c these peaks are labelled 110, 111, 112, 113, 114, 115, 116 and 310, with h and k satisfying the selection rule h and k odd. This implies that magnetic moments of atoms separated by a (or b) are opposite (cf Figure 2- TbNi₂Si₂).

The profile analysis of the diagram leads to the moments listed in Table II. All these moments are parallel to the c axis.

The magnetic (0 0 1/4) structure looks like that obtained at higher T (12K) and represented on Figure 5. The only difference is its squaring up, as revealed by the

existence of third order satellites. The ratio of the first and third order components of the magnetic moment (A and B) can be deduced from the ratio M/M' : $M=A+B$ and $M'=A-B$, leading to $B/A=0.225 \sim 2/3$ $1/3$ with $A=10.15(35)$ and $B=2.30(35)$. $A/B=1/3$ would correspond to a perfect squared modulated structure.

The magnetic (2a 2a 2c) structure is given on Figure 6.

2.4 Discussion

Let us notice that the magnetic structure at very low T ($T=1.45K$) as described in the preceding section is not really a reasonable one : for instance, the magnetic moment of Tb^{3+} on $z=1/4$ (a a 4c unit cell) is greater than the saturated Tb^{3+} value: $12.45 = 8.8 \sqrt{2} > g_J J = 9 \mu_B$. This does not mean that the structure (or profile) refinement is incorrect, but in the present case that neutron diffraction cannot yield the relative phases of the two propagating magnetic structures. Some complementary studies are needed to solve the problem, either experimental: magnetic measurements... or theoretical: group theory...

3. RBe_{13} (R=Gd,Tb,Dy,Ho,Er)

Our intention here is not to give in greater details the neutron diffraction studies on these materials. These can be found in references [4-10]. The results we obtained will only be presented and discussed, as an example of what can be done with neutron diffraction and magnetic structures.

3.1 Introduction

The Rare Earth beryllides RBe_{13} crystallise in the cubic $NaZn_{13}$ -type structure, space group $Fm\bar{3}c$ ($a \sim 10 \text{ \AA}$), with 8 R in (a) $\pm[1/4 \ 1/4 \ 1/4]$, 8 Be in (b) $[0 \ 0 \ 0]; [1/2 \ 1/2 \ 1/2]$ and 96 Be in (i) $\pm[0 \ y \ \pm z]$; $\pm[1/2 \ \pm z \ y]$ with $y \sim .114$ and $z \sim .176$.

The only magnetic ions in the structure are the R^{3+} ions; they are ordered in a cubic cell of parameter $a/2$. The local symmetry of the R^{3+} site is cubic (43), with a nearly spherical environment, thus leading to a rather small Crystalline Electric Field (CEF overall splitting less than 40K in the studied series [5]).

The magnetic structures thus result from the competition between exchange and anisotropy, two energy terms which are of the same order of magnitude.

3.2 Magnetic structures

Commensurate and/or Incommensurate (spiral) magnetic structures are observed, depending on the nature of the Rare Earth (see Table IV). Figure 7 gives the thermal variation of the propagation vector τ : $\tau = 1/3 [1-\epsilon(T)]c^*$. Figures 8 and 9 show respectively the incommensurate [$\epsilon(T) \neq 0$] and commensurate [$\epsilon(T) = 0$] RBe_{13} magnetic structures .

The commensurate structure, depicted in Figure 9, is not a regular helimagnetic structure: the sequence of magnetic moments $M_1, M_2, M_3 \dots$ in a regular helix would be $0, \pi/3, 2\pi/3 \dots$ and correspond only to 1st order satellites of the nuclear Bragg peaks $h k l$. Here we have $0, \pi/3 + \delta, 2\pi/3 - \delta \dots$. As an experimental evidence of $\delta \neq 0$, the 3rd order satellites of $h k l$ ($h, k, \text{ and } l$ even) are observed.

3.3 Model

As already mentioned, these structures result from a competition of isotropic magnetic exchange and magnetocrystalline anisotropy.

Magnetic exchange is of RKKY type: the Néel temperatures T_N are a function of the de Gennes' parameter $\zeta = (g_J - 1)^2 J(J+1)$ where $J = L+S$ and g_J is the Landé factor. We have $T_N = \zeta^{1.2}$.

This magnetic exchange can be treated within a molecular field approximation. We define the exchange parameters J_0, J_1, J_2 as magnetic interaction between a R^{3+} ion and all the R^{3+} ions in the same ferromagnetic (001) plane, in the nearest and next-nearest (001) planes respectively (Figure 10).

The exchange energy is then written as:

$$H_{\text{Exchange}} = -J_0 - J_1 \langle \cos(\theta_{j+1} - \theta_j) \rangle - J_2 \langle \cos(\theta_{j+2} - \theta_j) \rangle$$

where θ_j is the angle between one easy magnetisation axis and the magnetic moments M_j in the ferromagnetic (001) j^{th} plane.

For GdBe_{13} , this term is the only energy term: Gd^{3+} is an S ion, with no magnetocrystalline anisotropy. An incommensurate helimagnetic structure is easily obtained when $J_0 > 0$, $J_1 > 0$, $J_2 < 0$ and $J_1 + 4J_2 < 0$: the regular angle θ_0 between two magnetic moments in nearest (001) planes is then $\cos\theta_0 = -J_1/4J_2$.

For RBe_{13} , with $R = \text{Tb, Dy, Ho, Er}$, anisotropy corresponds to an easy (001) plane ; within this plane easy magnetisation axis are perpendicular. We can write:

$$H_{\text{Anisotropy}} = -h \langle \cos n\theta_j \rangle$$

with $n=4$ in the present case (tetragonal symmetry).

We must look for a minimum of $H = H_{\text{Exchange}} + H_{\text{Anisotropy}}$

$$\text{with } H = -4\cos\theta_0 \langle \cos(\theta_{j+1} - \theta_j) \rangle + \langle \cos(\theta_{j+2} - \theta_j) \rangle - h \langle \cos 4\theta_j \rangle$$

The solution we try is $\theta_j = j\theta + \alpha + A \sin 4(j\theta + \alpha)$, with parameters θ, α and A .

In the expression of H two cases must be distinguished for the mean values determination: incommensurate and commensurate θ values [$\theta = 2\pi/q \cdot p/q$ with p and q mutual primes, in the commensurate case].

Two distinct expressions of H are then obtained:

$$H_{\text{INC}} = -4\cos\theta_0 \cdot \cos\theta J_0(z_1) + \cos(2\theta) J_0(z_2) + h J_1(4A)$$

an expression which, as expected, is α independent

$H_{p,q}$ (commensurate) includes higher order ($k > 1$) Bessel functions $J_k(z)$ of the parameters $z_1 = 2A \sin 2\theta$, $z_2 = 2A \sin 4\theta$, $4A$ and is α dependent.

A numerical minimisation is done for either the incommensurate or the commensurate structure. The "minimum minimorum" is then taken and leads to the

magnetic phase diagram of Figure 11 (x-axis : anisotropy, y-axis : exchange). Let us notice that in the commensurate solution the α phase is fixed: $\alpha = 0$ if q odd and $\alpha = \pi/q$ if q even. The commensurate structures $[p,q]$ are also represented on that Figure: the hatched region is that corresponding to the observed commensurate structure in the RBe_{13} series we study.

This type of diagram can interpret (at least in a qualitative way) the thermal variation of the magnetic structure: we can easily imagine that exchange is a constant, but anisotropy is varying with T , increasing when T is lowered. For a given exchange parameters set (J_1, J_2), depending on the initial (i.e. $T > T_N$) value of anisotropy, we can then observe when T is decreased, either a transition from an incommensurate to a commensurate magnetic structure, either an "always" commensurate structure (with A function of T).

4.CONCLUSION

The preceding studies on rare earth intermetallics are characteristic examples of magnetic neutron diffraction.

$TbNi_2Ge_2$ exhibits two magnetic transitions as a function of T : below $T_N = 17$ K, the magnetic structure is a longitudinal sine-modulated structure (wave-vector $\tau = 1/4c^*$ and Tb^{3+} magnetic moments // c); below T_N' the Tb^{3+} magnetic moments are still directed along the tetragonal c axis, but at the present time, we have not yet solved the structure completely. Two wave-vectors coexist $\tau = 1/4c^*$ and $\tau' = 1/2(a^*+b^*+c^*)$ and the problem is to determine the relative phases of the two propagating magnetic components.

The neutron diffraction RBe_{13} study is more complete: from experiment to structure determination (commensurate and/or incommensurate magnetic structures) and interpretation (model of competing magnetic exchange and anisotropy). This series of intermetallic compounds has also been studied by other techniques: magnetic measurements, specific heat experiments, Mössbauer effect as a complement to elastic and inelastic neutron scattering [4-10 and references there in].

Finally, as already mentioned, we didn't present in this paper a systematic review of magnetic neutron diffraction: in particular, single crystal studies, polarised neutrons experiments and nuclear magnetic scattering have not been investigated.

ACKNOWLEDGMENTS

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TABLE CAPTIONS

Table I: TbT_2X_2 magnetic structures ([1] and references there in). $T_N(\text{K})$ is the magnetic ordering temperature, τ is the propagation vector of the magnetic structure. The direction of the Tb^{3+} magnetic moments is indicated: // c or $\perp c$ (c is the tetragonal crystallographic axis).

Table II: TbNi_2Ge_2 crystalline and magnetic parameters.

Table III: TbNi_2Ge_2 magnetic Bragg peaks at $T = 12\text{K}$ ($T_N' < T < T_N$). Two possibilities exist for indexing the peaks: in the first column, hkl values are indicated in the $a_1 a_2 4c$ magnetic unit cell; in the second column, the same Bragg peaks appear as 1st order satellites ($\tau = 0.25 c^*$) of hkl in the nuclear $a_1 a_2 c$ cell.

Table IV: RBe_{13} magnetic structures. C and I means respectively Commensurate and Incommensurate magnetic structure.

TABLE I

T	X	Si	Ge
Mn		$T_N = 550 \text{ K}$ $\text{Mn} \left\{ \begin{array}{l} \tau = (001) \\ M \parallel c \end{array} \right.$ $T_1 = 65 \text{ K}$ $\text{Tb}^{3+} \left\{ \begin{array}{l} F \\ M \parallel c \end{array} \right.$ $T_2 = 55 \text{ K}$	$T_N = 415 \text{ K}$ $\text{Mn} \left\{ \begin{array}{l} \tau = (001) \\ M \parallel c \end{array} \right.$ $T_1 = 110 \text{ K}$ $\text{Tb}^{3+} \left\{ \begin{array}{l} F \\ M \parallel c \end{array} \right.$ $T_2 = 25 \text{ K}$
Fe		$T_N = 10.5 \text{ K}$ $\tau = (0 \tau_y \tau_z)$ $M \parallel c$	No long range magnetic order ($T \geq 1.8 \text{ K}$)
Co		$T_N = 30 \text{ K}$ $\tau = (0 0 1)$ $M \parallel c$	$T_N = 10.5 \text{ K}$ $\tau = (0 0 1)$ $M \parallel c$
Ni		$T_N = 10 \text{ K}$ $\tau = (\frac{1}{2} \frac{1}{2} 0)$ $M \parallel c$	$T_N = 16 \text{ K} ; T_N' = 9 \text{ K}$
Cu		$T_N = 12 \text{ K}$ $\tau = (\frac{1}{2} 0 \frac{1}{2})$ $M \perp c$	$T_N = 13.5 \text{ K}$ $\tau = (\frac{1}{2} 0 \frac{1}{2})$ $M \perp c$

TABLE II

TbNi ₂ Ge ₂	T = 300 K	T = 12 K	T = 1.45 K
2-axis spectrometer	3T2	G4.1	G4.1

CRYSTALLINE STRUCTURE

a	4.0506(2) Å	4.0362(8) Å	4.0379(16) Å
c	9.7971(4) Å	9.7779(25) Å	9.7824(45) Å
z(Ge)	0.3714(2)	0.3680(12)	0.3696(8)
B _{Tb}	0.285(40)	0	0
B _{Ni}	0.745(25)	0	0
B _{Ge}	0.440(30)	0	0
G	0.195(5)	0.180(45)	0.210(20)

MAGNETIC STRUCTURES

$\vec{\tau} = \frac{1}{4} \vec{c}^*$		M = 8.8(2) μ _B	M = 12.45(35) μ _B M' = 7.85(30) μ _B
$\vec{\tau}' = \frac{1}{2}(\vec{a}^* + \vec{b}^* + \vec{c}^*)$			M = 9.50(25) μ _B

RELIABILITY FACTORS

R _N (%)	8.10	9.45	7.55
R _M (%)		5.90	6.05

TABLE III

a a 4c	$\tau = \frac{1}{4} c^*$
101	100 [±]
107	102 [·]
109	102 ⁺
113	111 [·]
115	111 ⁺

TABLE IV

R^{3+}	T_N (K)	T_N' (K)	Structure
Gd	27 ± 2		I
Tb	16.5 ± 1	8.5	C/I
Dy	10 ± 0.5		C
Ho	6 ± 0.5	4.5	C/I
Er	3 ± 0.25		C

FIGURE CAPTIONS

Figure 1: G4.1 2-axis spectrometer (ORPHEE Reactor, CEN-Saclay).

Figure 2: RT_2X_2 . Commensurate magnetic structures of $TbNi_2Si_2$ and $TbCo_2Si_2$.

Figure 3: $TbNi_2Ge_2$ neutron diffraction ($\lambda = 2.438 \text{ \AA}$) spectra at (a) $T = 85K$ ($T > T_N$) (b) $T = 12K$ ($T_N' < T < T_N$) and (c) $T = 1.45K$ ($T < T_N'$). Nuclear Bragg peaks (crystalline unit cell) are labelled hkl . Magnetic Bragg peaks are characteristic of two magnetic unit cells: a $a\ 4c$ and $2a\ 2a\ 2c$; they are respectively labelled $hkl^+...$ (wave vector notation: see Table III) and hkl .

Figure 4: $TbNi_2Ge_2$ Bragg scattering as a function of T . The ordering temperatures T_N' and T_N are deduced from the thermal variation of magnetic intensities 110, 111, 112 ($2a\ 2a\ 2c$ magnetic unit cell; full symbols) and 101 ($a\ 4c$ magnetic unit cell; open squares). As a reference, the nuclear Bragg peak 002 (+) is also drawn on the Figure.

Figure 5: $T = 12K$: $TbNi_2Ge_2$ magnetic structure (longitudinal sine-wave modulation).

Figure 6: $T = 1.45K$: $TbNi_2Ge_2$ magnetic unit cell $2a\ 2a\ 2c$

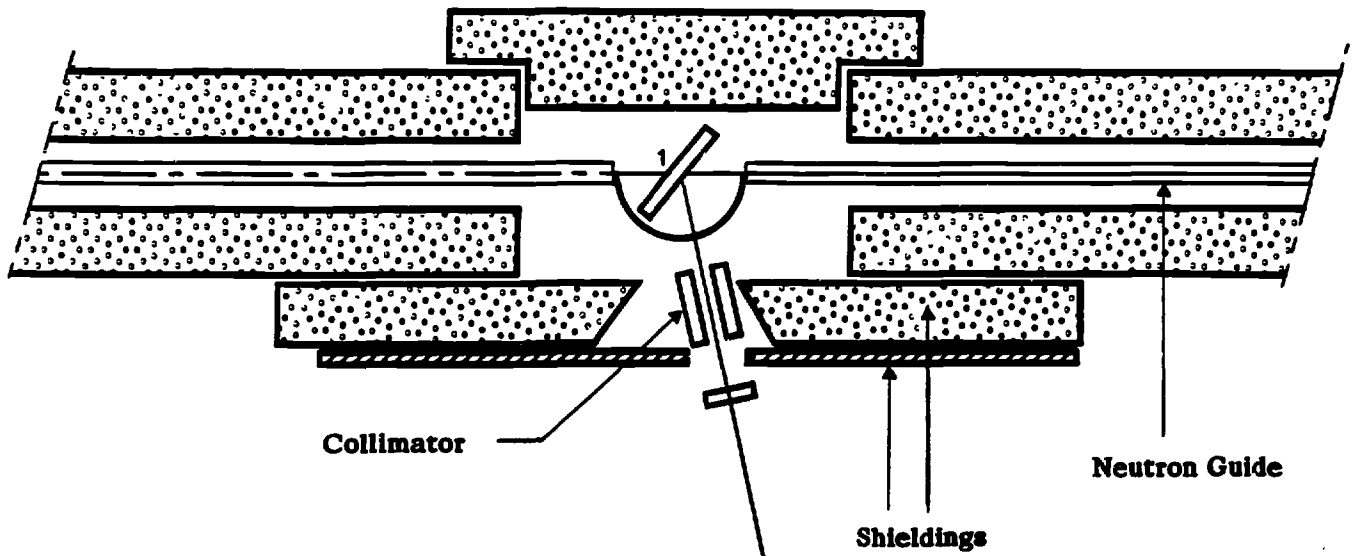
Figure 7: RBe_{13} magnetic propagation vector τ as a function of T (in reduced units).

Figure 8: RBe_{13} incommensurate magnetic structure (helimagnetism).

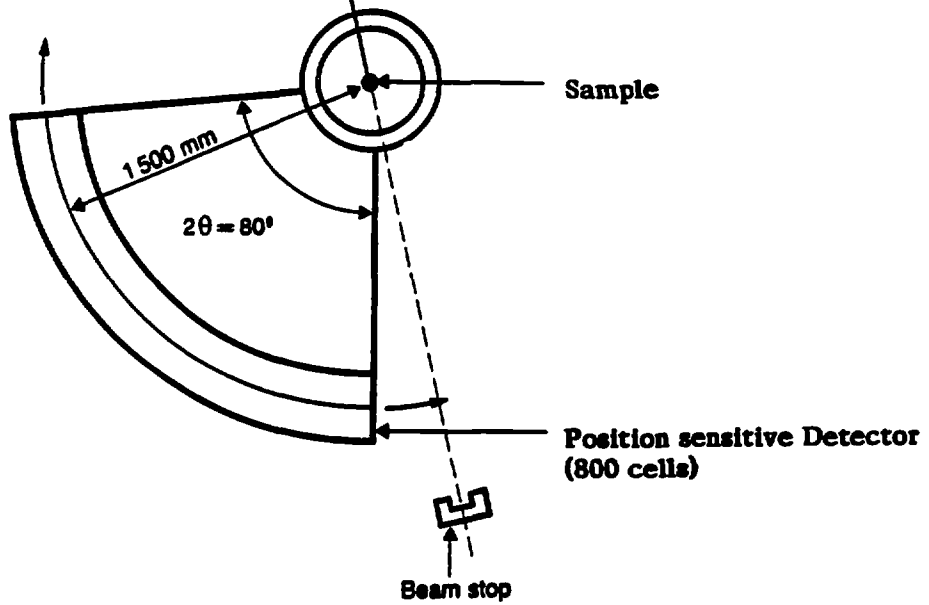
Figure 9: RBe_{13} commensurate magnetic structure.

Figure 10: RBe_{13} magnetic structures: ferromagnetic (001) planes and exchange constants J_0, J_1 and J_2 .

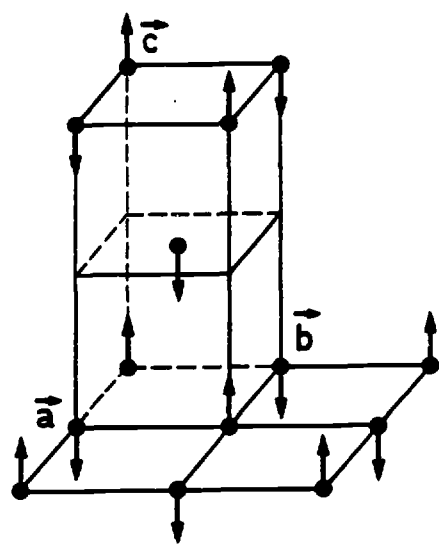
Figure 11: RBe_{13} magnetic phase diagram (x-axis = anisotropy, y-axis = exchange). I means Incommensurate (regular helix); the Commensurate Magnetic Structures are labelled $[p,q]$ and drawn in the corresponding areas of the diagram.



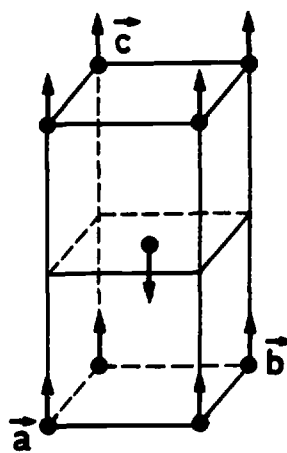
1. Monochromator



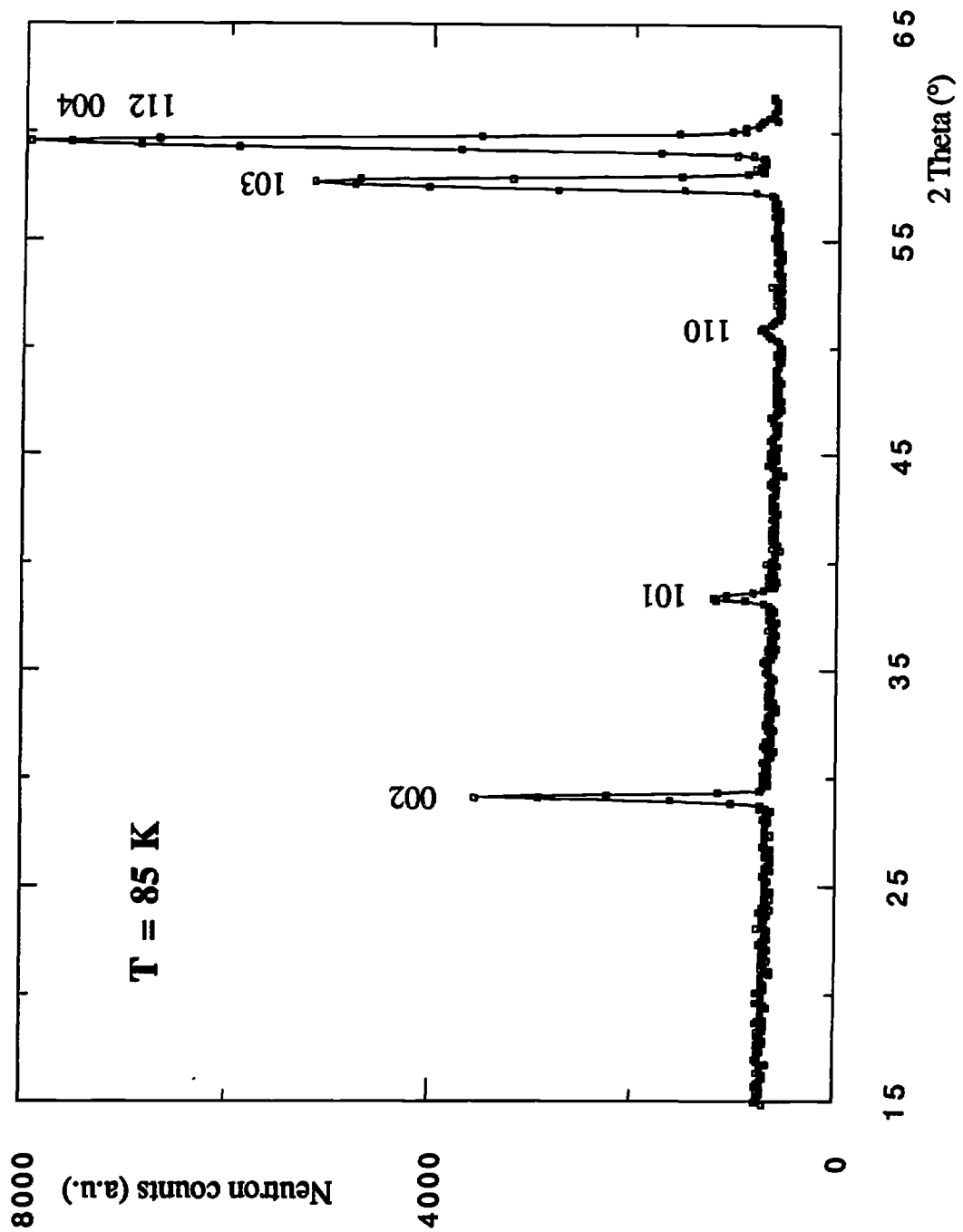
①



TbNi₂Si₂



TbCo₂Si₂



3a

3

3b

