

United Nations Educational Scientific and Cultural Organization  
and  
International Atomic Energy Agency

THE ABDUS SALAM INTERNATIONAL CENTRE FOR THEORETICAL PHYSICS

**THERMAL BEHAVIOUR OF A SOLAR AIR HEATER  
WITH A COMPOUND PARABOLIC CONCENTRATOR**

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**Abstract**

A mathematical model for computing the thermal performance of an air heater with a truncated compound parabolic concentrator having a flat one-sided absorber is presented. A computed code that employs an iterative solution procedure is constructed to solve the governing energy equations and to estimate the performance parameters of the collector. The effects of the air mass flow rate, the wind speed and the collector length on the thermal performance of the present air heater are investigated. Prediction for the performance of the solar heater also exhibits reasonable agreement with experimental data with an average error of 7%.

MIRAMARE – TRIESTE

November 2005

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## **1- Introduction**

Simulation models are important design tools and are useful for predicting the collector's experimental performance. In any solar energy application, it would be desirable to analyse theoretically any given system as extensively as possible before embarking the construction of one for installation. Rabl (1976), Hsieh (1981), Prapas et al. (1987), Norton et al. (1989), Eames and Norton (1993), and Oommen and Jayaraman (2001) analysed non evacuated CPC cavities with flat or cylindrical absorber. The thermal analyses of such collectors have been well documented (Tchinda et al. 1998, Fraidenraich et al. 1999, Tchinda 2003).

However, a close examination of the papers revealed that the case of a cylindrical absorber is of particular interest because standard piping and evacuated tubes are commonplace receiver elements, and because the cylindrical shape reduces thermal losses through the back of the collector. Other CPC configurations like non-evacuated stationary CPC solar collector with flat bifacial absorber (Tripanagnostopoulos et al. 2000), CPC augmented with a reverse flat plate absorber (Eames et al. 2001), asymmetric compound parabolic concentrator (Fang et al. 2003, Adsten et al. 2004, Mallick et al. 2004) have been proposed. Papers reporting thermal analysis of the CPC with flat one-side absorber are rarely found, and those published are devoted to the effect of truncation on optical, thermal losses and collectible energy (Carvalho et al. 1985), or to increase the electrical energy output (Gordon 1988). Recently, Pramuang and Exell (2005) reported the results of an experimental study in which the method of Chungpaibulpatana and Exell is used to determine the collector parameters of a solar flat plate collector with a CPC for heating air.

The purpose of this paper is to quantify the heat transfer within compound parabolic concentrating solar energy collectors with flat one-sided absorber. A mathematical model analysing the collector thermal performance is introduced and examined by using a constructed computer code that used an iterative procedure.

## **2- Structure of CPC and Mathematical modeling**

The CPC is capable of accepting solar radiation for long periods each day without diurnal tracking of the sun. It also has the advantage of concentrating the diffuse radiation, which is not possible using an imaging collector (Pramuang and Exell 2005). The two dimensional CPC collector with a flat absorber is the one studied experimentally by Pramuang and Exell (2005). The principal dimensions for the CPC collector used are labelled in figure 1 in both cross section figure 1-a and side view figure 1-b.

In order to simplify the analysis, the following main assumptions are made:

A-1: It is assumed that the CPC is ideal and free from fabrication errors.

A-2: Any beam of radiation incident within the acceptance angle  $\theta_a$ , with the help of the parabolic reflector can reach the receiver. The concentration ratio used in this work is defined on a geometrical basis and is expressed in terms of the total receiver area ( $C_a=1/\sin(\theta_a)=A_C/A_P$ ) (Hsieh 1981, Carvalho et al. 1985).

A-3: The reflection of radiation from the parabolic reflector is accounted for by the apparent reflectance  $\rho_m^{<n>}$ , with  $\langle n \rangle = 0.5 + 0.07C_a$  for a CPC with flat plate absorber (Rabl et al. 1979, Tchinda 2003).

A-4 The direction of the beam radiation incident on various components in the collector can be found through geometry. Any reflection from these components, particularly multireflections from the parabolic reflector, will cause a reorientation of rays to the effect that the ray's reflection pattern becomes exceedingly difficult to follow without reliance on a detailed ray tracing. To facilitate analysis these reflections are treated as diffuse and their energy accounted for in terms of diffuse reflectivities (Hsieh 1981, Tchinda 2003). The succeeding absorption and transmission processes inside CPC are diffusive and are accounted for in terms of diffuse properties. The solar and infrared energy exchanges in the collector are treated separately using pertinent radiative properties in the spectrum.

A-5 Physical and optical properties of materials are assumed to be independent of temperature.

A-6 The concentrator does not produce an image of the light source, hence it is called non-imaging concentrators.

Figure 1-c illustrates the electric analogy circuit for the CPC collector. Applying heat balances in a suitable way, the following set of partial differential equations can be derived:

**For cover**

$$M_c C_{pc} \frac{\partial T_c}{\partial t} = q_c(t) + h_{Rp}(T_p - T_c) + h_{p/c}(T_p - T_c) - h_{Rs}(T_c - T_s) - h_{c/a}(T_c - T_b) \quad (1)$$

with  $t > 0$ .

**For flate absorber**

$$M_p C_{pp} \frac{\partial T_p}{\partial t} = q_p(t) - h_{Rp}(T_p - T_c) - h_{p/c}(T_p - T_c) - q_u(t) \quad (2)$$

with  $t > 0$ .

## For fluid

$$\rho_f e_f C_{pf} \frac{\partial T_f}{\partial t} = q_u(t) - \frac{\dot{m} C_{pf}}{I_p} \frac{\partial T_f}{\partial x} - U_0(T_f - T_b) \quad (3)$$

with  $t > 0$  and  $0 < x < L$ .

In equations (1) and (2),  $q_c(t)$  and  $q_p(t)$  have been expressed using the Hsieh's theory (Tchinda, 2003), as:

$$q_c(t) = I(t) \left[ \bar{\alpha}_c + \bar{\alpha}_c \bar{\tau}_c \bar{\rho}_p \rho_m^{2\langle n \rangle} \right] \frac{A_c}{A_p} \quad (4)$$

$$q_p(t) = I(t) \bar{\tau}_c \rho_m^{2\langle n \rangle} P \left[ \bar{\alpha}_p + \bar{\alpha}_p \bar{\rho}_p \bar{\rho}_c \frac{A_p}{A_c} \right] \frac{A_c}{A_p} \quad (5)$$

$P$  is the gap loss factor, which is equal to  $1 - g/l_p$  (Rabl et al. 1979), where  $g$  is the gap thickness.  $A_c = W * L$  and  $A_p = l_p * L$

At any point  $x$ , the fluid temperature ( $T_f$ ) is related to the useful energy  $q_u$  (see equations (2) and (3)) and the absorber temperature ( $T_p$ ) by the following expression:

$$q_u = U_f (T_p - T_f) \quad (6)$$

The factor  $U_f$  is the convective heat transfer coefficient between heat transfer fluid and the walls of the absorber is calculated from the relationship:

$$U_f = \frac{N_{uf} \lambda_f}{D_H} \quad (7)$$

where the Nusselt number  $N_u$  and the hydraulic diameter  $D_H$  are given in the Appendix.

Since the absorptance of the cover and the thermal capacities of the components of the collector are small, we neglect them. However, the functioning of the collector remains variable with time because it depends on the unsteady solar intensity. Eliminating  $T_c$  and  $T_p$  from the simplified equations obtained, one gets:

$$C_{pf} \dot{m} \frac{dT_f}{dx} = I_p [S_p - U_L (T_f - T_b)] F' \quad (8)$$

with

$$S_p = I(t) \bar{\tau}_c \rho_m^{2\langle n \rangle} P \left[ \bar{\alpha}_p + \bar{\alpha}_p \bar{\rho}_p \bar{\rho}_c \frac{A_p}{A_c} \right] \frac{A_c}{A_p} + \frac{(h_{Rp} + h_{p/c}) \left( I(t) \left[ \bar{\alpha}_c + \bar{\alpha}_c \bar{\tau}_c \bar{\rho}_p \rho_m^{2\langle n \rangle} \right] \frac{A_c}{A_p} \right)}{h_{Rp} + h_{p/c} + h_{Rs} + h_{c/a}} - \frac{(h_{Rp} + h_{p/c}) \Delta T}{h_{Rp} + h_{p/c} + h_{Rs} + h_{c/a}} \quad (9)$$

$$U_L = \frac{(h_{Rp} + h_{p/c} + h_{Rs} + h_{c/a})(U_0 U_f + U_0 h_{Rp} + U_0 h_{p/c} + h_{Rp} U_f + h_{p/c} U_f) + (U_0 - U_f)(h_{Rp} + h_{p/c})^2}{(h_{Rp} + h_{p/c} + h_{Rs} + h_{c/a}) U_f} \quad (10)$$

$$F' = \frac{U_f (h_{Rp} + h_{p/c} + h_{c/a} + h_{Rs})}{(h_{Rp} + h_{p/c} + h_{c/a} + h_{Rs})(h_{Rp} + h_{p/c} + U_f) - (h_{Rp} + h_{p/c})^2} \quad (11)$$

To evaluate the collector's performance, it is necessary to estimate the overall loss coefficient  $U_L$ , the collector efficiency factor  $F'$  and the internal heat transfer coefficients. The relations about the various heat transfer coefficients determined are presented in the Appendix.

Assuming that the overall heat loss coefficient  $U_L$  and the collector efficiency factor are temperature independent in position, the efficiency is found to be:

$$\eta_{inst} = \frac{Q_u}{A_c I(t)} \quad (12)$$

where the useful thermal power  $Q_u$  extracted from the CPC collector is calculated from the relationship:

$$Q_u = F_R A_f \{S_p - U_L (T_{fc}(0,t) - T_b(t))\} \quad (13)$$

$F_R$  is a removal factor, it is given by:

$$F_R = \frac{C_{pf} \dot{m}}{I_p L U_L} \left( 1 - e^{\left( \frac{-I_p L F' U_L}{C_{pf} \dot{m}} \right)} \right) \quad (14)$$

Using equations (12) and (13),  $\eta_{inst}$  becomes:

$$\eta_{inst} = (\eta_0 + F_A) F_R - \frac{U_L}{C_a I(t)} F_R (T_{fc}(0,t) - T_b(t)) \quad (15)$$

where the optical efficiency is given:

$$\eta_0 = \bar{\tau}_c \rho_m^n \bar{\alpha}_p P \left( 1 + \bar{\rho}_p \rho_c \frac{I_p}{2W} \right) \quad (16-a)$$

According to Rabl et al. (1980) and to Pramuang and Exell (2005), the optical efficiency is given by:

$$\eta_{01} = \bar{\tau}_c \rho_m^{(n)} \bar{\alpha}_p \quad (16-b)$$

The optical efficiency determined from direct measurements (see Pramuang and Exell 2005) of the optical properties of the materials listed in table 1 using equations (16-a and b) have values  $\eta_0 \approx 0.72$  and  $\eta_{01} \approx 0.75$ , respectively. However the result of Pramuang and Exell (2005) obtained using equation (16-b) is different. The difference is due to the fact that in the numerical calculation of Pramuang and Exell (2005), the number of reflections is computed

using the relation  $\langle n \rangle = 1 + 0.07C_a$  which is a relation used for CPC with tubular absorber (Rabl et al. 1979). Analytical results of equation (16-a) agree with the optical efficiency found by direct measurements ( $\eta_0 = 0.67$ , see Pramuang and Exell 2005) with an error of 7%. Comparing equations (16-a) and (16-b), the ratio gives:

$$\frac{\eta_0}{\eta_{01}} = P \left( 1 + \bar{\rho}_p \rho_c \frac{l_p}{2W} \right) < 1 \quad (17)$$

An examination of this equation, when  $P \rightarrow 1$  ( $g \rightarrow 0$ , corresponding to a case where reflector touches receiver) shows that equation (16-a) agrees with (16-b) with an average error of 1%. In many solar thermal applications, however, it is necessary to have  $g \neq 0$  ( $P < 1$ ), because a gap between the reflector and the absorber is needed to reduce conductive heat losses. The above result shows that a gap between the reflector and the absorber causes optical losses, but a compromise between optical and thermal performance must be made.

In equation (15)  $F_A$  is named the enclosure absorption factor (Tchinda 2003). It is given by the relationship:

$$F_A = \frac{(h_{Rp} + h_{p/c})}{(h_{Rp} + h_{p/c} + h_{c/a} + h_{Rs})} \left\{ \bar{\alpha}_c + \bar{\alpha}_c \bar{\tau}_c \bar{\rho}_p \rho_m^{2\langle n \rangle} - \frac{\Delta T h_{Rs}}{I(t) C_a} \right\} \quad (18)$$

The performance of the system over a period of a day is computed as the daily average efficiency:

$$\eta = \frac{t_r \int \dot{m} C_{pf} (T_{f0}(L, t) - T_{fe}(0, t)) dt}{A_c \int I(t) dt} \quad (19)$$

where  $t_r = 6$  a.m. and  $t_s = 6$  p.m.

### 3- Calculation procedure

In numerical calculations, an iterative method is used to bring the effect of the temperature dependence of various heat transfer coefficients. For certain temperatures, they are first calculated by using the standard expressions given earlier. Equations are solved by assuming the constant and the new solutions used to generate all the heat transfer coefficients again till the values converge. The convergence criteria are given the following relationship:

$$\text{Sup} \left[ \max_i \left| T_{xi}^{k+1} - T_{xi}^k \right|, \left| T_c^{k+1} - T_c^k \right|, \left| T_p^{k+1} - T_p^k \right| \right] \leq \gamma \quad (20)$$

An appropriate choice of the  $\gamma$  is important to make sure that the convergence is rich. Several tests have been made for which,  $\gamma$  tacked  $10^{-3}$ ,  $10^{-4}$  and  $10^{-5}$ , the results values and numbers of iterations were compared. The results showed that for the low value of flux ( $I(t) < 270 \text{ W/m}^2$ ), the value  $\gamma = 10^{-3}$  was satisfactory while, for the higher values of flux  $I(t)$ ,  $\gamma \sim 8 \cdot 10^{-4}$  was adequate. The value of  $\gamma$  was kept constant,  $10^{-5}$ , throughout the present calculations. The computer program is based on FORTRAN and proceeds as outlined above.

#### **4- Physical parameters**

One collector panel with CPC collectors truncated to one-third of the full size within the acceptance half-angle of  $15^\circ$  is considered. The collector has a total aperture area of  $0.72 \text{ m}^2$  and a flat plate absorber area of  $0.24 \text{ m}^2$ . This collector has overall dimensions  $0.6 \text{ m}$  height,  $0.6 \text{ m}$  width,  $8 \text{ mm}$  gap thickness and the calculations are done for three values of CPC length,  $L$ , from  $1.2$  to  $2 \text{ m}$ . The receiving surface, which is painted non-selective matt black, forms the upper side of a rectangular airflow duct of depth  $0.03 \text{ m}$  made of aluminium sheet  $0.2 \text{ mm}$  thick (Pramuang and Exell 2005). The bottom of the duct is insulated with fibre glass  $0.05 \text{ m}$  thick. The optical properties of the materials in the collector are listed in table 1. The physical properties of air were assumed to vary linearly with temperature within the range encountered in solar air heaters. Therefore, typical linear equations for the viscosity, density, thermal conductivity, and specific heat of air were implemented in the theoretical procedure. The following are recalled in the Appendix. The mean values of the ambient temperature and global radiation in May at Garoua in Cameroon ( $9^\circ 20' \text{ N}$ ;  $13^\circ 23' \text{ E}$ ; altitude  $241 \text{ m}$ ) are used (Tchinda et al. 2004).

#### **5- Results and discussion**

A series of runs with individual parameters varied while others, held constant, were conducted and analysed to investigate the influence of these parameters on the thermal performance of the present model. The effect of increasing the volume flow rate on the local air, the air outlet, the absorber plate and the cover temperatures and the instantaneous and daily average efficiencies is presented in figures 2 to 5. It is apparent, as expected, that as the air mass flow rate increases the air flow local temperature and air outlet temperature decreases. Further, for high mass flow rates the collector operating temperature would be lower, resulting in lower heat losses and, subsequently, higher efficiencies. In all the results, it observed is that the absorber plate exhibits the highest temperature, and the cover the

lowest. As air flow rate increases, the temperature differences between the air and the absorber plate decrease. The effects of wind on the instantaneous and daily efficiencies are shown in figure 4-a and b. The results show that by decreasing the value of the wind speed, as expected, the wind heat transfer coefficient decreases, and thus the overall loss coefficient value, instantaneous and daily efficiencies increased.

The effect of increasing the collector length on the thermal performance is displayed in figures 2-a and 5. It can be seen that as the collector length is increased the absorber average temperature is appreciably increased as was the air temperature. However, the instantaneous and daily average efficiencies slightly decrease with the increase in length of the collector, which presumably results from the greater heat losses to the surroundings since both the average absorber temperature and size of the collector are increased. Figure 6 shows the instantaneous efficiency calculated for different solar irradiances.

Figure 7 shows the effect of the air mass flow rate on  $U_L$  and  $F'$ . It is shown that the collector efficiency factor  $F'$  increases with the air mass flow rate. It is also observed, as expected, that  $U_L$  decreases with the increase of the air mass flow rate.

Figure 8 compares the efficiency obtained from the present mathematical model and experimental data of Pramuang and Exell (2005). The test data have been taken from a collector having conditions sufficiently close to those given by Pramuang and Exell (2005). It can be seen that the results obtained show a good agreement with experimental data, with an average error of 8%.

## **6- Conclusion**

The heat transfer characteristics and thermal performance of a solar flat plate collector with a CPC has been presented. A theoretical solution procedure of the energy equations using a computer code for predicting the thermal performance of the present solar air heater has been made. The influence of the air mass flow rate, collector length and wind speed on the performance of the present air heater has been discussed. Reasonable agreement is obtained from the comparison between the numerical results and experimental data.



## Appendix

The different heat transfer coefficients for each surface in the present system are evaluated as follows.

### *Radiation heat transfer from the cover to the Sky*

The radiative  $h_{Rp}$  heat transfer coefficient between the flat plate absorber and the cover is:

$$h_{Rp} = \frac{\sigma(T_p^2 + T_c^2)(T_p + T_c)}{\frac{1}{\varepsilon_p} + \frac{A_p}{A_c} \left( \frac{1}{\varepsilon_c} - 1 \right)} \quad (\text{A1})$$

### *Radiation heat transfer from the flat plate absorber to the cover*

The radiative heat loss coefficient  $h_{Rs}$  between cover and the sky is calculated from the relationship:

$$h_{Rs} = \sigma \varepsilon_c (T_c^2 + T_s^2)(T_c + T_s) \frac{A_c}{A_p} \quad (\text{A2-a})$$

where the expression of the sky temperature is given by (Hsieh 1979, Hsieh 1981, Tchinda et al. 1998):

$$T_s = T_b - 6 \quad (\text{A2-b})$$

### *Convection heat transfer coefficient from the cover due to wind*

The heat loss coefficient by convection  $h_{c/a}$  between cover and the ambient is correlated by Duffie and Beckman (1974) as:

$$h_{c/a} = (5.7 + 3.8 v) \frac{A_c}{A_p} \quad (\text{A3-a})$$

or by Watmuff et al. (1977) as:

$$h_{c/a} = (2.8 + 3.3 v) \frac{A_c}{A_p} \quad (\text{A3-b})$$

where  $v$  is the wind velocity. The Duffie and Beckman correlation was the one that was employed in this study.

### *Convective heat transfer coefficient between flat plate absorber and cover*

According to the Hsieh theory (Hsieh 1981, Tchinda 2003) the convective  $h_{p/c}$  heat transfer between the flat plate absorber and the cover is:

$$h_{p/c} = (3.25 + 0.0085 \frac{T_p - T_c}{2 D_H}) \frac{A_c}{A_p} \quad (\text{A4-a})$$

$$\text{where } D_H = \frac{2 l_p e_f}{l_p + e_f} \quad (\text{A4-b})$$

The flow is assumed to be hydrodynamically fully developed at the collector inlet. The inner surface convective heat transfer coefficients were modelled according to the flow regime.

- For laminar flow ( $Re < 2100$ ) by Mercer correlation (Mercer et al. 1967, Brodkey and Hershey 1988)

$$N_u = 4.9 + \frac{0.0606 (Re Pr D_H / L)^{1.2}}{1 + 0.0909 (Re Pr D_H / L)^{0.7} Pr^{0.17}} \quad (\text{A-4})$$

- For turbulent flow ( $Re > 2100$ ) by the Kays correlation presented in a mathematical form by Duffie and Beckman (1980)

$$N_u = 0.0158 Re^{0.8} \quad (\text{A-5})$$

$$\text{With } Re = \frac{\dot{m} D_H}{l_p e_f \mu_f}, \quad Pr = \frac{\mu_f C_f}{\lambda_f} \quad (\text{A-6})$$

*Physical properties of air (Ong 1995)*

$$\text{Viscosity: } \mu = [1.983 + 0.00184(T-27)]10^{-5} \quad (\text{A-7})$$

$$\text{Density: } \rho = 1.1774 - 0.00359(T-27) \quad (\text{A-8})$$

$$\text{Thermal Conductivity: } \lambda = 0.02624 + 0.0000758(T-27) \quad (\text{A-9})$$

$$\text{Specific heat: } C_p = 1.0057 + 0.000066(T-27) \quad (\text{A-10})$$

### Acknowledgments

This work was done within the framework of the Associateship Scheme of the Abdus Salam International Centre for Theoretical Physics, Trieste, Italy. Financial support from the Swedish International Development Cooperation Agency is acknowledged.

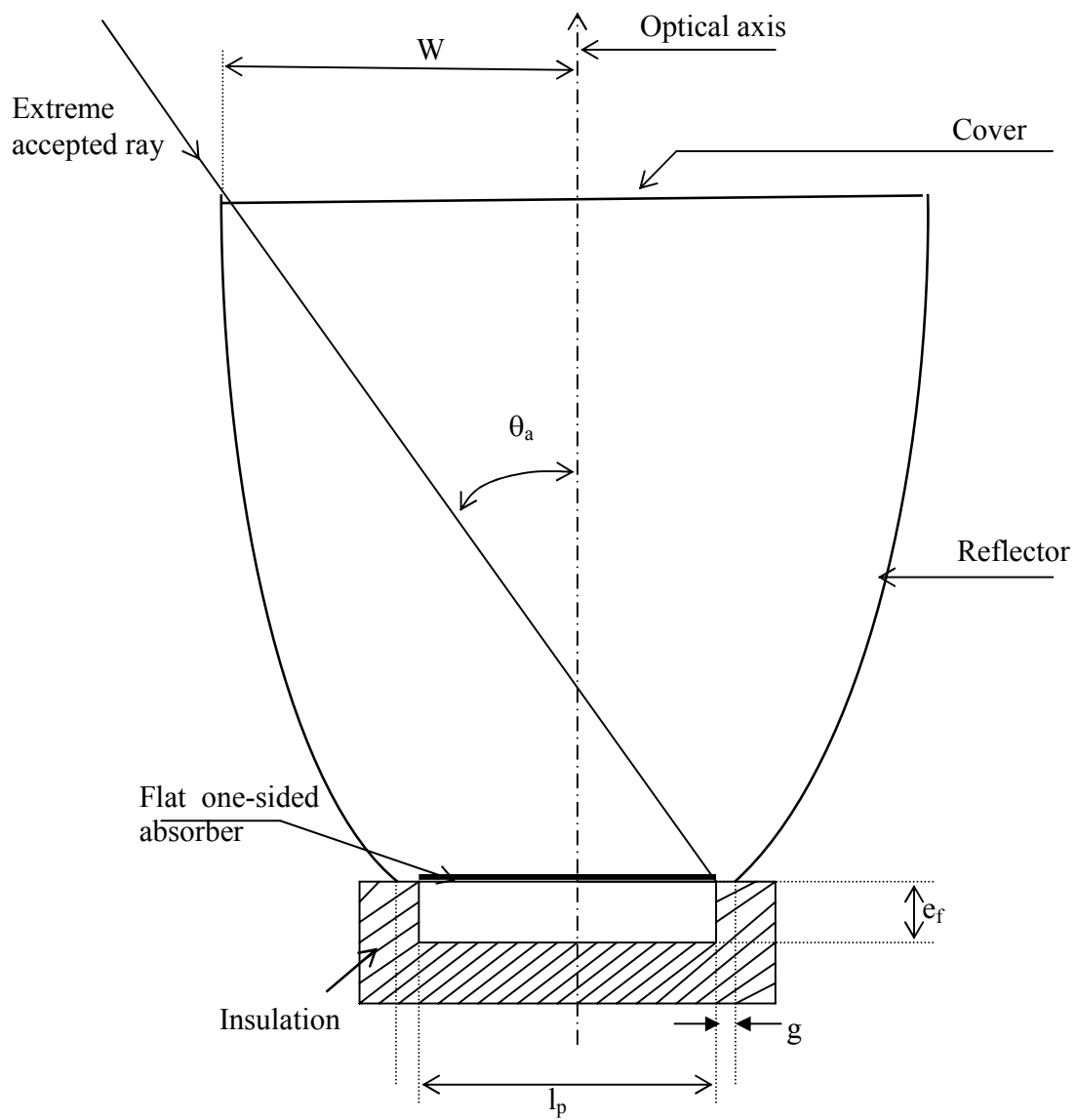
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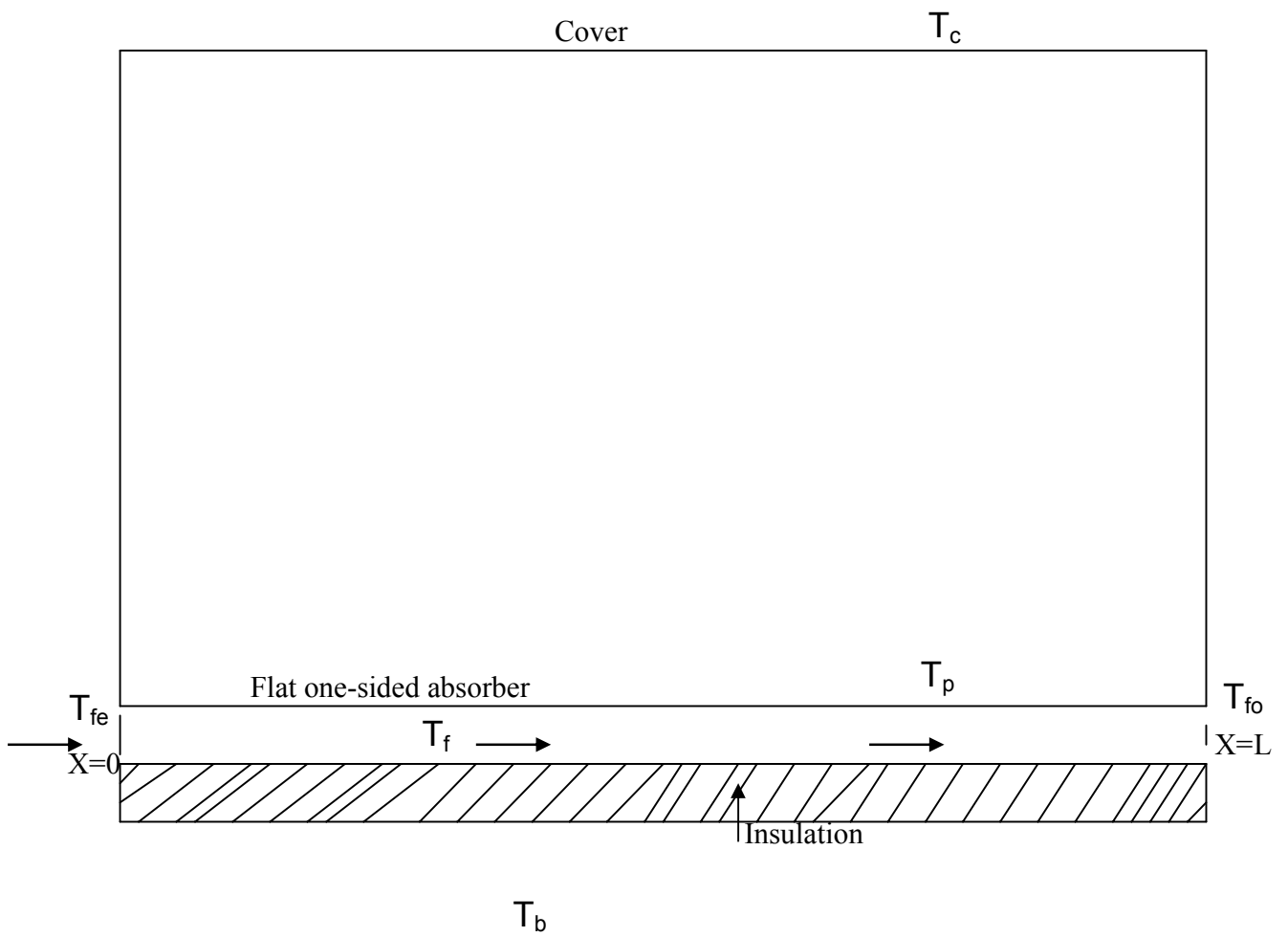
**Table 1:** The characteristics of the CPCs

Parameter	Symbol	Units	Value
Acceptance half angle	$\theta_a$	°	15
Cover absorptance	$\bar{\alpha}_c$		0.05
Flat plate absorber absorptance	$\bar{\alpha}_p$		0.95
Cover transmittance	$\bar{\tau}_c$		0.89
Cover emittance	$\varepsilon_c$		0.85
Flat plate absorber emittance	$\varepsilon_p$		0.91
Cover reflectance	$\bar{\rho}_c$		0.05
Reflector reflectance	$\rho_m$		0.86
Flat plate absorber reflectance	$\bar{\rho}_p$		0.15

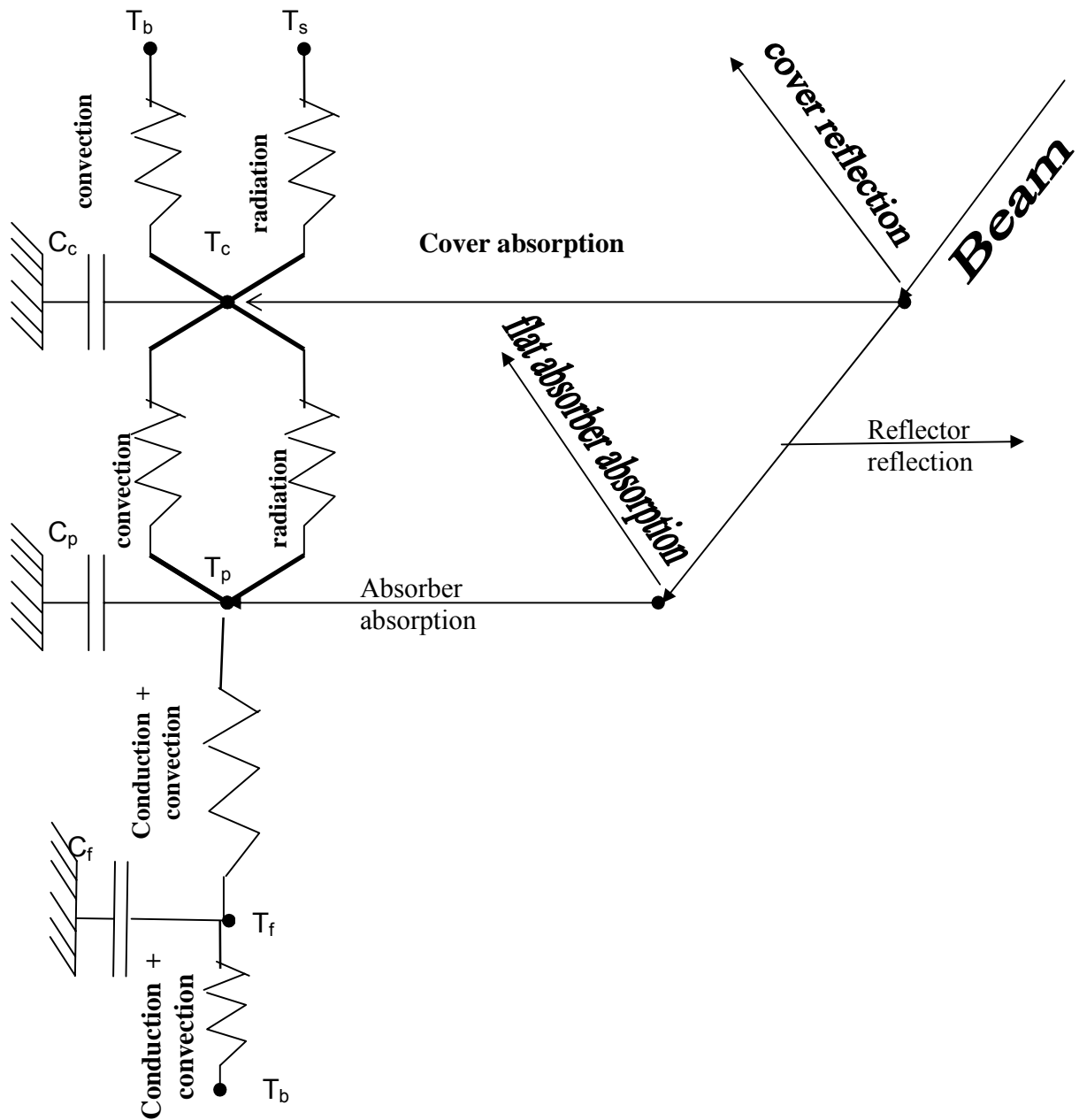


**Figure 1:** A two-dimensional CPC with a flat one-sided absorber

**a-** Cross section



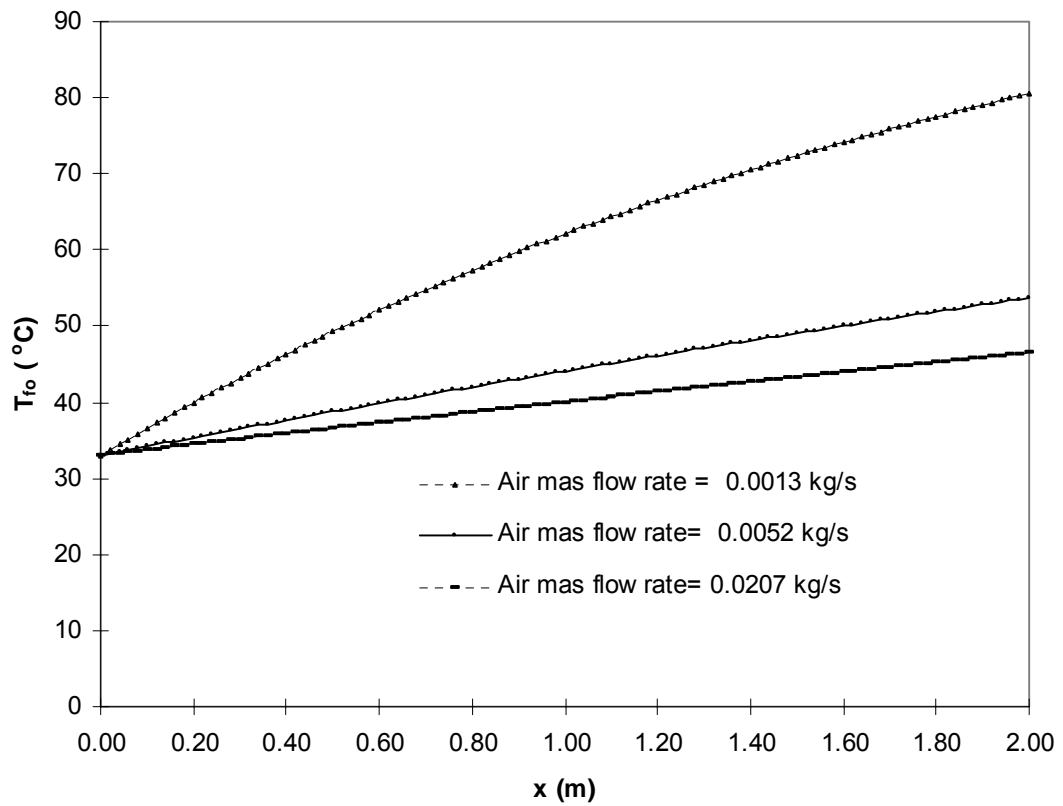
**Figure 1:** A two-dimensional CPC with a flat one-sided absorber  
**b-** Side view



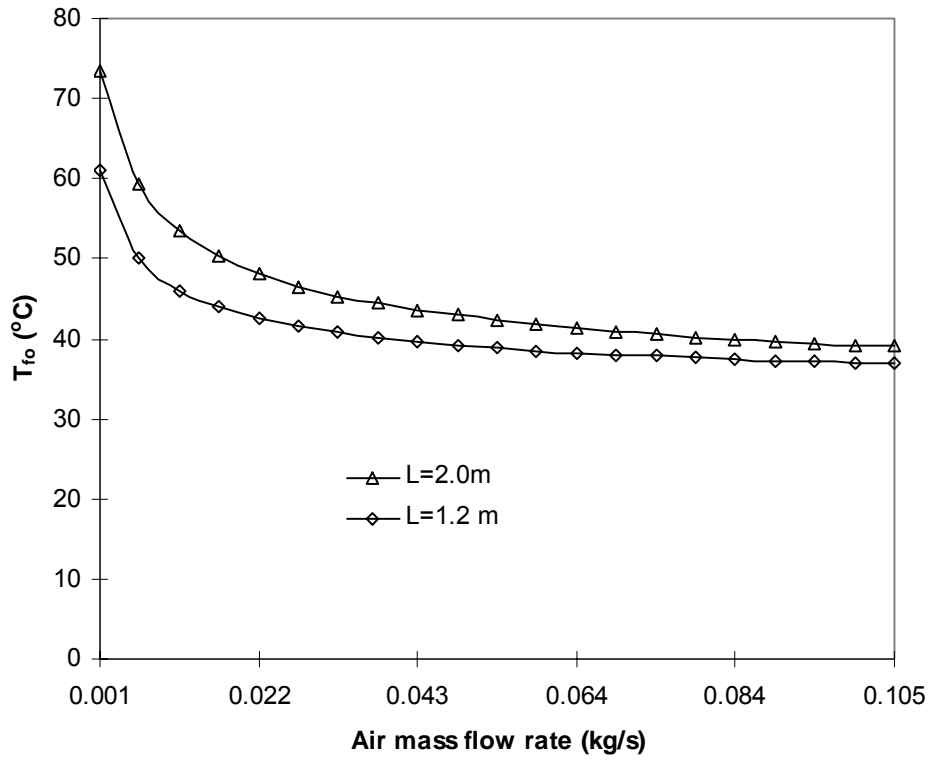
**Figure 1:** A two-dimensional CPC with a flat one-sided absorber

**c:** Electric analogy circuit

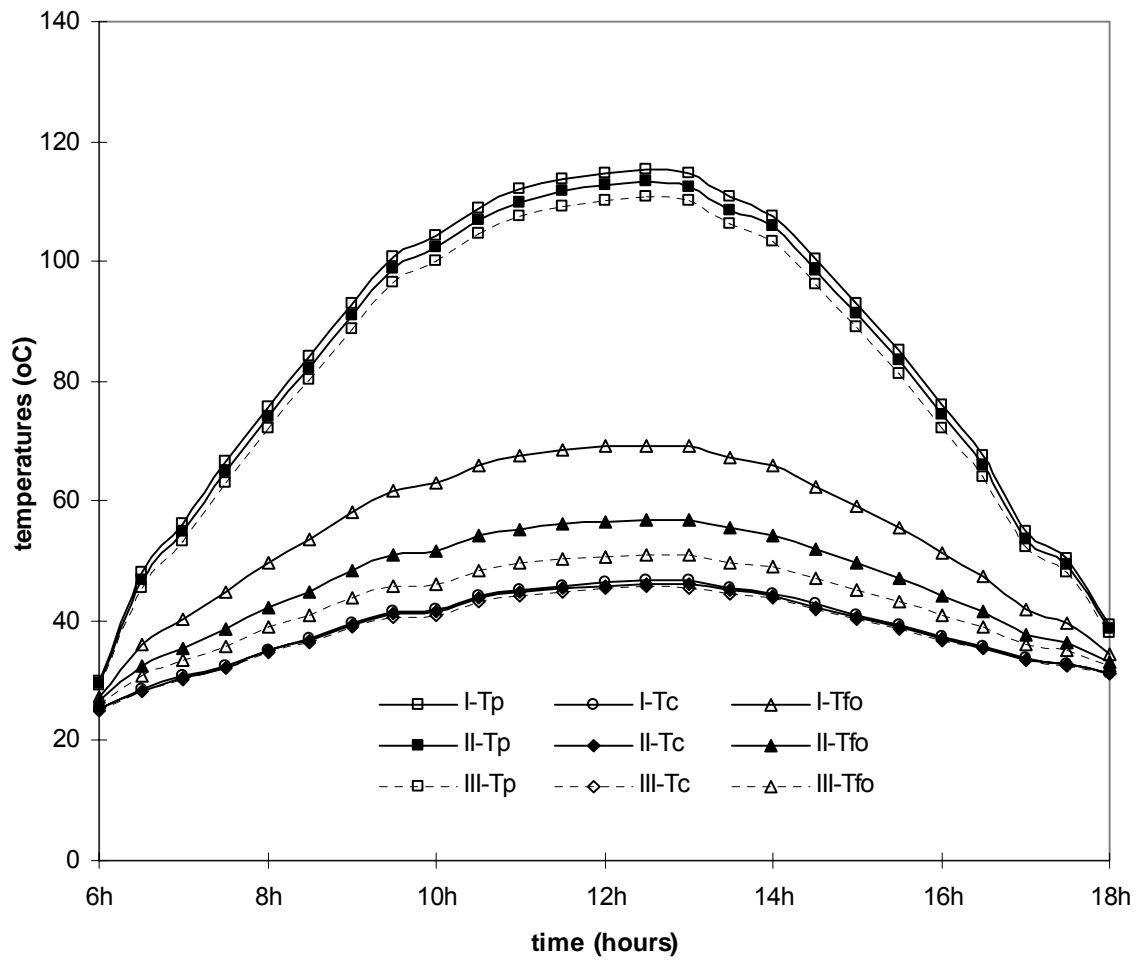




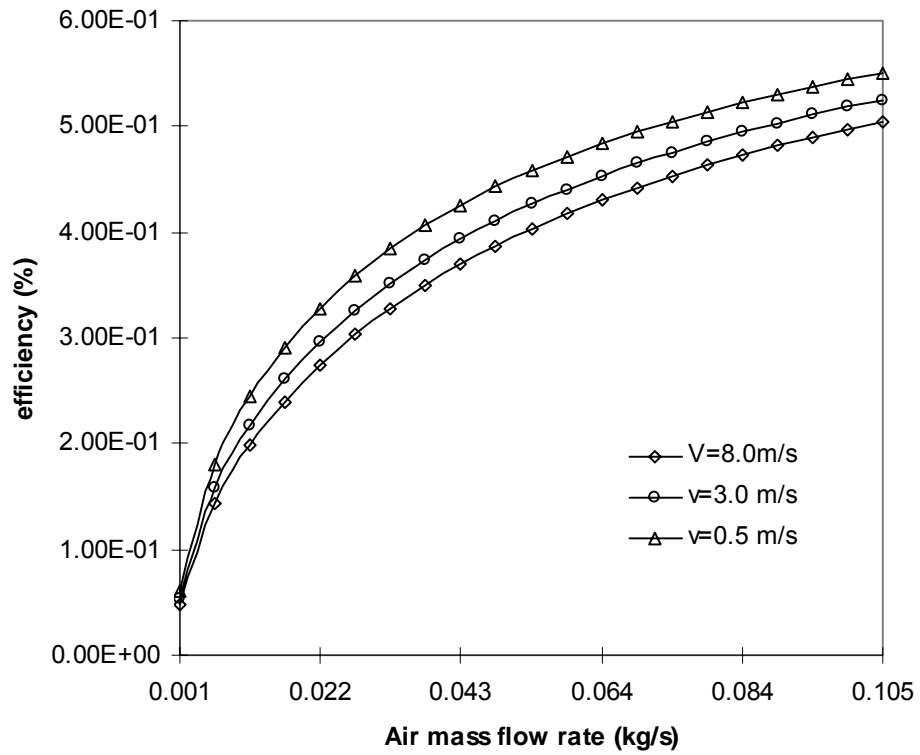
**Figure 2-a:** Effect of the air mass flow rate on the local temperature in the flow direction;  $L=1.2\text{m}$ ,  $T_{fe}=33^{\circ}\text{C}$ ,  $v=3.0\text{ m/s}$



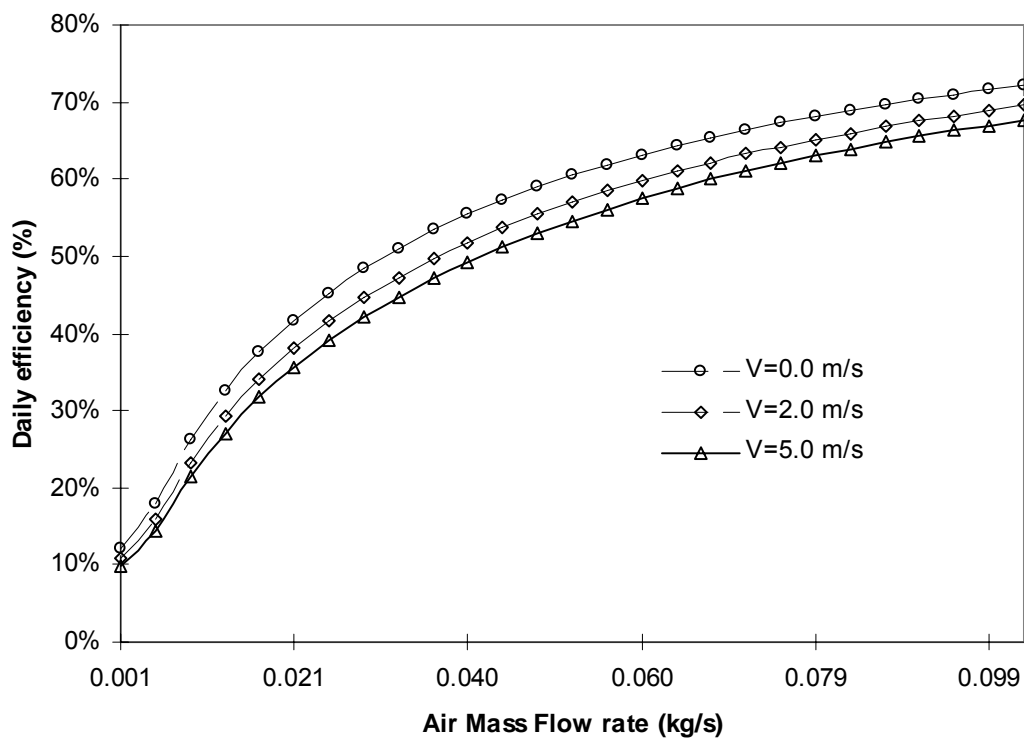
**Figure 2-b:** The outlet air temperature at  $t_M=12.30\text{p.m.}$  as a function of the mass flow rate for some values of  $L$



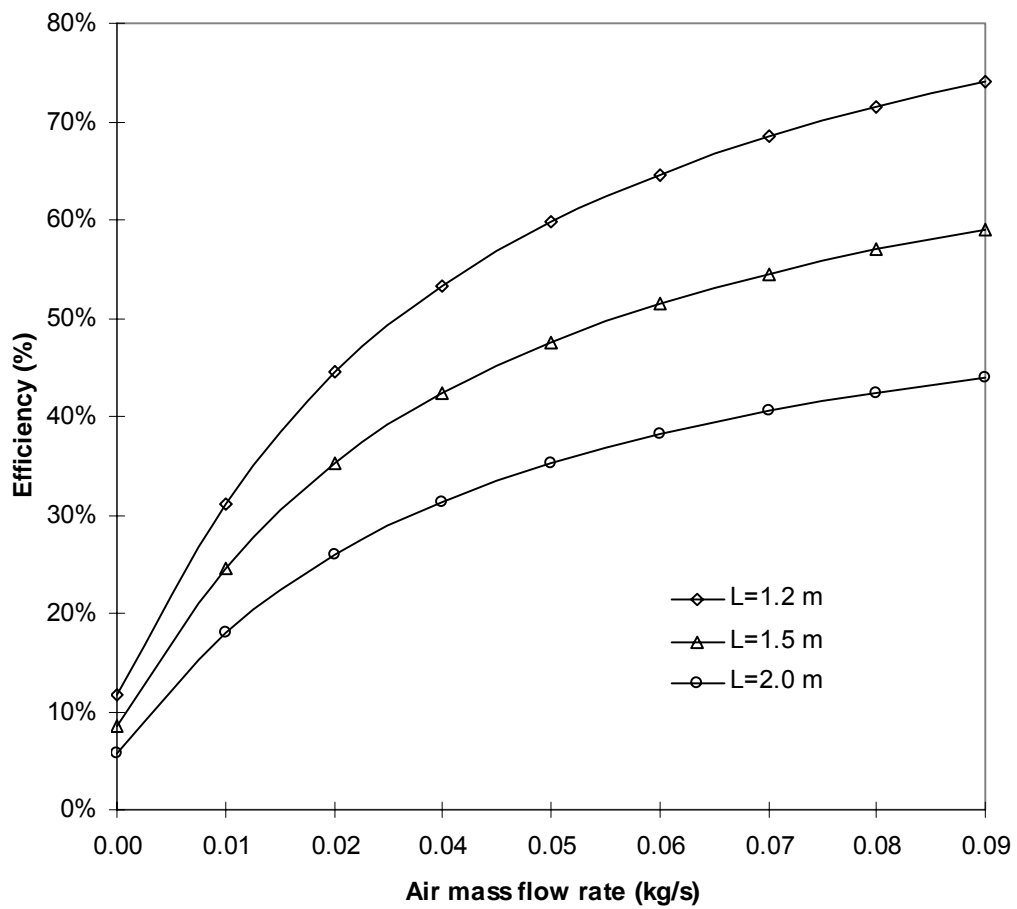
**Figure 3:** Effect of the air mass flow rate on the hourly variations of temperatures of the collector, I- air mass flow rate=0.0013 kg/s; II- air mass flow rate=0.0065g/s; III- air mass flow rate=0.013 kg/s, L=2.0m



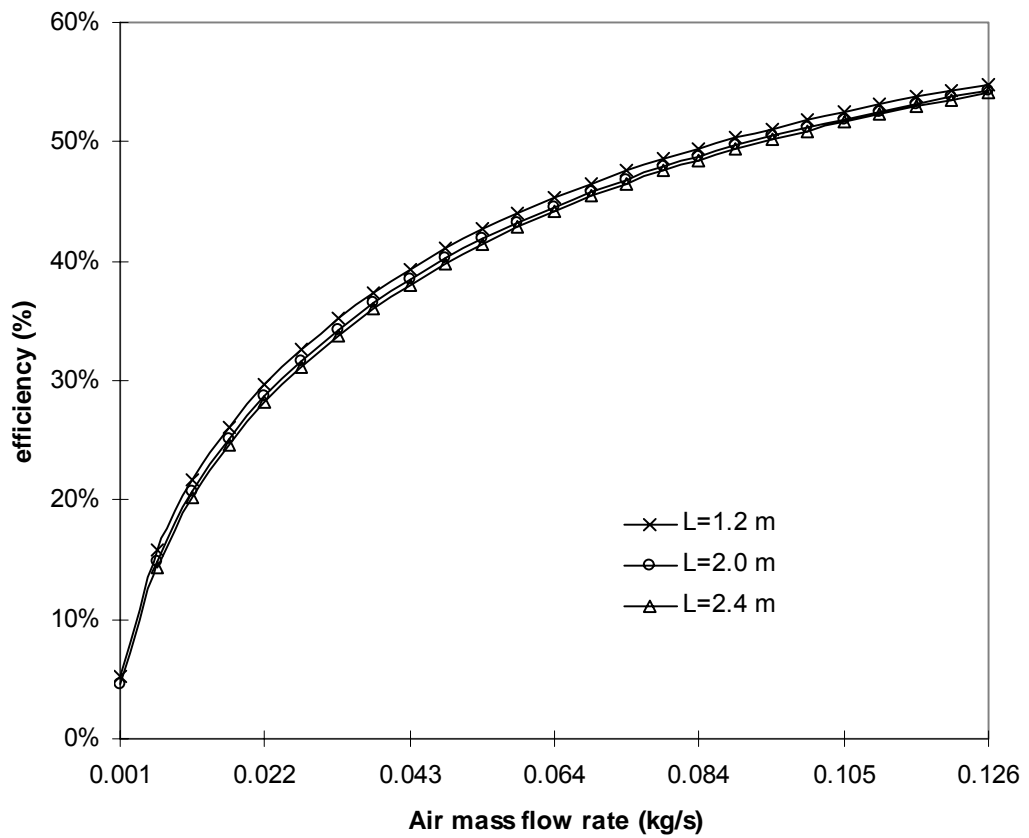
**Figure 4-a:** Graph of the instantaneous efficiency numerical results for tree wind speeds



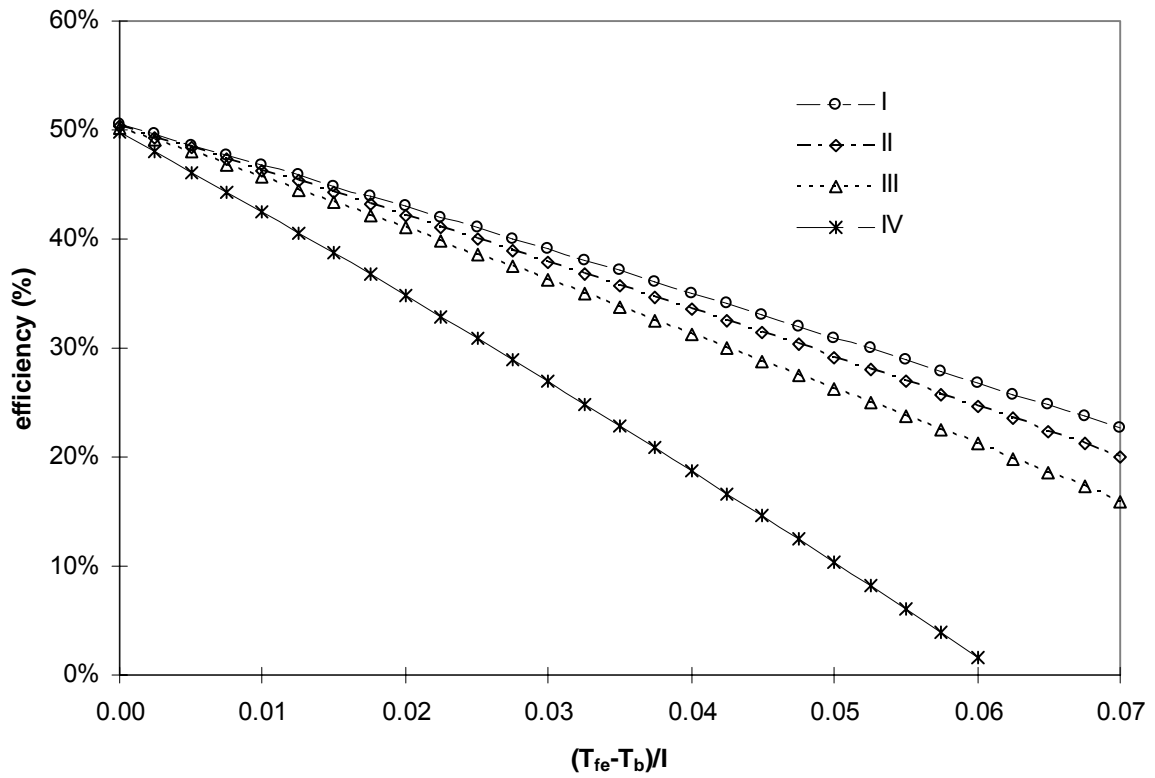
**Figure 4-b:** Effect of the air mass flow rate on the daily efficiency for tree values of wind speed,  $L=1.2$  m,  $T_{fe}=33^{\circ}\text{C}$



**Figure 5-a :** Effect of the air mass flow rate on the daily efficiency of the collector for three values of L

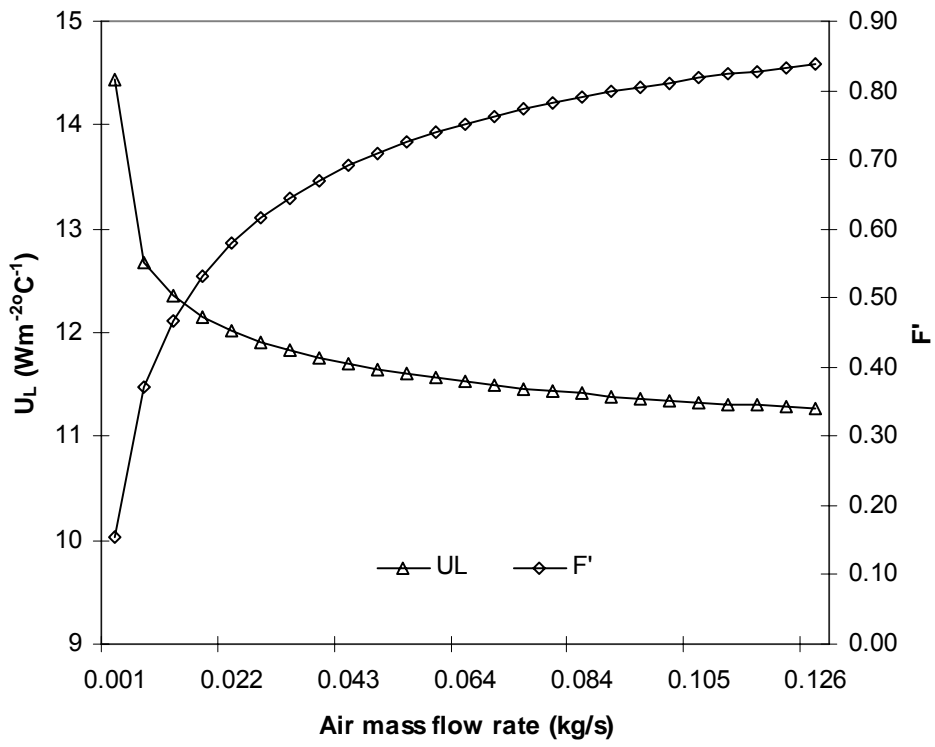


**Figure 5-b:** Effect of the air mass flow rate and collector length on the instantaneous efficiency at  $t_M=12.30$ p.m.

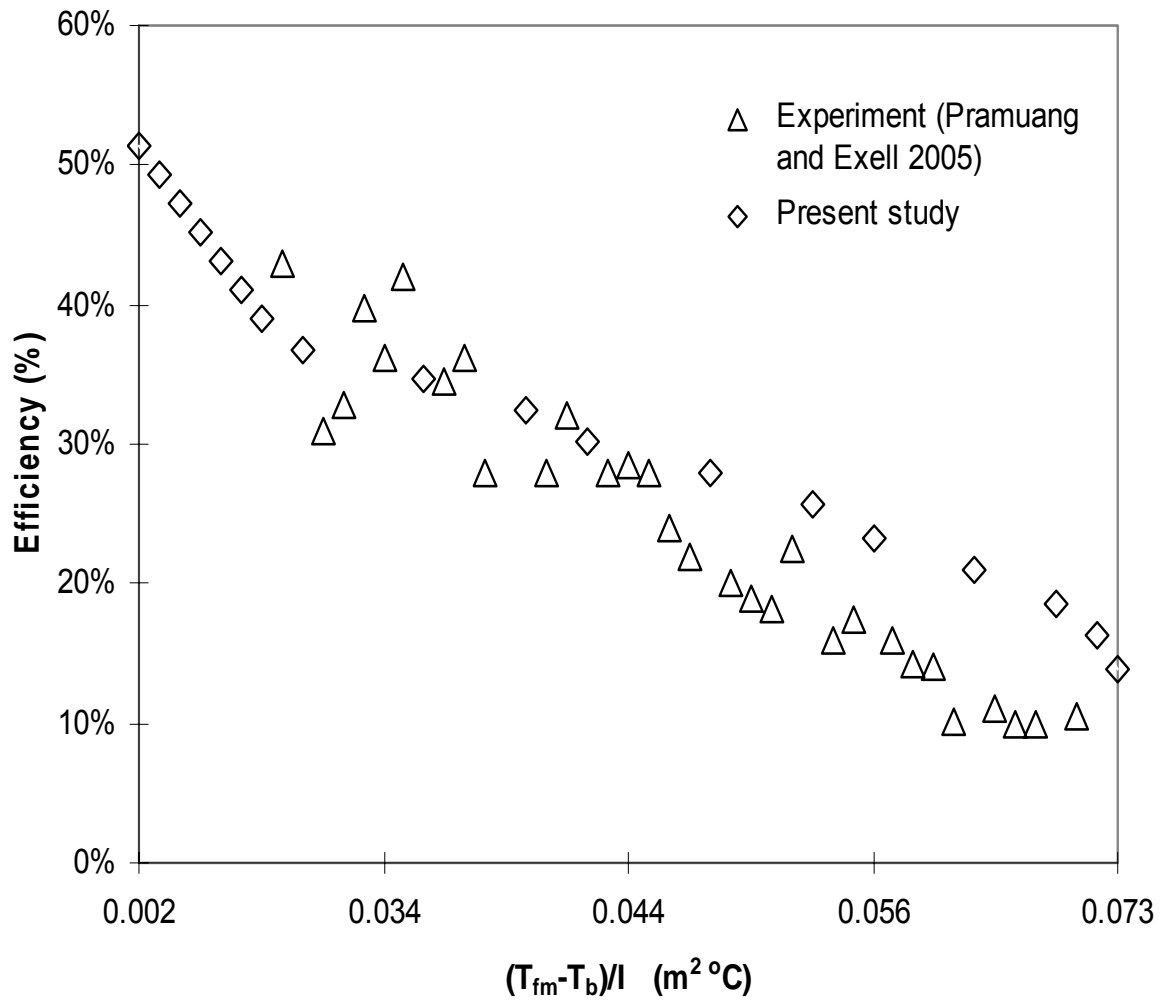


**Figure 6:** Collector efficiency curves calculated for four values of global radiation: I- I~951 W/m<sup>2</sup>; II- I~815 W/m<sup>2</sup>; III- I~636 W/m<sup>2</sup>; IV- I~327 W/m<sup>2</sup>; v=3,0 m/s, air mass flow rate~0.09 kg/s





**Figure 7:** Effect of the air mass flow rate and collector length on  $F'$  and  $U_L$



**Figure 8:** Comparison of the Collector efficiencies