

Scattering of W and Z Bosons at High-Energy Lepton Colliders

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ABSTRACT

We present a new study of quasi-elastic W and Z scattering processes in high-energy e^+e^- collisions, based on and extrapolating the low-energy effective theory which extends the Standard Model with a 125 GeV Higgs boson. Besides parameterizing deviations in terms of the dimension-8 operators that arise in the effective theory, we also study simplified models of new physics in W/Z scattering in terms of scalar and tensor resonance multiplets. The high-energy asymptotics of all models is regulated by a universal unitarization procedure. This enables us to provide benchmark scenarios which can be meaningfully evaluated off-shell and in exclusive event samples, and to determine the sensitivity of an e^+e^- collider to the model parameters. We analyze the longitudinal vector boson scattering modes, where we optimize the cuts for the fiducial cross section for different collider scenarios. Here, we choose energy stages of 1.0, 1.4 and 3 TeV, as motivated by the extendability of the ILC project and the staging scenario of the CLIC project.

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1 Introduction

Quasi-elastic scattering processes of the massive electroweak bosons W^\pm, Z (vector-boson scattering, VBS) are a cornerstone in the phenomenology of electroweak interactions. The longitudinal polarization components of on-shell energetic W and Z particles are closely related to the unobservable Goldstone bosons that constitute the elementary Higgs doublet together with the physical Higgs boson [1,2]. Their interactions thus probe the mechanism of electroweak symmetry breaking.

If the Higgs was missing from the particle spectrum, the W/Z interaction strength would rise with energy into a non-perturbative regime, indicating an intrinsic cutoff of the effective theory and new strong interactions [3,4]. However, the recent discovery of a 125 GeV Higgs boson implies that this is not the case. The existence of the Higgs boson allows all VBS interactions to remain weak asymptotically, calculable in electroweak perturbation theory. For the necessary cancellation of terms to take effect to all orders, the vector-boson, Higgs and Goldstone couplings must coincide exactly with their Standard Model (SM) values [5].

Without sufficient experimental data, we cannot decide whether the pure SM is the correct description of the electroweak symmetry-breaking sector. Beyond the SM, processes that involve Higgs and Goldstone fields could rather open a new portal to phenomena and structures that do not couple directly to matter particles, and are thus detached from immediate experimental access. New physics in the Higgs-Goldstone sector could have only a tiny impact on low-energy precision observables and is therefore largely unconstrained by existing data. Collider experiments will have to search for new effects in this area and complete our knowledge about the particle and interaction spectrum at accessible energies.

VBS processes have been observed at the Large Hadron Collider (LHC) in Run I [6,7,8], and the analysis of future LHC runs at full energy and increased luminosity will considerably improve our knowledge in this sector. At hadron colliders, VBS is accessible in processes of the type $pp \rightarrow q^*q^* \rightarrow qq + VV$, where q indicates any light quark, and $V = W, Z$. The analysis has been demonstrated to be feasible, but nevertheless suffers from limitations that do not simply disappear with increasing collider luminosity or energy. Leptonic decays of vector bosons either yield incomplete kinematic information (W) or a low branching ratio (Z). Hadronic decays are difficult to isolate from a large QCD background. VBS processes must be separated from vector-boson pair production, $q\bar{q}' \rightarrow VV$, QCD production of VV and two jets, as well as top-quark production as SM background. The initial state, i.e., the flavor and energy of the initial quarks, cannot be controlled or detected, and steeply falling parton structure functions limit the accessible energy for the elementary VBS interaction.

By contrast, e^+e^- colliders provide a clean environment where the VBS process class has a unique signature, and most decays of W and Z bosons are accessible and can be observed with high efficiency and purity [9,10]. The initial state is known exactly, and the e^+e^- c.m. energy is fixed up to minor electromagnetic radiation effects. We expect more detailed and complementary information to be available from e^+e^- collisions compared to hadronic collisions. The decisive factor for an e^+e^- collider is the availability of sufficient energy combined with high luminosity.

The complete list of e^+e^- VBS processes accessible at an e^+e^- collider with sufficient energy reads

$$e^+e^- \rightarrow \bar{\nu}_e\nu_e W^+W^-, \quad (1)$$

$$\bar{\nu}_e\nu_e ZZ, \quad (2)$$

$$\bar{\nu}_ee^-W^+Z, \quad (3)$$

$$e^+\nu_e ZW^-, \quad (4)$$

$$e^+e^-W^+W^-, \quad (5)$$

$$e^+e^-ZZ. \quad (6)$$

with various decay channels of the final-state bosons. These processes allow us to study interactions of W and Z bosons in the following elementary scattering channels, which are realized as distinct, approximately on-shell factorized contributions to the amplitudes:

$$W^+W^- \rightarrow W^+W^-, \quad (7)$$

$$W^+W^- \rightarrow ZZ, \quad (8)$$

$$W^\pm Z \rightarrow W^\pm Z, \quad (9)$$

$$ZZ \rightarrow W^+W^-, \quad (10)$$

$$ZZ \rightarrow ZZ. \quad (11)$$

By kinematics alone, the threshold for these processes is just above the vector-boson pair production threshold of 160...180 GeV, but for a meaningful analysis of deviations from the SM, a significantly larger vector-boson pair energy (i.e., invariant mass of the VV system) is necessary.

The prospects for the measurement of VBS processes at lepton colliders, including potential non-SM contributions, have been studied extensively in the literature [11,12,13,14,15,16,17,18,19,20]. However, most previous studies have investigated no-Higgs (or heavy-Higgs) scenarios, occasionally in comparison to the pure SM with a light Higgs of some arbitrarily assumed mass. Since a Higgs-like boson has been found, its mass has been precisely determined, and the measurement of its couplings is in accordance with the pure SM prediction, Higgs-less models do no longer provide a viable scenario for electroweak interactions. The analysis of VBS should rather be based on models that reduce to the SM with a 125 GeV Higgs at low energy and take into account all recently accumulated knowledge about the Higgs boson.¹

In this paper, we therefore present a new study of VBS processes at an e^+e^- lepton collider. We take the SM with a Higgs mass of 125 GeV as reference and determine the sensitivity to effects beyond the SM in VBS interactions. Given the exploratory nature of this task and the emergence of strong-interaction effects, we can restrict our calculation to leading order in the SM and EFT predictions. Actual data analysis should incorporate NLO corrections in the SM and its EFT extension, cf. [22,23,24], which eventually should become available for the complete six-fermion partonic processes. For a meaningful extrapolation to energy and parameter ranges where partial-wave unitarity becomes an issue, we apply a universal unitarization method, the T-matrix framework. The concrete results are computed for specific values of the collider energy, $\sqrt{s} = 1.4$ TeV and 3.0 TeV with integrated luminosities of $\mathcal{L}_{int} = 1.5 \text{ ab}^{-1}$ and 2 ab^{-1} , as planned for the Compact Linear Collider (CLIC) [25,26,27]. Furthermore, we make use of specific properties of the CLIC collider environment in its currently planned state, including the most relevant detector properties, to estimate the sensitivity on anomalous effects beyond the SM. For completeness, we also include numbers for a lower collider energy of 1 TeV with an integrated luminosity of $\mathcal{L}_{int} = 5 \text{ ab}^{-1}$, which should also illuminate the potential of an energy upgrade of the International Linear Collider (ILC) [28,29].

2 Effective Field Theory and Vector Boson Scattering

The theoretical basis for the current study is the SM with a single complex Higgs doublet. Since we want to provide not just the unique SM prediction but a range of possibilities for the high-energy behavior of electroweak interactions, we have to regard the SM as an effective field theory (EFT). I.e., we assume an infinite series of interactions, organized by operator dimension [30,31,32]. The pure SM limit consists of setting the couplings of all operators with dimension greater than four to zero, or alternatively, letting the intrinsic mass scale of those dimensionful couplings to infinity.

Within the EFT formalism, we assume that the strong-electroweak $SU(3)_{QCD} \times SU(2)_L \times U(1)_Y$ gauge symmetry of the SM Lagrangian is a fundamental property, and therefore organize all higher-dimensional operators in terms of gauge-invariant polynomials. This implies global strong-electroweak invariance for all terms and promoting partial derivatives to covariant derivatives where required by the field representation. We do not consider CP symmetry

¹Turning this around, VBS at high energy can be utilized to supply indirect information on Higgs boson properties [21].

breaking effects (beyond those already present in the SM) in the current study.

The SM Higgs, in the gauge-invariant Lagrangian, appears as a complex doublet which transforms linearly under $SU(2)_L \times U(1)_Y$.² If we neglect the interactions of heavy SM fermions, the global symmetry is approximately $SU(2)_L \times SU(2)_R$ [34,35]. This symmetry is explicitly broken by the hypercharge gauge coupling. The obstruction can be controlled as a spurion, and the analysis can be based on an exactly $SU(2)_L \times SU(2)_R$ symmetric Lagrangian. This is a reasonable simplification since we are interested in the high-energy range of VBS processes where gauge interactions play a minor role, i.e., can be viewed as a perturbation entirely. The Higgs vacuum expectation value (vev) spontaneously breaks the global symmetry down to the diagonal $SU(2)_{L+R}$, known as the custodial symmetry $SU(2)_C$.

In this context, it is natural to represent the Higgs field multiplet as a 2×2 matrix [36,37],

$$\mathbf{H} = \frac{1}{2} \begin{pmatrix} v + h - iw^3 & -i\sqrt{2}w^+ \\ -i\sqrt{2}w^- & v + h + iw^3 \end{pmatrix} . \quad (12)$$

which transforms linearly under $U \in SU(2)_L$ and $V \in SU(2)_R$ as

$$\mathbf{H} \rightarrow U\mathbf{H}V^\dagger . \quad (13)$$

The covariant derivative of the Higgs matrix is given by

$$\mathbf{D}_\mu \mathbf{H} = \partial_\mu \mathbf{H} - ig \mathbf{W}_\mu \mathbf{H} + ig' \mathbf{H} \mathbf{B}_\mu \quad (14)$$

where

$$\mathbf{W}_\mu \equiv W_\mu^a \frac{\tau^a}{2}, \quad \mathbf{B}_\mu \equiv B_\mu \frac{\mathbf{T}}{2} \quad (15)$$

and \mathbf{T} is a $SU(2)_R$ -breaking spurion with ground state $\mathbf{T} = \tau^3$. Finally, we define the matrix-valued field strengths

$$\mathbf{W}^{\mu\nu} = \partial_\mu \mathbf{W}_\nu - \partial_\nu \mathbf{W}_\mu - ig [\mathbf{W}_\mu, \mathbf{W}_\nu], \quad \mathbf{B}^{\mu\nu} = \partial_\mu \mathbf{B}_\nu - \partial_\nu \mathbf{B}_\mu \quad (16)$$

and quote the bosonic part of the SM Lagrangian (omitting QCD),

$$\begin{aligned} \mathcal{L}_{SM} = & -\frac{1}{2} \text{tr} [\mathbf{W}_{\mu\nu} \mathbf{W}^{\mu\nu}] - \frac{1}{2} \text{tr} [\mathbf{B}_{\mu\nu} \mathbf{B}^{\mu\nu}] \\ & + \text{tr} [(\mathbf{D}_\mu \mathbf{H})^\dagger \mathbf{D}^\mu \mathbf{H}] + \mu^2 \text{tr} [\mathbf{H}^\dagger \mathbf{H}] - \frac{\lambda}{2} (\text{tr} [\mathbf{H}^\dagger \mathbf{H}])^2 . \end{aligned} \quad (17)$$

The power of an EFT series as a perturbative expansion lies in the accuracy of a truncation at low order. New mutual and self-interactions of bosons only take the form of gauge-invariant operators of even dimension. The leading non-SM order is thus dimension six, so it appears natural to truncate the EFT at this order. The complete set of dimension-six operators has been discussed extensively in the literature [38,39,40,41,42,43].

²A non-linear Higgs representation might be chosen to allow for more freedom in Higgs couplings that are not yet constrained with precision, but this property is of secondary importance in our study of VBS processes. It becomes more relevant when considering also Higgs final states, cf. [33].

However, new-physics effects in the Higgs-Goldstone sector, including new strong interactions, largely decouple from precision observables as they are accessible today. While several dimension-six operators in the EFT do affect VBS processes at tree level, they simultaneously modify other couplings which can be measured independently. Such operators are an inadequate representation of the specific new-physics scenarios that VBS is most sensitive to. In fact, for the purpose of studying VBS, we may assume that the coefficients of dimension-six operators are known to sufficient precision; we set them to zero as the standard reference point.

Traces of genuine new Higgs-Goldstone physics appear first in dimension-eight operators. These modify VBS interactions independently of other types of interaction. For instance, the exchange of massive resonances generically results in dimension-eight effective operators. Our study therefore includes the relevant dimension-eight operators.

It is evident that any truncation at this level, while technically consistent, is of questionable value. Amplitudes modified by dimension-eight operators rise rapidly with energy and thus yield large effects [37]. This fact also indicates the breakdown of the perturbative expansion. Our version of the EFT with dimension-eight operators is therefore not intended as an approximation that can be systematically improved. It rather serves as a phenomenological tool to describe dominant non-SM phenomena in VBS. At low energy, $O(100 \text{ GeV})$, it smoothly matches to the EFT within its range of validity. Extrapolated to high energy, it gives a flavor of the maximum impact that BSM can have on VBS. The extrapolation incorporates unitarity as the only damping mechanism and thus asymptotically approaches the unitarity bound for each partial-wave amplitude. However, additional structure can easily be included, as we will describe below using simplified models containing resonances.

3 Anomalous Interactions of Vector Bosons

The complete set of dimension-eight operators for the SM fields is rather large. In line with the above considerations, we resort to standard simplifications in order to make the set manageable. First of all, as stated before, we only consider bosonic operators. (That is, we treat fermionic currents as external probes for bosonic interactions, neglecting genuine fermionic anomalous contributions.) We furthermore assume the global $SU(2)_L \times SU(2)_R$ symmetry of the fermion- and gaugeless SM to hold also at higher orders. This introduces relations between W and Z scattering amplitudes and simplifies the scattering matrix for the purpose of unitary extrapolation.

Focusing on operators that directly modify quartic vector-boson interactions, there are three classes which affect Higgs/Goldstone bosons only (index: S), gauge bosons only (index: T), or both (index: M), respectively. We recall that, taking EWSB into account, Goldstone bosons are probed via the longitudinal polarization direction of energetic W and Z bosons, while gauge bosons translate into transversal polarization.

Operators involving only the Higgs/Goldstone bosons sector, i.e., S-type, are represented by a combination of covariant derivatives acting on the Higgs fields. Two linearly independent

operators can be identified

$$\mathcal{L}_{S,0} = F_{S,0} \operatorname{tr} \left[(\mathbf{D}_\mu \mathbf{H})^\dagger \mathbf{D}_\nu \mathbf{H} \right] \operatorname{tr} \left[(\mathbf{D}^\mu \mathbf{H})^\dagger \mathbf{D}^\nu \mathbf{H} \right], \quad (18a)$$

$$\mathcal{L}_{S,1} = F_{S,1} \operatorname{tr} \left[(\mathbf{D}_\mu \mathbf{H})^\dagger \mathbf{D}^\mu \mathbf{H} \right] \operatorname{tr} \left[(\mathbf{D}_\nu \mathbf{H})^\dagger \mathbf{D}^\nu \mathbf{H} \right]. \quad (18b)$$

In the present paper, we do not study the transversal and mixed interactions but defer this to future work. For completeness, we list the T and M -type operators in the Appendix. We also neglect operators which are proportional to $\mathbf{H}^\dagger \mathbf{H}$; as long as Higgs final states are not considered, this class of operators merely renormalizes the dimension-six part of the EFT Lagrangian.

We may compare this EFT framework with the corresponding expansion [44,45] and subsequent analysis for the no-Higgs (or heavy-Higgs) case, as it was investigated, for instance, in [16,17]. In the pure SM, a light Higgs boson and no higher-order operators, the amplitude for VBS remains perturbative at all energies. Beyond the SM, new physics that appears exclusively in the Higgs-Goldstone sector corresponds to dimension-eight operators as argued above, therefore any deviation from the SM increases rapidly with energy. Since the pure SM amplitude is small, interference plays a minor role and the phenomenologically relevant behavior originates from the dimension-eight interactions, squared. By contrast, if the light Higgs boson did not exist, the reference amplitude would grow with energy and render the interaction strong in the TeV range by itself, while anomalous effects would contribute first via their interference, which is a less striking modification of the reference amplitude. In this study, which is based on the now established light-Higgs scenario, we therefore will face a sudden transition from a weakly-interacting to a strongly-interacting regime when increasing the energy in the VBS process.

4 Unitary Extrapolation

The SM amplitudes for VBS, as for any other elementary process, are perturbative throughout the accessible energy range and therefore do not pose a unitarity problem. If anomalous effects are present which cannot simply be mapped to an extended renormalizable (weakly interacting) model, this property is lost, and we have to deal with unitarity violation in the tree-level prediction. Clearly, this indicates the breakdown of perturbation theory. On the other hand, the quantitative analysis of actual data relies on the availability of a prediction which depends on a suitable set of new parameters. Such a reference allows us to quantitatively study or exclude a deviation from the SM. In order to discard grossly unphysical parameterizations, we have to ensure that any such extrapolation is at least in accordance with unitarity, all assumed symmetries, and smoothly matches to the low-energy effective theory

In [37,46], based on earlier work in [47], we have described the T-matrix unitarization framework as a generic scheme that allows for a unitary extrapolation of any model without introducing arbitrary artefacts in the asymptotic regime. We adopt this framework for the current paper.

At the fundamental level of the complete scattering matrix $\mathbf{S} = 1 + i\mathbf{T}$ (T matrix), the unitarization framework relies on the formula

$$\mathbf{T}(\mathbf{T}_0) = \frac{1}{\text{Re}(\mathbf{T}_0^{-1}) - \frac{i}{2}\mathbf{1}}, \quad (19)$$

which transforms an arbitrary model of the scattering matrix \mathbf{T}_0 into a unitary model of the scattering matrix \mathbf{T} . In particular, the set of amplitudes is invariant under the transformation if it already respects unitarity. For the application of the formula, it is advantageous to diagonalize the scattering matrix first and apply unitarization to eigenamplitudes, since this amounts to a simple multiplication or subtraction. In the present context, this can be done most easily in the high-energy limit where the gauge sector decouples from the Higgs sector. Since unitarity is an issue only for high energies, such an approach is sufficient to remove all dangerous terms.

The method does not refer to any property of the original model which is encoded in \mathbf{T}_0 ; in particular, it does not assume a perturbative expansion or a particular analytical structure. While it reconciles any model \mathbf{T}_0 with unitarity, the result is not a unique prediction. It is merely a model that describes possible behavior of the amplitude up to the highest energies, as opposed to a unitarity-violating model or extrapolation that describes impossible behavior.

In practice, we identify the asymptotically leading terms in the diagonal scattering matrix, replace them by their unitary equivalents, and invert the diagonalization. Factoring out Lorentz tensors and subtracting the original EFT contribution, we cast this in the form of extra momentum-dependent Feynman rules. The new terms resemble the local Feynman rules that describe the original EFT operators, but they carry prefactors that depend on invariant momentum combinations in a non-analytical form. Nevertheless, for calculational purposes the new terms play a role analogous to the local counterterms that arise in a NLO calculation, and are straightforward to take into account in the construction and evaluation of scattering matrix elements. This allows us to perform off-shell calculations and evaluate the unitarized amplitudes for external fermions, as long as the kinematic assumptions underlying the procedure are satisfied.

For illustration, in plots below (Figs. 4, 5, 6) we display both the unitarized model behavior and the unphysical results that we would have obtained without unitarization. The latter are marked as dashed lines, while continuous curves refer to the respective unitary versions. While for some parameter sets, the unitarization correction remains a minor issue, there are various cases where unitarization has a large impact. This property clearly indicates that for CLIC energies, VBS processes are probed in a range where undetermined new-physics effects are actually important, and systematic approximations do no longer yield unambiguous results. Under no circumstances, calculation results without unitarization may be used for the analysis of actual data, as this would grossly overestimate the sensitivity on the model parameters.

5 Cut-Based Extraction of the VBS Signal

Based on the theoretical framework as described above, we now turn to the actual prospects for measuring vector-boson scattering processes at high effective energy at a high-energy lepton

collider, like e.g. the CLIC collider. The strategy of such an analysis does not depend strongly on the underlying physics model. We can therefore follow the ideas of [13,16,17] and adapt the analysis to the CLIC environment.

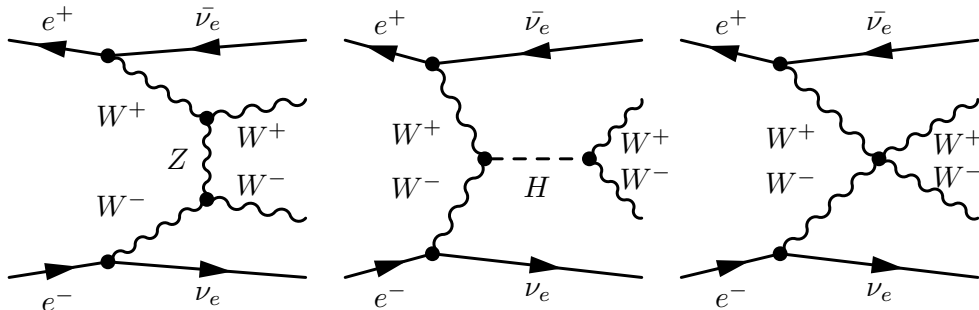


Figure 1: *Signal Feynman diagrams contributing to the VBS process.*

The main idea is to isolate a signal of vector-boson pairs in association with very forward neutrinos or electrons. This is the kinematic situation where in the diagrams of Fig. 1, the incoming vector bosons which participate in the VBS interaction have small invariant mass, so the amplitude is enhanced by the small denominator of the t-channel propagators. The nonvanishing mass of $V = W, Z$ bosons cuts off the approach to the actual particle pole, so the enhancement factor is of order m_V^2/E_V^2 in this kinematic range, and the typical recoil p_T of the radiating lepton becomes of order m_V . Graphs without the VBS interaction (Figs. 2, 3) do not benefit from this effect.

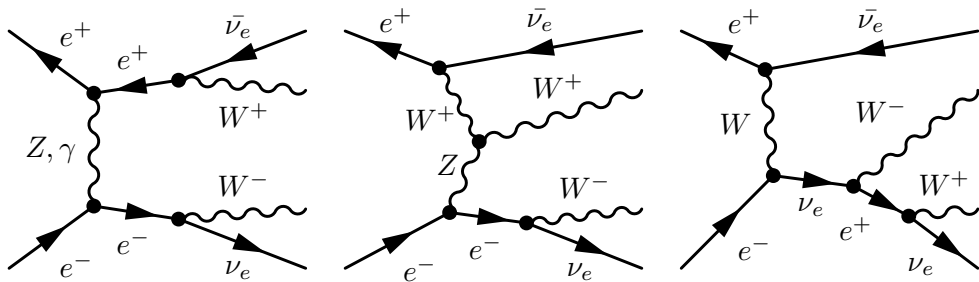


Figure 2: *Feynman diagrams contributing to the irreducible background.*

A large part of the total rate is due to W -boson pair production initiated by photons, cf. Fig. 3 (left). Photon-induced VBS processes are interesting by themselves, but photons do not have a longitudinal component and therefore do not receive contributions from new physics in the Higgs sector. For our purposes, the photon-induced contribution is therefore considered as a background. In contrast to the distribution of intermediate W/Z bosons, which is dominated by $Q \sim m_{W/Z}$, the distribution of photons extends down to nearly zero momentum transfer and is cut off only by the finite electron mass. Electrons in forward direction disappear in the beampipe and are thus indistinguishable from neutrinos, so in this kinematic range,

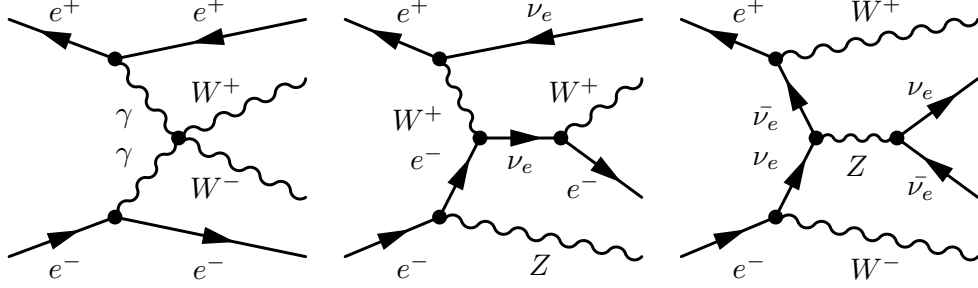


Figure 3: *Feynman diagrams contributing to the partially reducible background.*

intermediate photons cannot be separated by detecting the radiating fermion. Nevertheless, this background can be reduced without losing too much of the signal by vetoing against very forward electrons and simultaneously cutting on the p_T distribution of the vector-boson pair system.

We are interested in the vector-boson pair system at large combined invariant mass, as this is the energy value that enters the basic VBS interaction. Hence, we propose the following set of selection cuts, where the first number always refers to the 3.0 TeV CLIC staging, while the one in parentheses corresponds to the lower-energy staging at 1.4 TeV.

1. $M_{inv}(\bar{\nu}\nu) > 230(175)$ GeV. The signal process contains two neutrinos in the final state. This cut removes events where the neutrinos originate from Z decay; a majority of these neutrinos will have an invariant mass $M_{inv}(\bar{\nu}\nu) \sim 91$ GeV. Backgrounds from W^+W^- and QCD four-jet production are also removed by this cut.
2. $|\cos\theta(W/Z)| < 0.8$ and $p_{\perp}(W/Z) > 300(180)$ GeV. Events where the vector bosons have a small distance from the beam pipe or a small transverse momentum are cut away. This reduces backgrounds which result from t-channel exchange in the subprocess.
3. $\theta(e) > 15$ mrad and $p_{\perp}(WW) > 100(50)$ GeV, $p_{\perp}(ZZ) > 60(40)$ GeV. Together with a cut on the transverse momentum of the vector boson pair system, background resulting from $\gamma\gamma$ fusion will substantially be decreased.
4. $900(800)$ GeV $< M_{inv}(WW) < 1900(1175)$ GeV, $850(800)$ GeV $< M_{inv}(ZZ) < 1900(1175)$ GeV. The influence of the operators Eq. (18) increases with the invariant mass of the vector boson pair. We therefore only consider events within a small invariant mass range.

The following cuts are applied for the ILC staging scenario at 1.0 TeV:

1. $M_{inv}(\bar{\nu}\nu) > 150$ GeV.
2. $|\cos\theta(W/Z)| < 0.8$ and $p_{\perp}(W/Z) > 150$ GeV.
3. $\theta(e) > 15$ mrad and $p_{\perp}(WW) > 45$ GeV, $p_{\perp}(ZZ) > 40$ GeV.

4. $575 \text{ GeV} < M_{inv}(WW) < 800 \text{ GeV}$, $600 \text{ GeV} < M_{inv}(ZZ) < 800 \text{ GeV}$.

For the calculation, we have used the implementation of the SM in the WHIZARD Monte-Carlo generator [48,49]. The SM extensions that we consider in later sections are likewise handled by dedicated WHIZARD model implementations, taking into account unitarization corrections where necessary. The WHIZARD generator provides a physics simulation framework that can include beam properties (polarization, beamstrahlung and ISR), the complete partonic final state to leading and next-to-leading order QCD, parton shower, and hadronization, eventually complemented by detector-level tools and analysis methods [50,51,52,53].

For this exploratory study, we have largely restricted ourselves to on-shell W/Z bosons in the final state and concentrate on total cross section values after cuts. Polarization, ISR, and beamstrahlung are not taken into account for the tables below. Further below, we comment on possible improvements if polarization and details of the partonic final state are taken into account, using off-shell simulation for the latter. We expect that a future experimental study which can be performed using the WHIZARD generator in connection with detector simulation, jet algorithms, etc., should give more accurate results which we nevertheless expect to lie in the numerical range as our final results suggest. Clearly, especially ISR and beamstrahlung will lead to a distortion of distributions and to a depletion of events in the high-energy region, but we do not expect our results to fundamentally change. Our first estimates which should be backed up by future experimental studies confirmed that, and especially the number that roughly half of the events is in the highest ten-percent energy bin from Tab. 2.2 in [25] when beamstrahlung is actually simulated.

The tables 1 and 2 contain our results for the SM cross sections of the processes of interest, before and after cuts, respectively. As argued above, the results apply to on-shell bosons in the final state and do not refer to detailed properties of the CLIC collider, with two notable exceptions that we discuss in the following.

Process	1.4 TeV	3 TeV	Factor
$W^+W^-\nu\bar{\nu}$	47.1	132	1
$W^+W^-e^+e^-$	1570	3820	1
$W^\pm Ze^\mp\nu$	138	408	0.136
ZZe^+e^-	3.78	4.70	0.019
$W^+W^-(Z \rightarrow \nu\bar{\nu})$	11.7	9.35	1
$ZZ\nu\bar{\nu}$	15.7	57.5	1
ZZe^+e^-	3.78	4.70	1
$W^\pm Ze^\mp\nu$	138	408	0.136
$W^+W^-e^+e^-$	1570	3820	0.019
$ZZ(Z \rightarrow \nu\bar{\nu})$	0.484	0.237	1

Table 1: *Standard model total cross sections in fb ($\pm 1\%$ error) without cuts for center-of-mass energies of $\sqrt{s} = 1.4 \text{ TeV}$ and 3 TeV . Both particle beams are unpolarized. Detection efficiencies and branching ratios are not included. All cross sections have to be multiplied by the factors in the fourth column to take the misidentification of vector bosons into account.*

Process	1.4 TeV	3 TeV	Factor
$W^+W^-\nu\bar{\nu}$	0.119	0.790	1
$W^+W^-e^+e^-$	0.000	0.000	1
$W^\pm Ze^\mp\nu$	0.269	1.200	0.136
ZZe^+e^-	0.000	0.000	0.019
$W^+W^-(Z \rightarrow \nu\bar{\nu})$	0.039	0.610	1
$ZZ\nu\bar{\nu}$	0.084	0.790	1
ZZe^+e^-	0.000	0.000	1
$W^\pm Ze^\mp\nu$	0.288	1.590	0.136
$W^+W^-e^+e^-$	0.000	0.000	0.019
$ZZ(Z \rightarrow \nu\bar{\nu})$	0.000	0.000	1

Table 2: *Same as Tab. 1, but with cuts.*

1. For suppressing the contribution from photon-induced processes, the analysis has to rely on the ability to detect energetic electrons in the very forward region, which are barely deflected by the photon emission. If such electrons are vetoed against, the ambiguity between W and Z/γ bosons in the initial state is greatly reduced. For the current study we have assumed that a veto against electrons is possible down to an angle of 15 mrad [54].
2. The clean environment and triggerless operation of a lepton collider allows us to detect final-state vector bosons by their decay products in essentially all channels. For the current study, we have concentrated on the hadronic decay channels. These decays provide the major part of the decay branching fractions and yield complete kinematic information. In particular, the momenta of the forward neutrinos can be inferred from the missing energy and momentum. A disadvantage of hadronic channels is the absence of charge information and the finite jet-pair invariant mass resolution, which adds on the natural decay width of W and Z bosons. As a result, there is a probability for misidentification between W and Z . We take this into account by the matrix for identification probabilities as it was determined in [55]:

$$W \rightarrow 88\% W, 12\% Z \quad (20a)$$

$$Z \rightarrow 12\% W, 88\% Z \quad (20b)$$

Partonic WW , WZ and ZZ final states therefore will be identified as a $WW(ZZ)$ event with probabilities 77.4%, 10.6%, 1.4%, which yields the weighting factors 1:0.136:0.019 given in the final column of both tables 1 and 2. Taking the hadronic W and Z boson branching ratios of 67.70% and 69.91% into account and including the di-lepton modes of the Z boson (BR=6.729% for e^+e^- and $\mu^+\mu^-$), the efficiencies for detecting a WW , WZ , ZZ pair originating from a partonic WW , WZ , ZZ final state are 35.4%, 40.1% and 45.5%, respectively.

A significant part of the $VV\nu\nu$ final state is contributed by triple vector boson production, where the third boson is a Z with invisible decay to neutrinos, cf. Fig. 3 (right). This might be considered as a separate background, and it is tempting to calculate this via a separate calculation of triple vector boson production with Z decay. However, the process is probed in a kinematical region where the would-be Z boson is far off shell. The distribution in this region cannot be defined in a gauge-invariant way if we select only diagrams with a virtual Z boson. We have compared the results of [16,17], which were obtained for this selection of Feynman diagrams using 'tHooft-Feynman gauge for the gauge bosons, with an analogous WHIZARD calculation where all amplitudes are computed in unitarity gauge. As one may expect, the two results differ by a large factor in the signal region of high $\bar{\nu}\nu$ invariant masses, while coinciding on the Z mass peak. The momentum factors in the unitarity-gauge propagators produce a gauge-dependent excess which is cancelled against a matching piece if the full gauge-invariant set of diagrams is taken into account. In tables 1 and 2, we quote the unitarity-gauge results for the three-boson subprocess for completeness, but we emphasize that after cuts, this number is unphysical and actually irrelevant for the signal sensitivity; as a background, it can be ignored for all practical purposes.

In other words, such a selection of Feynman graphs should not be attempted and a triple-boson background contribution cannot be defined. For the remainder of our study we only use results for the complete process which are gauge invariant by construction.

Besides gauge-invariance issues, we should note that the VVZ contribution to the processes of interest does not depend significantly on the coefficients of the operators in Eq. 18. This is easily understood if we remember that in the high-energy limit gauge and Goldstone bosons decouple. An intermediate off-shell Z or γ couples to a massless fermion current and therefore behaves as a gauge boson. A Goldstone boson contribution is excited only via mixing, suppressed by m_Z/\sqrt{s} . Indeed we observe that in the low-mass region for the neutrino system where the Z decay contributes, the dependence on the anomalous parameters is negligible. We can therefore cut on high VV invariant mass without losing sensitivity and thus concentrate on the genuine VBS topology. This property also removes any need for unitarizing the triple-production channel, since the SM contribution is guaranteed to respect perturbative unitarity.

6 Results for EFT Operator Coefficients

We now consider the extrapolated EFT as the most straightforward extension of the SM for VBS at high energy. We use the SM Lagrangian (17) and add the two dimension-eight operators (18) with their coefficients $F_{S,0}$ and $F_{S,1}$ as free parameters. The calculation is analogous to the LHC case [56]; for the numerical results, we use the model implementation in the WHIZARD event generator and the automatic calculation of unitarized tree-level amplitudes, distributions, and cross sections.

At low energy, the free parameters $F_{S,0}$ and $F_{S,1}$ are identified as expansion parameters in the EFT, within the range of validity of the latter.³ Where we extrapolate the EFT to high

³In the ATLAS analysis of VBS at the LHC [6], the notation (α_4, α_5) was adopted instead, borrowed from the no-Higgs EFT [45], although the theory model included the light Higgs and unitarization, i.e., worked with

energies beyond its validity range, we apply T-matrix unitarization to the calculated amplitude. The unitarization correction will set in where the extrapolated amplitude becomes strong. In effect, we obtain a smooth transition to high energy asymptotics with saturation of unitarity in all partial waves. This is a two-parameter model for a structureless strongly interacting continuum.

This expectation is confirmed by the numerical results which we display in Figs. 4, 5, 6. In the plotted distributions, we choose exemplary values for the model parameters. As in the SM results listed above, all distributions are shown for unpolarized, structureless e^+e^- beams.

The result of this calculation can be expressed in terms of exclusion contours in a two-dimensional parameter space, centered on the SM as reference point. The exclusion contours are based on the hypothesis that no deviations from the SM are observed in an experiment. Given that our estimates follow from a simple cut-based analysis, we find it sufficient to calculate a small number of parameter points and suitably interpolate. In Fig. 7, we show the results for the sensitivity to $F_{S,0}$ and $F_{S,1}$. In addition to the exclusion contours that we obtain for the W^+W^- and ZZ final states, respectively, we indicate a 90% exclusion limit that would be deduced from combining both channels. Comparing the three selected collider energies, we conclude that increasing the energy from 1 TeV to 3 TeV improves the sensitivity by roughly one order of magnitude, ultimately $\Delta F_{S,0/1} \sim 5 \text{ TeV}^{-4}$. These results may be compared to the run-I LHC limit on the same parameters, as obtained by ATLAS [7], $\Delta F_{S,0/1} \sim 500 \text{ TeV}^{-4}$ (cf. [46] for the conversion of exclusion limits).

In Fig. 8, we repeat the same analysis for an assumed beam polarization of 80% (e^-), 0% (e^+). The polarization effect enhances the signal more than the background and thus improves the sensitivity by another factor of 1.5. Finally, Fig. 9 displays the same 90% exclusion contours with polarization for all three energy values in a common plot, for convenience of the reader.

We deliberately have included only the two channels W^+W^- and ZZ . Additional information can be gained by evaluating the other possible final states. However, these channels suffer from a larger fraction of γ -induced background and add independent information only if we relax the custodial-symmetry assumption, such that W and Z states are no longer related. For the current analysis, additional channels are of minor importance.

The sensitivity range for the anomalous coupling is of the order $1/\Lambda_{\text{eff}}^4$, where the effective scale Λ_{eff} is given by the W/Z pair energy where the differential distribution is maximal, cf. Fig. 5. This is the region where the anomalous couplings have the strongest impact — at low energies, their effect is naturally suppressed, while at high energies, unitarity becomes saturated and the sensitivity disappears again. Clearly, the measurement is limited by statistics.

For the purpose of this study, we rely only on the total cross section within a fiducial phase space which is isolated by the cut strategy as described above. Further details can be deduced from the vector-boson pair invariant mass distribution, as displayed in the figures. The availability of this important observable, in form of the total hadronic energy and momentum, is a great advantage of the clean lepton-collider environment, as compared to the situation at a hadron collider.

A complete experimental analysis, which is beyond the scope of the present paper, should

the extrapolated EFT model of the present paper. For the relation of coefficients, cf. [43].

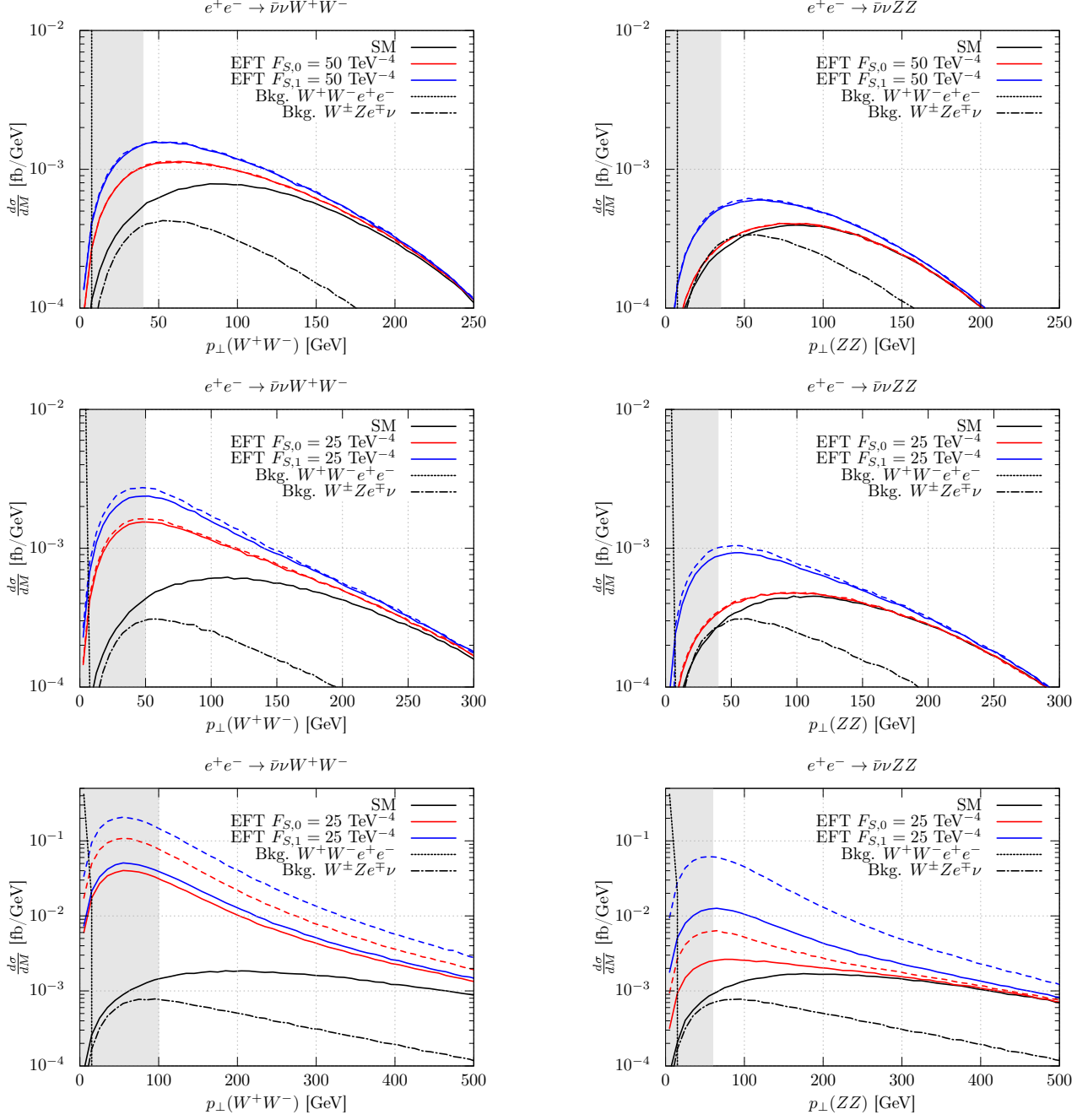


Figure 4: *Differential cross sections depending on the transverse momentum of the W (left plots) and the Z boson pair (right plots) at center-of-mass energies of 1 TeV (upper plots), 1.4 TeV (middle plots) and 3 TeV (lower plots). The solid lines show the signal process $\bar{\nu}\nu W^+W^-$ (ZZ) with SM values $F_{S,0} = F_{S,1} = 0$. The red/blue lines indicate the signal process with non SM value $F_{S,0,1} = 25/50 \text{ TeV}^{-4}$ (dashed lines: naive EFT results, solid lines: unitarized results). In addition, the two SM background processes $W^+W^-e^+e^-$ and $W^{\pm}Ze^{\mp}\nu$ (with 13.6% misidentification probability) are also plotted. The shaded area is removed by the cut on the W (Z) boson system. All other cuts have been applied as described. No detection efficiencies are included.*

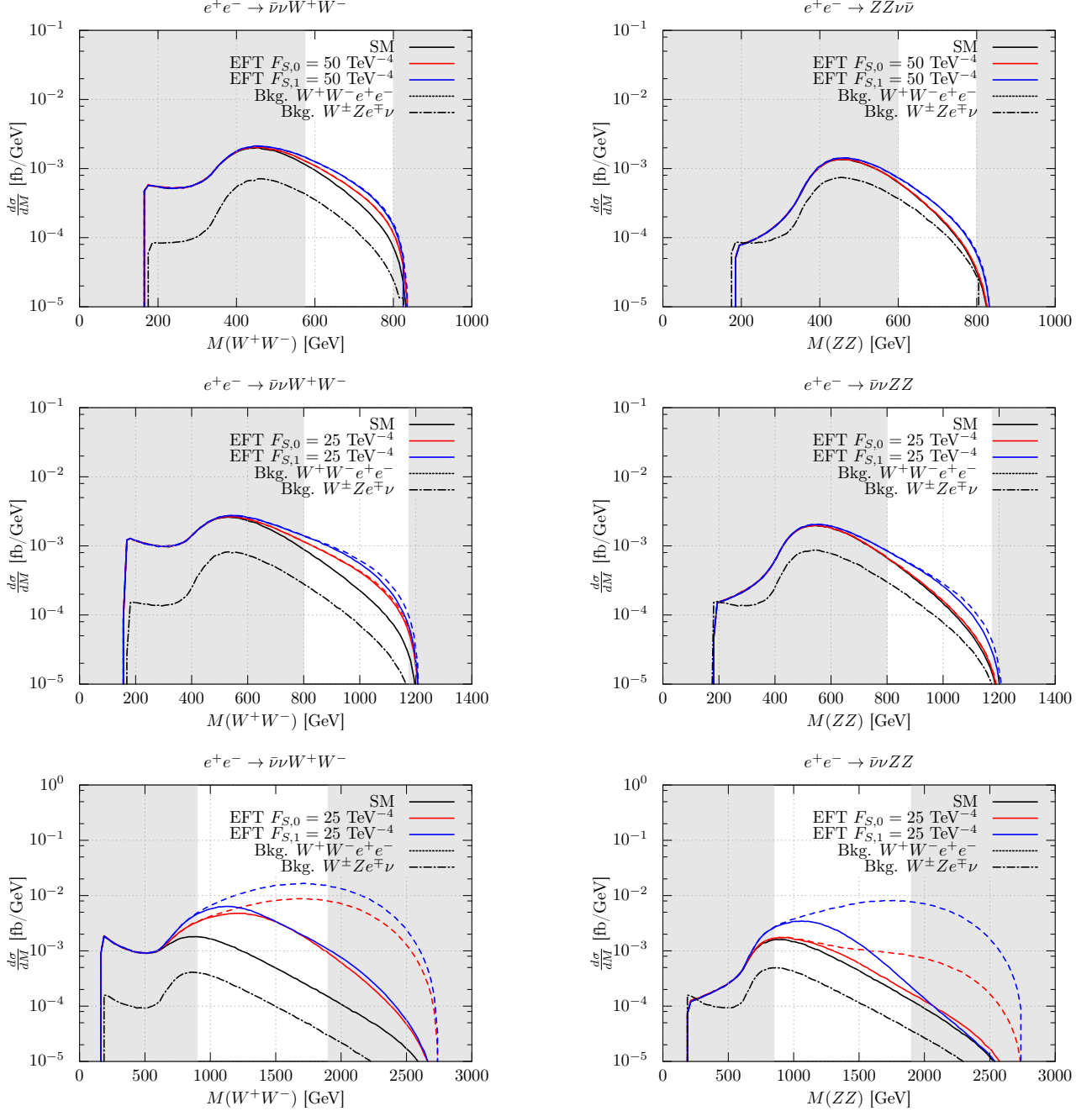


Figure 5: *Differential cross sections depending on the invariant mass of the W (left plots) and the Z boson pair (right plots) at center-of-mass energies of 1 TeV (upper plots), 1.4 TeV (middle plots) and 3 TeV (lower plots). The solid lines show the signal process $\bar{\nu}\nu W^+W^-$ (ZZ) with SM values $F_{S,0} = F_{S,1} = 0$. The red/blue lines indicate the signal process with non SM value $F_{S,0,1} = 25/50 \text{ TeV}^{-4}$ (dashed lines: naive EFT results, solid lines: unitarized results). In addition, the two SM background processes $W^+W^-e^+e^-$ and $W^\pm Ze^\mp\nu$ (with 13.6% misidentification probability) are also plotted. The shaded area is removed by the cut on the $W(Z)$ boson system. All other cuts have been applied as described. No detection efficiencies are included.*

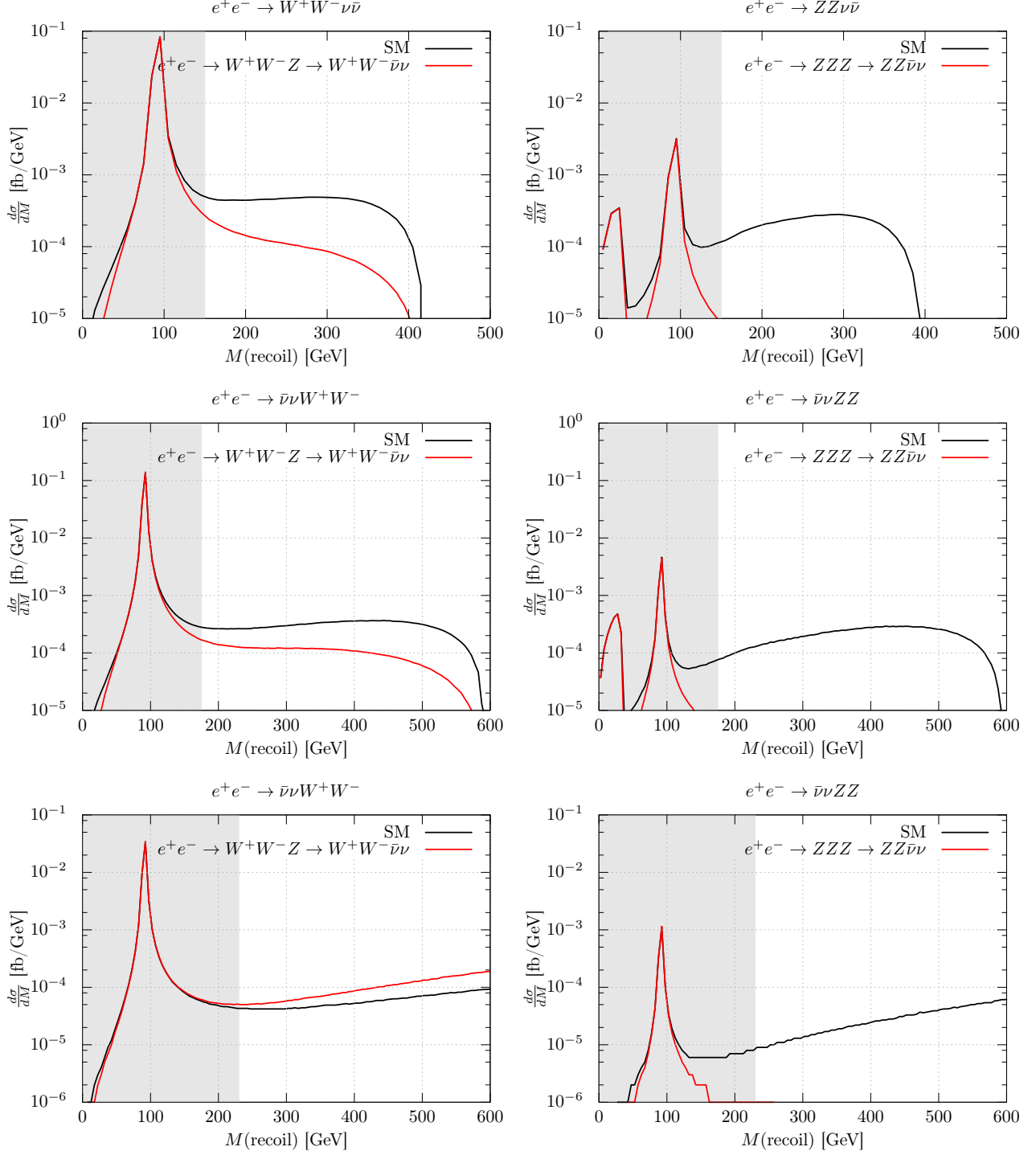


Figure 6: *Differential cross sections depending on the recoil mass of the W (left plots) and the Z boson pair (right plots) at center-of-mass energies of 1 TeV (upper plots), 1.4 TeV (middle plots) and 3 TeV (lower plots). The solid lines show the signal process $\bar{\nu}\nu W^+W^- (ZZ)$. The red lines show the background process $e^+e^- \rightarrow W^+W^-(ZZ)Z \rightarrow W^+W^-(ZZ)\nu\bar{\nu}$, where the two neutrinos are generated through a decaying Z boson. The shaded area is removed by the cut on the neutrino system. All other cuts have been applied as described above. No detection efficiencies are included.*

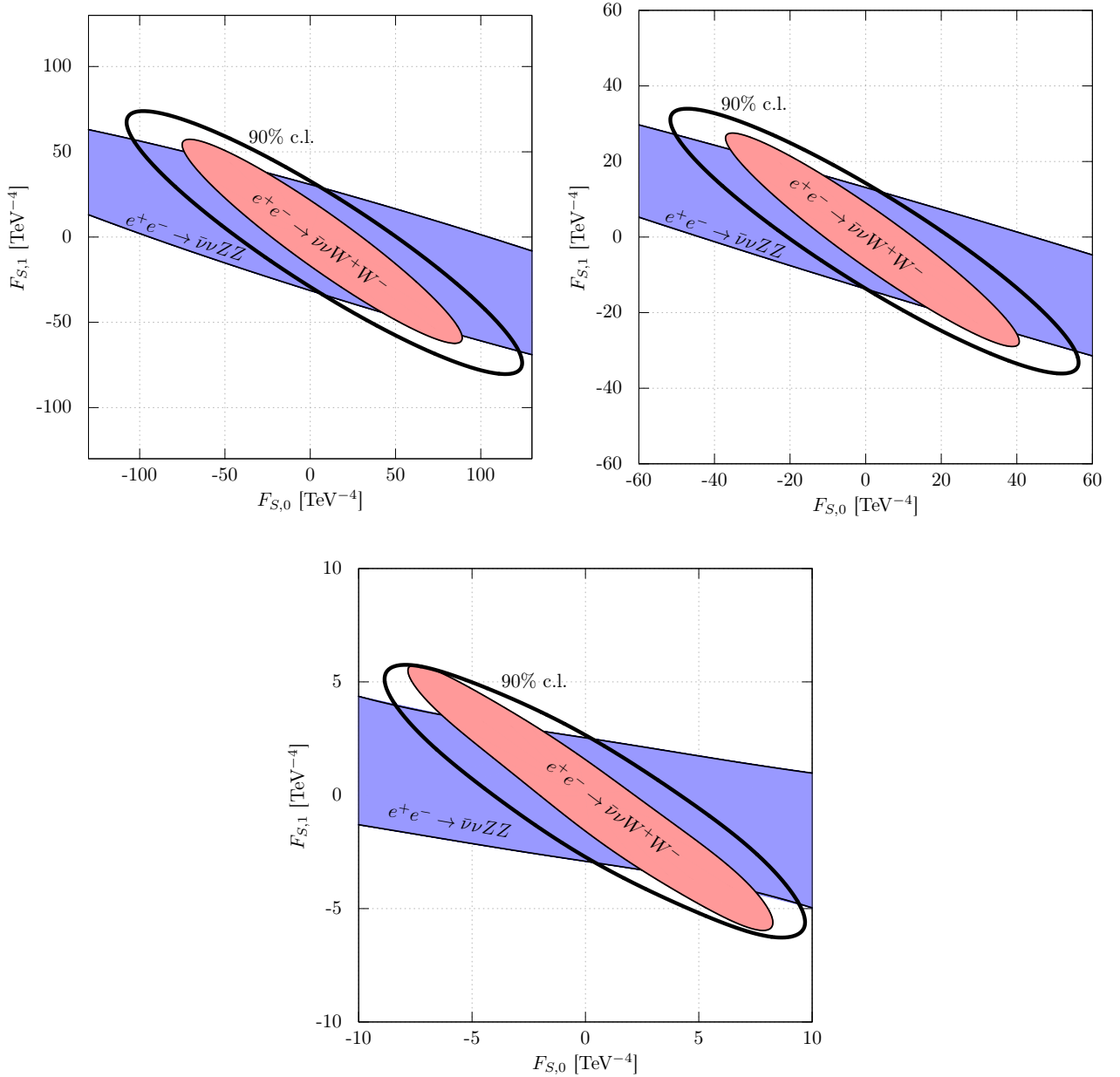


Figure 7: $\pm 1\sigma$ exclusion contours in the $F_{S,0}/F_{S,1}$ plane for the two signal processes $e^+e^- \rightarrow \bar{\nu}\nu W^+W^-$ and $e^+e^- \rightarrow \bar{\nu}\nu ZZ$ including all background processes based on the assumption $F_{S,0} = F_{S,1} = 0$. The e^- (e^+) beam is unpolarized at energies of 1.0 TeV (upper left plot), 1.4 TeV (upper right plot) and 3 TeV (lower plot). The corresponding integrated luminosities are $5 ab^{-1}$, $1.5 ab^{-1}$ and $2 ab^{-1}$, respectively. All cuts have been applied and detection efficiencies are included. The thick line indicates the 90% exclusion sensitivities obtained by the combination of the two signal channels. All cross sections are unitarized.

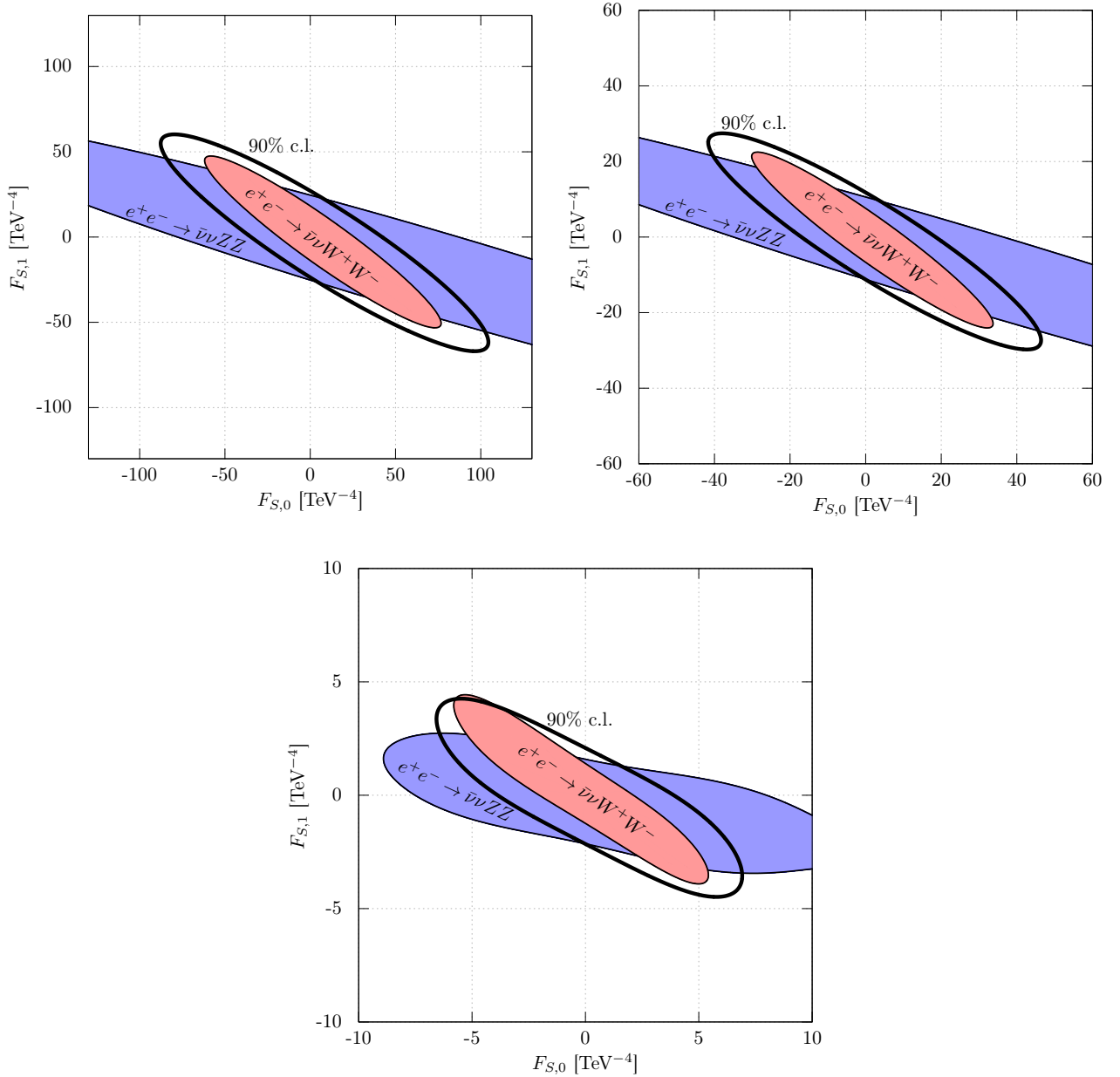


Figure 8: $\pm 1\sigma$ exclusion contours in the $F_{S,0}/F_{S,1}$ plane for the two signal processes $e^+e^- \rightarrow \bar{\nu}\nu W^+W^-$ and $e^+e^- \rightarrow \bar{\nu}\nu ZZ$ including all background processes based on the assumption $F_{S,0} = F_{S,1} = 0$. The e^- (e^+) beam is polarized at a degree of 80% (0%) at energies of 1.0 TeV (upper left plot), 1.4 TeV (upper right plot) and 3 TeV (lower plot). The corresponding integrated luminosities are 5 ab^{-1} , 1.5 ab^{-1} and 2 ab^{-1} , respectively. All cuts have been applied and detection efficiencies are included. The thick line indicates the 90% exclusion sensitivities obtained by the combination of the two signal channels. All cross sections are unitarized.

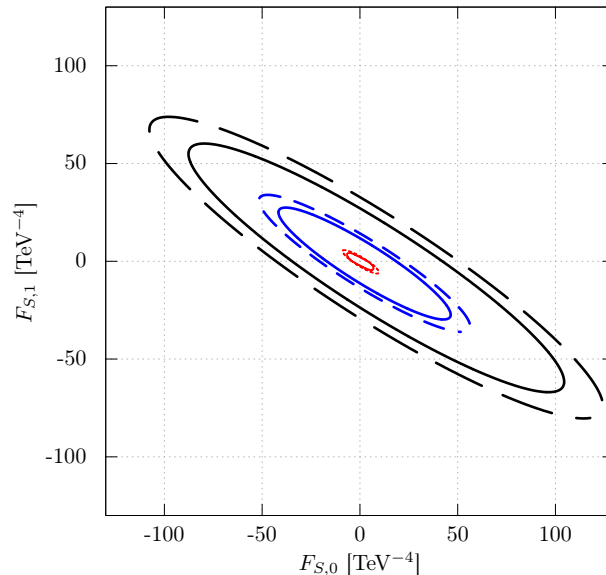


Figure 9: *90 % exclusion sensitivities for polarized (solid) and unpolarized (dashed) particle beams at energies of $\sqrt{s} = 1$ (black), 1.4 (blue), 3 TeV (red) combined, assuming integrated luminosities of 5 ab^{-1} , 1.5 ab^{-1} and 2 ab^{-1} , respectively.*

take the simulation results and apply a proper fitting procedure that takes into account all available information. Such an analysis of VBS data would exploit a complete set of observables. In particular, it will be advantageous to resolve the decay products of the vector bosons into individual jets – quarks in the language of the partonic elementary process – and take into account their angular and energy distributions. For illustration of the added value, we have generated WHIZARD event samples for the complete exclusive process $e^+e^- \rightarrow \bar{\nu}\nu + 4j$ with all possible Feynman graphs included, summed over neutrino and quark flavors, for the SM and for some nonzero values of the EFT operator coefficient $F_{S,0}$, Fig. 10.

In this figure, we show the distribution in the polar angle θ^* between the final state jets in the rest frame of the parent (off-shell) vector boson. This cut is applied at Monte Carlo truth level to both jet pairs including all combinatorics. Expanding on this result, to enhance the vector boson scattering signal further above the background, the following cut on the angle θ^* could be used (as before: first number applies for 3 TeV and the number in brackets for 1.4 TeV):

$$0.2(0.4) < |\cos(\theta^*)| < 0.75 \quad (21)$$

A more sophisticated analysis would exploit the complete information from this distribution and add in any further observable that provides discriminating power.

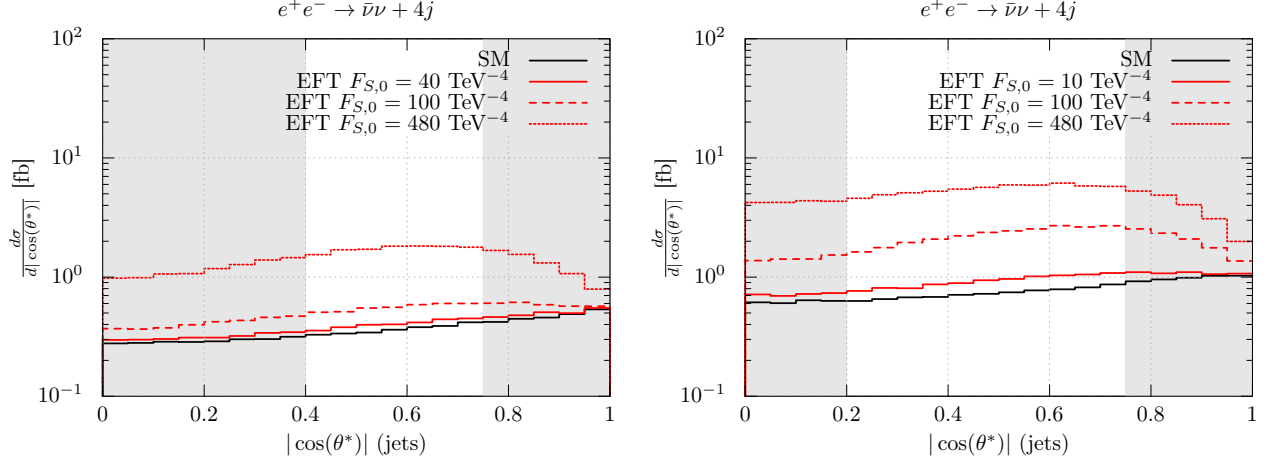


Figure 10: *Differential cross sections of the process $e^+e^-\bar{\nu} \rightarrow \nu + 4j$ at center-of-mass energies of 1.4 TeV (left plot) and 3 TeV (right plot) depending on the jet pairs $|\cos(\theta^*)|$ at different values of $F_{S,0}$. All cuts have been applied as described above. No detection efficiencies are included and all cross sections are unitarized.*

7 Results for Resonances

Besides the extrapolated EFT of the previous section, we now consider a second set of models for VBS at high energy. Starting again from the Lagrangian (17), we add a field with high mass, definite $SU(2)_L \times SU(2)_R$ quantum numbers and with a minimal coupling to a Higgs-Goldstone current in the Lagrangian, as a possible resonance. For concreteness, we adopt resonance quantum numbers and parameters that we did study for the LHC in Ref. [56], and specifically select three models, namely an isoscalar-scalar σ , an isotensor-scalar ϕ , and an isoscalar-tensor f . For each model, we introduce the resonance mass and the coupling to the Higgs current as two independent new parameters. Ignoring further decay channels, the coupling and mass also determine the width of the resonance.

The Lagrangians for the three fields σ , f , ϕ are

$$\mathcal{L}_\sigma = \frac{1}{2} \partial_\mu \sigma \partial^\mu \sigma - \frac{1}{2} m_\sigma^2 \sigma^2 + \sigma J_\sigma \quad (22a)$$

$$\mathcal{L}_\phi = \frac{1}{2} \sum_{i=s,v,t} \text{tr} [\partial_\mu \Phi_i \partial^\mu \Phi_i - m_\Phi^2 \Phi_i^2] + \text{tr} \left[\left(\Phi_t + \frac{1}{2} \Phi_v - \frac{2}{5} \Phi_s \right) J_\phi \right], \quad (22b)$$

$$\begin{aligned} \mathcal{L}_f = & \frac{1}{2} \partial_\alpha f_{\mu\nu} \partial^\alpha f^{\mu\nu} - \frac{1}{2} m^2 f_{\mu\nu} f^{\mu\nu} \\ & - \partial^\alpha f_{\alpha\mu} \partial_\beta f^{\beta\mu} - f_\alpha^\alpha \partial^\mu \partial^\nu f_{\mu\nu} - \frac{1}{2} \partial_\alpha f_\mu^\mu \partial^\alpha f_\nu^\nu + \frac{1}{2} m^2 f_\mu^\mu f_\nu^\nu + f_{\mu\nu} J_f^{\mu\nu}, \end{aligned} \quad (22c)$$

where J_σ, J_ϕ, J_f are the currents which couple to the new fields, respectively. We note that the isotensor-scalar ϕ , defined by its $SU(2)_R \times SU(2)_L$ quantum numbers $\mathbf{1} \times \mathbf{1}$, decomposes after electroweak symmetry breaking into an isotensor Φ_t , an isovector Φ_v and isoscalar Φ_s transforming under custodial $SU(2)$.

The currents that interact with the resonances are given by

$$J_\sigma = F_\sigma \text{tr} \left[(\mathbf{D}_\mu \mathbf{H})^\dagger \mathbf{D}^\mu \mathbf{H} \right], \quad (23a)$$

$$J_\phi = F_\phi \left((\mathbf{D}_\mu \mathbf{H})^\dagger \otimes \mathbf{D}^\mu \mathbf{H} + \frac{1}{8} \text{tr} \left[(\mathbf{D}_\mu \mathbf{H})^\dagger \mathbf{D}^\mu \mathbf{H} \right] \right) \tau^a \otimes \tau^a, \quad (23b)$$

$$J_f^{\mu\nu} = F_f \left(\text{tr} \left[(\mathbf{D}^\mu \mathbf{H})^\dagger \mathbf{D}^\nu \mathbf{H} \right] - \frac{c_f}{4} g^{\mu\nu} \text{tr} \left[(\mathbf{D}_\rho \mathbf{H})^\dagger \mathbf{D}^\rho \mathbf{H} \right] \right). \quad (23c)$$

For further details, cf. [56].

At low energy, each of these three distinct models reduces to a one-parameter effective theory, since a single combination of mass and coupling parameters enters into effective values of $F_{S,0}$ and $F_{S,1}$. These models therefore provide high-energy extensions of the generic low-energy EFT, as alternatives to the straightforward extrapolation of the preceding section. The resonance models exhibit more structure than the simple extrapolation. All models require unitarization, which we again implement using the T-matrix framework, since the interaction operators introduce terms that rise with energy.

If the effect of the new states is to be sizable and thus observable, the interactions should be rather strong, so generically we do not expect a renormalizable model with tree-level unitary asymptotics. Nevertheless, weakly interacting models such as a UV-complete Higgs-singlet model are included in this model space. For a renormalizable model, any terms that apparently rise with energy would cancel against higher-order contributions. From a phenomenological perspective, renormalizable models are exceptional points in a larger parameter space that we cover by the above definitions.

In Fig. 12, we display the vector-boson pair invariant mass distribution for the SM with an additional isoscalar scalar resonance σ , equivalent to an extra Higgs-like singlet boson. The plots show both the W^+W^- final state (left column) and the ZZ final state (right column). We have chosen a moderately high mass of $M_\sigma = 800$ GeV and a rather small width of $\Gamma_\sigma = 80$ GeV (blue curve). The distribution, which for the full process translates into the invariant mass of the hadronic (four-jet) system, shows an unambiguous peak at the resonance mass that is distinguishable in shape from the SM background (black), given sufficient luminosity. The peak is more pronounced for 3 TeV collider energy, but also clearly visible for 1.4 TeV. It is evident that for this choice of parameters, the formally correct EFT expansion (red curve) does not approximate the actual model behavior at all. Unitarization does not play a significant role except for the naively extrapolated EFT (dashed red) which overshoots the unitarized curves (solid), and thus the unitarity bounds, by a substantial amount.

The plots in Fig. 12 depict a somewhat lighter isoscalar-scalar resonance ($M_\sigma = 650$ GeV) with a larger width ($\Gamma_\sigma = 260$ GeV). In this case, the resonance shape follows the shape of the extrapolated EFT but leads to a significantly larger peak cross section. Since the equivalent EFT parameter, matching to the slope of the resonance curve below threshold, is twice as large as in the previous set of plots, the unphysical behavior is evident that we would get without unitarization (dashed curves). This applies not just to the EFT approximation (red), but also to the resonance curves (blue).

In Fig 13, we consider a isoscalar tensor resonance with $M_f = 1$ TeV and $\Gamma_f = 100$ GeV, which produces a rather narrow peak in all distributions. With a collider energy of 3 TeV, we

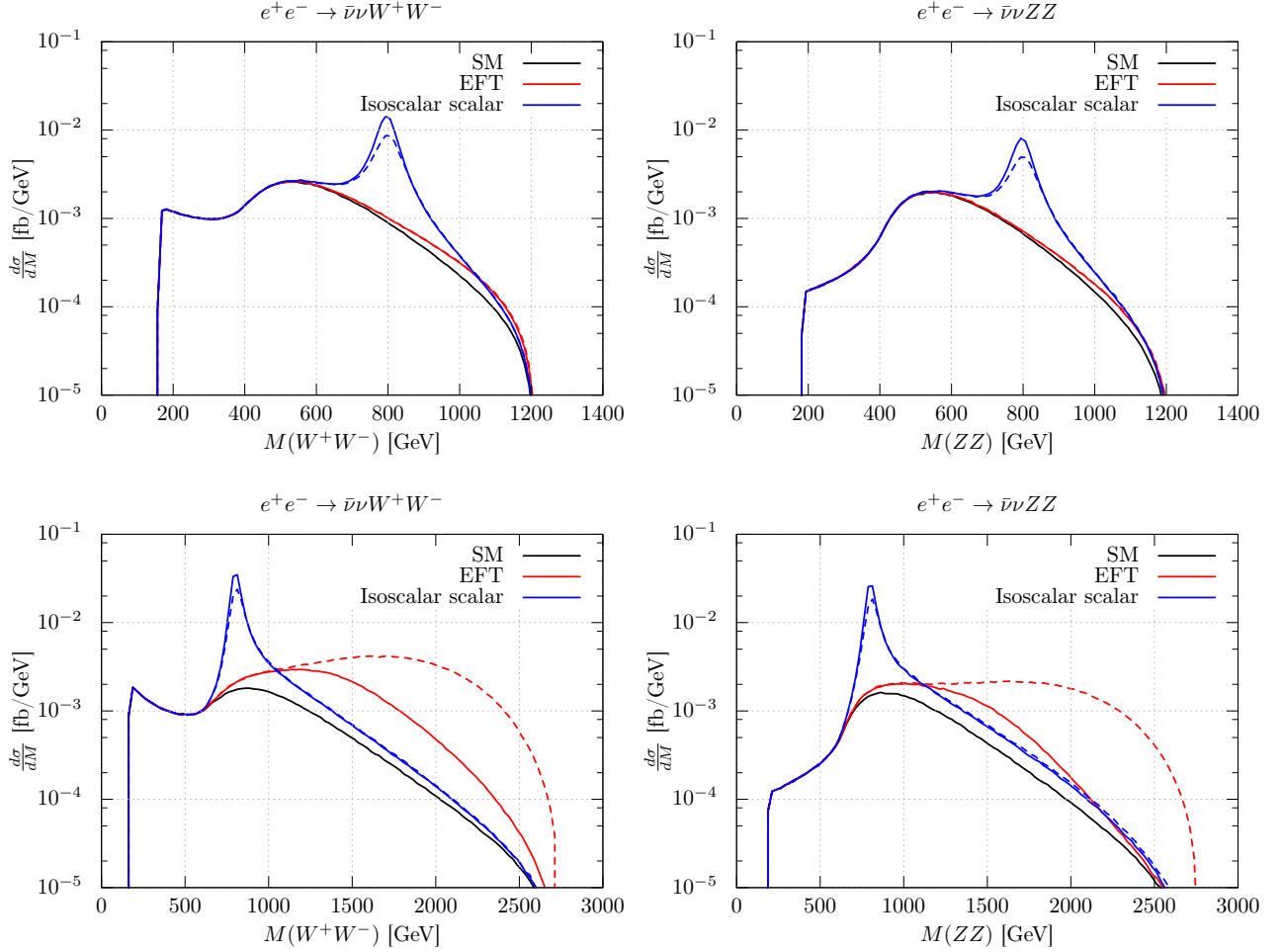


Figure 11: *Differential cross sections including a weakly coupled isoscalar scalar resonance ($m_\sigma = 800$ GeV, $F_\sigma = 4.0$ TeV $^{-1}$, $\Gamma_\sigma = 80$ GeV) depending on the invariant mass of the vector boson pair at center-of-mass energies of $\sqrt{s} = 1.4$ TeV (upper plots) and $\sqrt{s} = 3$ TeV (lower plots). Plots on the left show the process $e^+e^- \rightarrow \bar{\nu}\nu W^+W^-$, plots on the right $e^+e^- \rightarrow \bar{\nu}\nu ZZ$. Blue line: isoscalar scalar resonance, red line: matched EFT results ($F_{S,0} = 0$, $F_{S,1} = 12.3$ TeV $^{-4}$). Solid line: unitarized results, dashed line: naive results.*

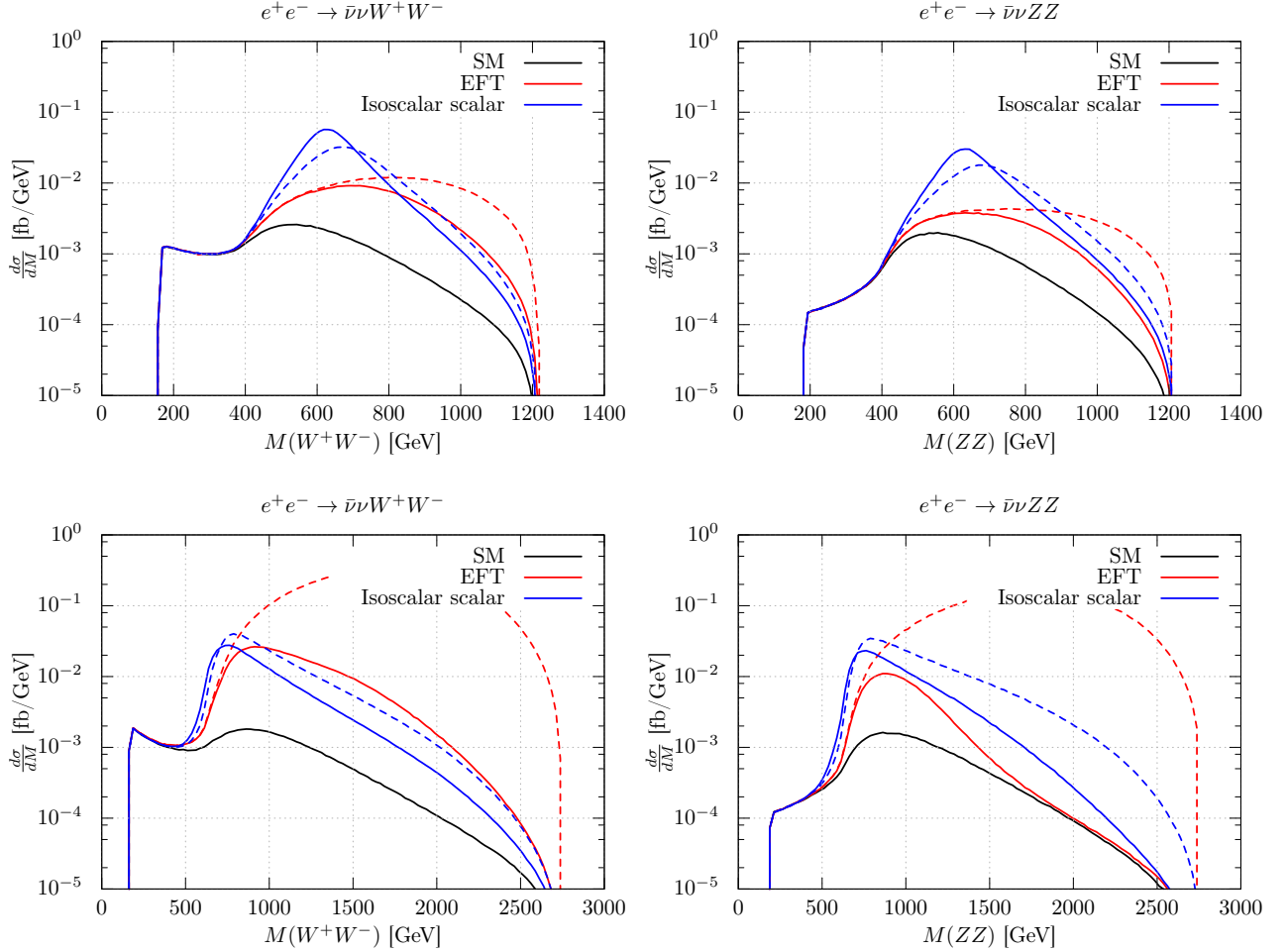


Figure 12: *Differential cross sections including a low lying isoscalar scalar resonance ($m_\sigma = 650$ GeV, $F_\sigma = 9.8$ TeV $^{-1}$, $\Gamma_\sigma = 260$ GeV) depending on the invariant mass of the vector boson pair at center-of-mass energies of $\sqrt{s} = 1.4$ TeV (upper plots) and $\sqrt{s} = 3$ TeV (lower plots). Plots on the left show the process $e^+e^- \rightarrow \bar{\nu}\nu W^+W^-$, plots on the right $e^+e^- \rightarrow \bar{\nu}\nu ZZ$. Blue line: isoscalar scalar resonance, red line: matched EFT results ($F_{S,0} = 0$, $F_{S,1} = 112.6$ TeV $^{-4}$). Solid line: unitarized results, dashed line: naive results.*

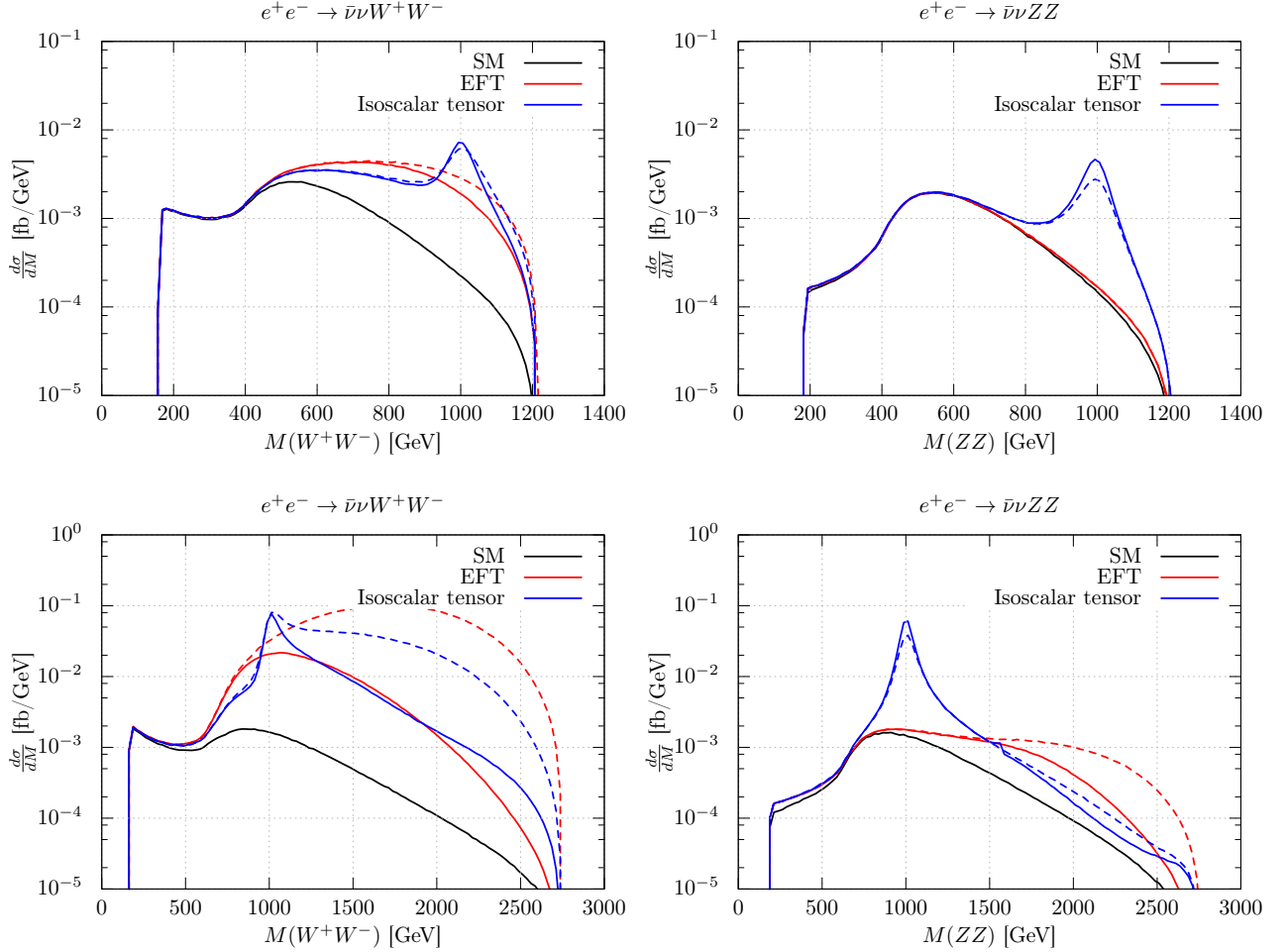


Figure 13: *Differential cross sections including an isoscalar tensor resonance ($m_f = 1000 \text{ GeV}$, $F_f = 17.4 \text{ TeV}^{-1}$, $\Gamma_f = 100 \text{ GeV}$) depending on the invariant mass of the vector boson pair at center-of-mass energies of $\sqrt{s} = 1.4 \text{ TeV}$ (upper plots) and $\sqrt{s} = 3 \text{ TeV}$ (lower plots). Plots on the left show the process $e^+e^- \rightarrow \bar{\nu}\nu W^+W^-$, plots on the right $e^+e^- \rightarrow \bar{\nu}\nu ZZ$. Blue line: isoscalar tensor resonance, red line: matched EFT results ($F_{S,0} = 150.8 \text{ TeV}^{-4}$, $F_{S,1} = -50.3 \text{ TeV}^{-4}$). Solid line: unitarized results, dashed line: naive results.*

observe the necessity for unitarization beyond the mass peak (in the WW final state), caused by the dimensionality of the effective tensor-scalar interaction. As well as in all other cases, if we had a UV-complete model at hand, we would expect any variation of the resonance-model prediction (blue) in this range: further resonances, a featureless continuum, or suppression that accommodates the emergence of further inelastic channels. However, neither of these scenarios could produce a unitarity-violating result like the naive blue-dashed line, so the unitarized model prediction serves as a conservative estimate of the asymptotic shape.

The final parameter set in Fig. 14, an isotensor-scalar multiplet ϕ , illustrates a possible strongly interacting multi-Higgs scenario. The broad resonance, actually a combination of resonance exchange in all isospin channels, is indistinguishable from an arbitrary continuum. It is remarkable that the EFT approximation follows the shape of the resonance model in the WW final state but fails completely for the ZZ final state. As before, the naive extrapolations (dashed) overshoot the unitarized models (solid) by a large amount.

8 Conclusions

We have performed a new study of the capability of a high-energy lepton collider (such as CLIC or an upgraded ILC) to measure quasi-elastic vector-boson scattering, as a dedicated probe of the Higgs sector. For realistic luminosity-energy combinations, we cannot restrict the investigation to a pure effective field theory (EFT), but have to take into account strong interactions or resonant behavior. Specifically, we have considered a straightforwardly extrapolated EFT Lagrangian and related this to alternative models where the anomalous effects develop into resonances within the kinematical range.

Our phenomenological scenarios all reduce to the Standard Model with leading higher-dimensional corrections at the low-energy threshold for vector boson scattering processes, but run into unitarity saturation at high energy or on a resonance peak. The T-matrix unitarization framework lets us handle this issue by a universal algorithm and simultaneously allows us to embed the models in a full off-shell calculation and Monte-Carlo simulation. For the purpose of working with fully exclusive event samples, all models have been implemented in the public version of the WHIZARD Monte-Carlo event generator.

The results yield an overview over the experimental reach of the CLIC and ILC colliders in the various scenarios. Using optimized cuts for longitudinal vector boson scattering, we generically obtain a sensitivity on the extrapolated EFT parameters $F_{S,0}$ and $F_{S,1}$ of $O(1/\Lambda^4)$, where Λ indicates the location of the maximum of the unitarized cross section, in terms of the vector-boson pair invariant mass as the relevant energy scale. Regarding resonance models, we have restricted ourselves to a few exemplary parameter points in this exploratory study, which should be representative of the phenomenology that can be expected. For precise and systematic parameter determinations, the specific models should be subject to an experimental fitting procedure and analysis which takes into account complete event information and weighs the distributions according to their sensitivity to the specific model in question.

The expected sensitivity of the CLIC collider with 3 TeV, as expressed for the parameters of the extrapolated EFT as the simplest model, improves over the current LHC limits by

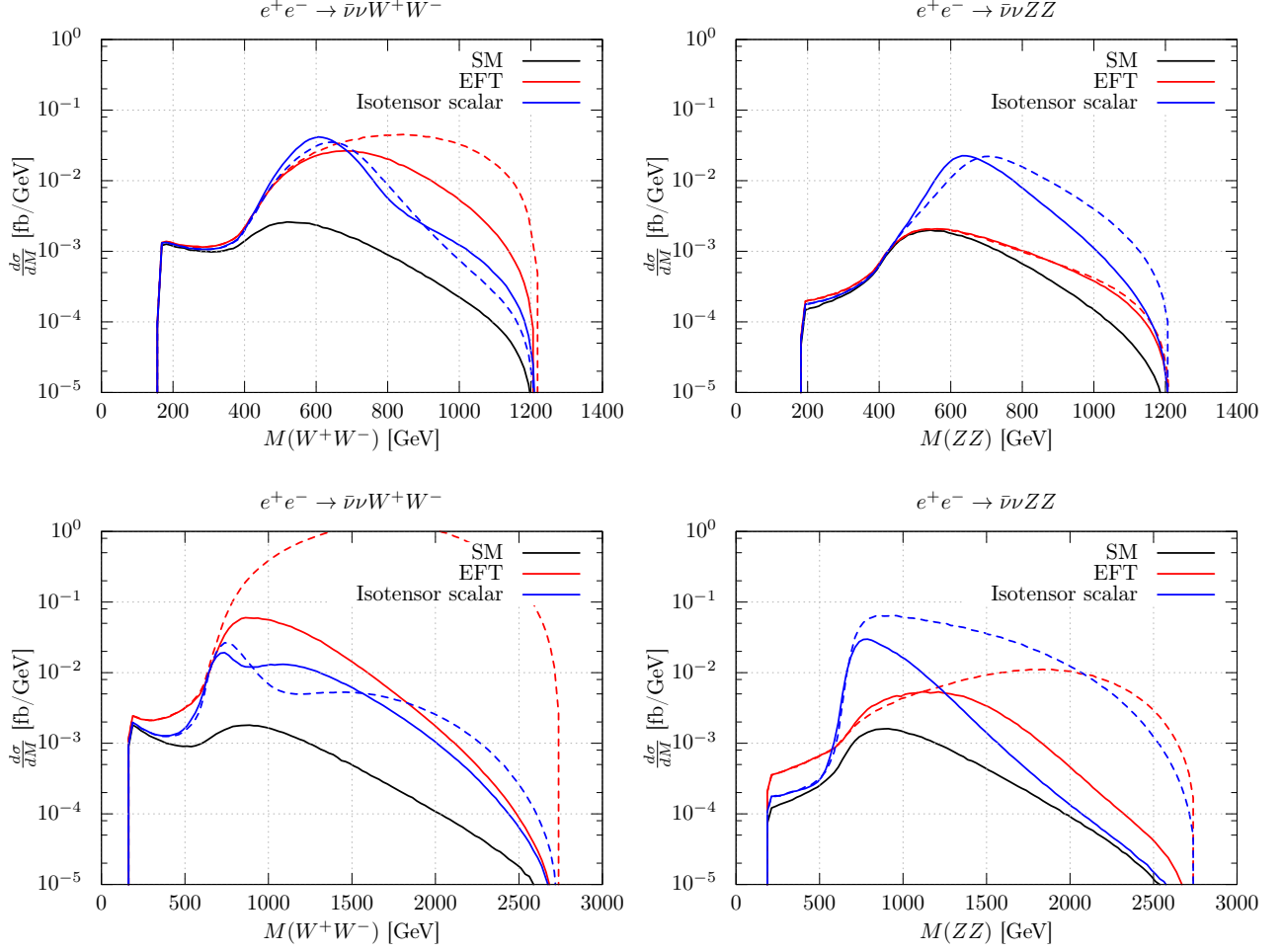


Figure 14: *Differential cross sections including a low lying isotensor scalar resonance ($m_\phi = 650$ GeV, $F_\phi = 19.5$ TeV $^{-1}$, $\Gamma_\phi = 260$ GeV) depending on the invariant mass of the vector boson pair at center-of-mass energies of $\sqrt{s} = 1.4$ TeV (upper plots) and $\sqrt{s} = 3$ TeV (lower plots). Plots on the left show the process $e^+e^- \rightarrow \bar{\nu}\nu W^+W^-$, plots on the right $e^+e^- \rightarrow \bar{\nu}\nu ZZ$. Blue line: isotensor scalar resonance, red line: matched EFT results ($F_{S,0} = 450.5$ TeV $^{-4}$, $F_{S,1} = -112.6$ TeV $^{-4}$). Solid line: unitarized results, dashed line: naive results.*

two orders of magnitude. Clearly, the CLIC expectation has to be compared to the ultimate precision achievable by the LHC experiments. A detailed comparison of sensitivities would require applying the available analysis techniques to a full-simulation prediction for either collider, which is beyond the scope of the present paper. However, the e^+e^- environment allows for the detection of well-defined final states, hadronic decays, and a direct measurement of the most relevant distribution – the vector-boson pair invariant mass – and thus remains the preferred setup for a comprehensive study of VBS in the TeV energy range.

Acknowledgments

We would like to thank Lucie Linssen, Philipp Roloff and Marcel Vos for enlightening discussions on the CLIC project. MS acknowledges the support of BMBF Verbundforschung (HEP Theory).

A Dimension-8 Operators that Affect VBS

The following list of dimension-8 operators includes all leading interactions that modify the SM form of VBS interactions. In the current paper, we restrict the investigation to the first set of operators which describes genuine Goldstone-Higgs self-interactions, which for completeness we repeat here from 18:

$$\mathcal{L}_{S,0} = F_{S,0} \text{tr} \left[(\mathbf{D}_\mu \mathbf{H})^\dagger \mathbf{D}_\nu \mathbf{H} \right] \text{tr} \left[(\mathbf{D}^\mu \mathbf{H})^\dagger \mathbf{D}^\nu \mathbf{H} \right], \quad (24a)$$

$$\mathcal{L}_{S,1} = F_{S,1} \text{tr} \left[(\mathbf{D}_\mu \mathbf{H})^\dagger \mathbf{D}^\mu \mathbf{H} \right] \text{tr} \left[(\mathbf{D}_\nu \mathbf{H})^\dagger \mathbf{D}^\nu \mathbf{H} \right]. \quad (24b)$$

Exchanging two covariant derivatives with field strength tensors, further possibilities arise to construct linearly independent operators

$$\mathcal{L}_{M,0} = -g^2 F_{M,0} \text{tr} \left[(\mathbf{D}_\mu \mathbf{H})^\dagger (\mathbf{D}^\mu \mathbf{H}) \right] \text{tr} [\mathbf{W}_{\nu\rho} \mathbf{W}^{\nu\rho}], \quad (25a)$$

$$\mathcal{L}_{M,1} = -g^2 F_{M,1} \text{tr} \left[(\mathbf{D}_\mu \mathbf{H})^\dagger (\mathbf{D}^\rho \mathbf{H}) \right] \text{tr} [\mathbf{W}_{\nu\rho} \mathbf{W}^{\nu\mu}], \quad (25b)$$

$$\mathcal{L}_{M,2} = -g'^2 F_{M,2} \text{tr} \left[(\mathbf{D}_\mu \mathbf{H})^\dagger (\mathbf{D}^\mu \mathbf{H}) \right] \text{tr} [\mathbf{B}_{\nu\rho} \mathbf{B}^{\nu\rho}], \quad (25c)$$

$$\mathcal{L}_{M,3} = -g'^2 F_{M,3} \text{tr} \left[(\mathbf{D}_\mu \mathbf{H})^\dagger (\mathbf{D}^\rho \mathbf{H}) \right] \text{tr} [\mathbf{B}_{\nu\rho} \mathbf{B}^{\nu\mu}], \quad (25d)$$

$$\mathcal{L}_{M,4} = -gg' F_{M,4} \text{tr} \left[(\mathbf{D}_\mu \mathbf{H})^\dagger \mathbf{W}_{\nu\rho} (\mathbf{D}^\mu \mathbf{H}) \mathbf{B}^{\nu\rho} \right], \quad (25e)$$

$$\mathcal{L}_{M,5} = -gg' F_{M,5} \text{tr} \left[(\mathbf{D}_\mu \mathbf{H})^\dagger \mathbf{W}_{\nu\rho} (\mathbf{D}^\rho \mathbf{H}) \mathbf{B}^{\nu\mu} \right], \quad (25f)$$

$$\mathcal{L}_{M,7} = -g^2 F_{M,7} \text{tr} \left[(\mathbf{D}_\mu \mathbf{H})^\dagger \mathbf{W}_{\nu\rho} \mathbf{W}^{\nu\mu} (\mathbf{D}^\rho \mathbf{H}) \right]. \quad (25g)$$

Here, we kept the numbering analogue to the linear Higgs doublet representation in [43] for future comparisons, where some linear dependent operators of [41] are already omitted.

Operators affecting only the gauge bosons consist of four electroweak field strength tensors

$$\mathcal{L}_{T,0} = g^4 F_{T,0} \text{tr} [\mathbf{W}_{\mu\nu} \mathbf{W}^{\mu\nu}] \text{tr} [\mathbf{W}_{\alpha\beta} \mathbf{W}^{\alpha\beta}], \quad (26a)$$

$$\mathcal{L}_{T,1} = g^4 F_{T,1} \text{tr} [\mathbf{W}_{\alpha\nu} \mathbf{W}^{\mu\beta}] \text{tr} [\mathbf{W}_{\mu\beta} \mathbf{W}^{\alpha\nu}], \quad (26b)$$

$$\mathcal{L}_{T,2} = g^4 F_{T,2} \text{tr} [\mathbf{W}_{\alpha\mu} \mathbf{W}^{\mu\beta}] \text{tr} [\mathbf{W}_{\beta\nu} \mathbf{W}^{\nu\alpha}], \quad (26c)$$

$$\mathcal{L}_{T,5} = g^4 F_{T,5} \text{tr} [\mathbf{W}_{\mu\nu} \mathbf{W}^{\mu\nu}] \text{tr} [\mathbf{B}_{\alpha\beta} \mathbf{B}^{\alpha\beta}], \quad (26d)$$

$$\mathcal{L}_{T,6} = g^4 F_{T,6} \text{tr} [\mathbf{W}_{\alpha\nu} \mathbf{W}^{\mu\beta}] \text{tr} [\mathbf{B}_{\mu\beta} \mathbf{B}^{\alpha\nu}], \quad (26e)$$

$$\mathcal{L}_{T,7} = g^4 F_{T,7} \text{tr} [\mathbf{W}_{\alpha\mu} \mathbf{W}^{\mu\beta}] \text{tr} [\mathbf{B}_{\beta\nu} \mathbf{B}^{\nu\alpha}], \quad (26f)$$

$$\mathcal{L}_{T,8} = g^4 F_{T,8} \text{tr} [\mathbf{B}_{\mu\nu} \mathbf{B}^{\mu\nu}] \text{tr} [\mathbf{B}_{\alpha\beta} \mathbf{B}^{\alpha\beta}], \quad (26g)$$

$$\mathcal{L}_{T,9} = g^4 F_{T,9} \text{tr} [\mathbf{B}_{\alpha\mu} \mathbf{B}^{\mu\beta}] \text{tr} [\mathbf{B}_{\beta\nu} \mathbf{B}^{\nu\alpha}]. \quad (26h)$$

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